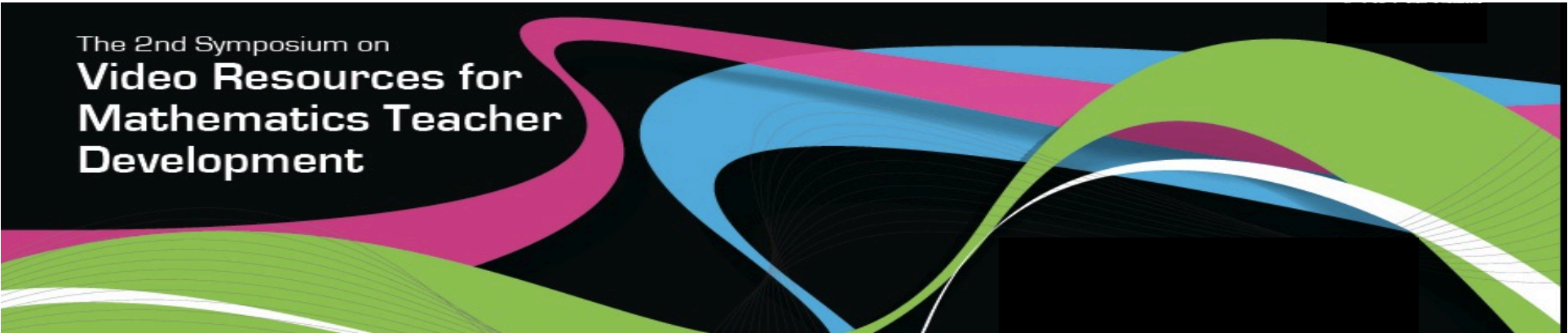


# **Potentials and limits for the use of videos in professional development at scale:**

## **The case of learning scaffolding**

The 2nd Symposium on  
**Video Resources for  
Mathematics Teacher  
Development**



# Specific challenge for the use of videos: Scaling up

## Formerly in our work:

- often used videos for PD (professional development) in joint reflections of own practice (kind of lesson study) and simulations  
(Ball 1993, Sherin et al. 2009: Video clubs)
- successful “boutique projects” with face-to-face-facilitation and many intuitive ad hoc decisions



## New challenge for us: PD at scale

- > 500 preservice teachers every year
- nation-wide programs, ideally for about 90 000 inservice math teachers and 500-1000 PD facilitators
- scaling up needs own strategies and considerations  
(Clark, Wilson, Hoyles, Noss 2013; Levin 2008; Schneider & MacDonald 2007)



DZLM 

→ need for **robust** video-assisted PD modules with more explicit support and a priori defined content

## Selected goal: learning scaffolding

---

### Approach for research-based design of video-assisted modules:

- not „what can the technique do“ (as warned by Seago 2000, Sherin 2004)
- but starting from identifying a goal, subgoals and concrete demands

(as suggested by Blomberg, Sherin et al. 2013)

### Selected goal: teachers learn to offer interactional scaffolding

- Definition of interactional scaffolding:  
teachers' practice of supporting learning in interactions  
by which students gradually become more involved in practices or understandings

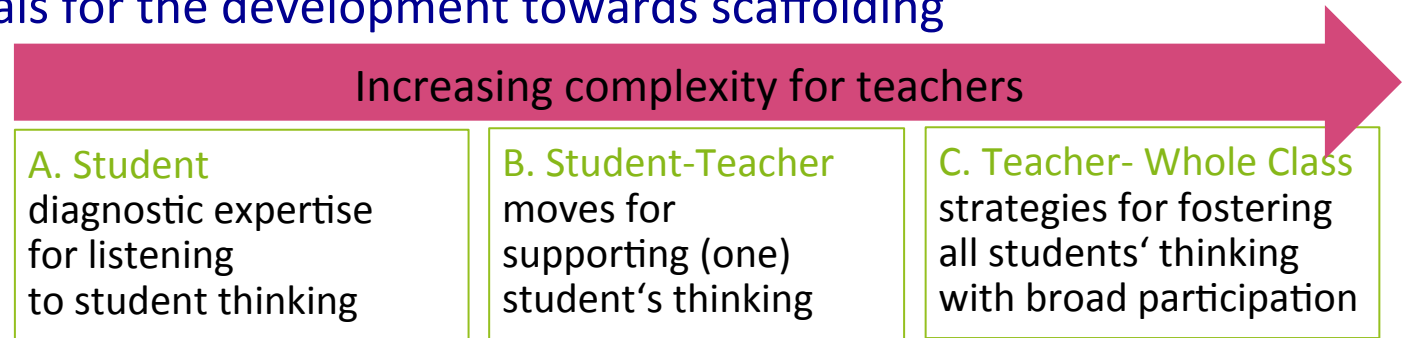
(Wood, Bruner, & Ross, 1976, p. 90, Anghileri 2006, Sleep & Boerst 2013)

- not only in one-by-one-situations, but also in whole class discussions

Interactional scaffolding is a specific challenge for scaling up  
since it is hardly material-based!!

# Steps for research-based design of video-assisted PD modules

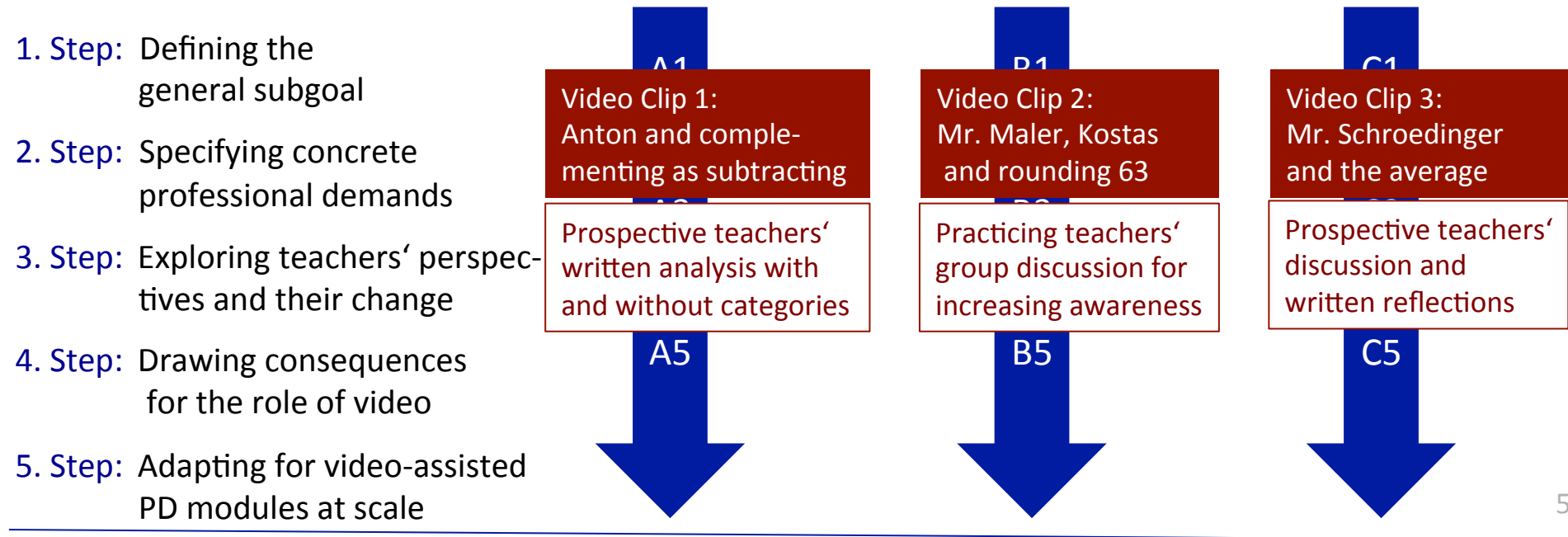
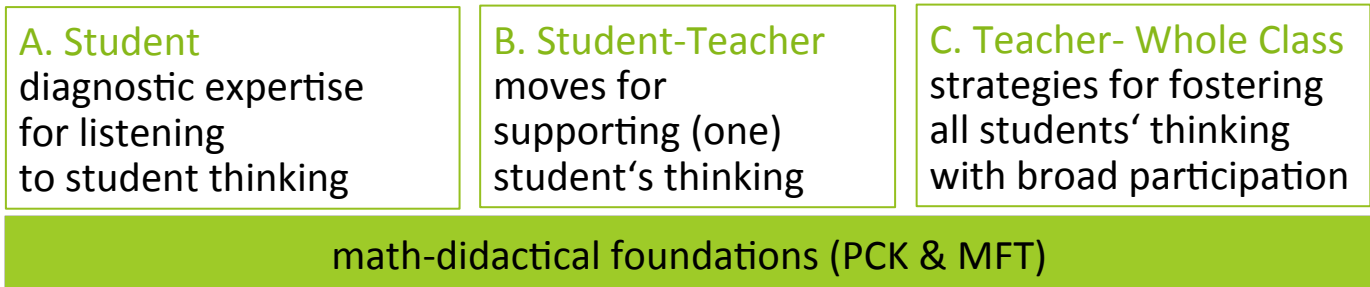
Three identified subgoals for the development towards scaffolding



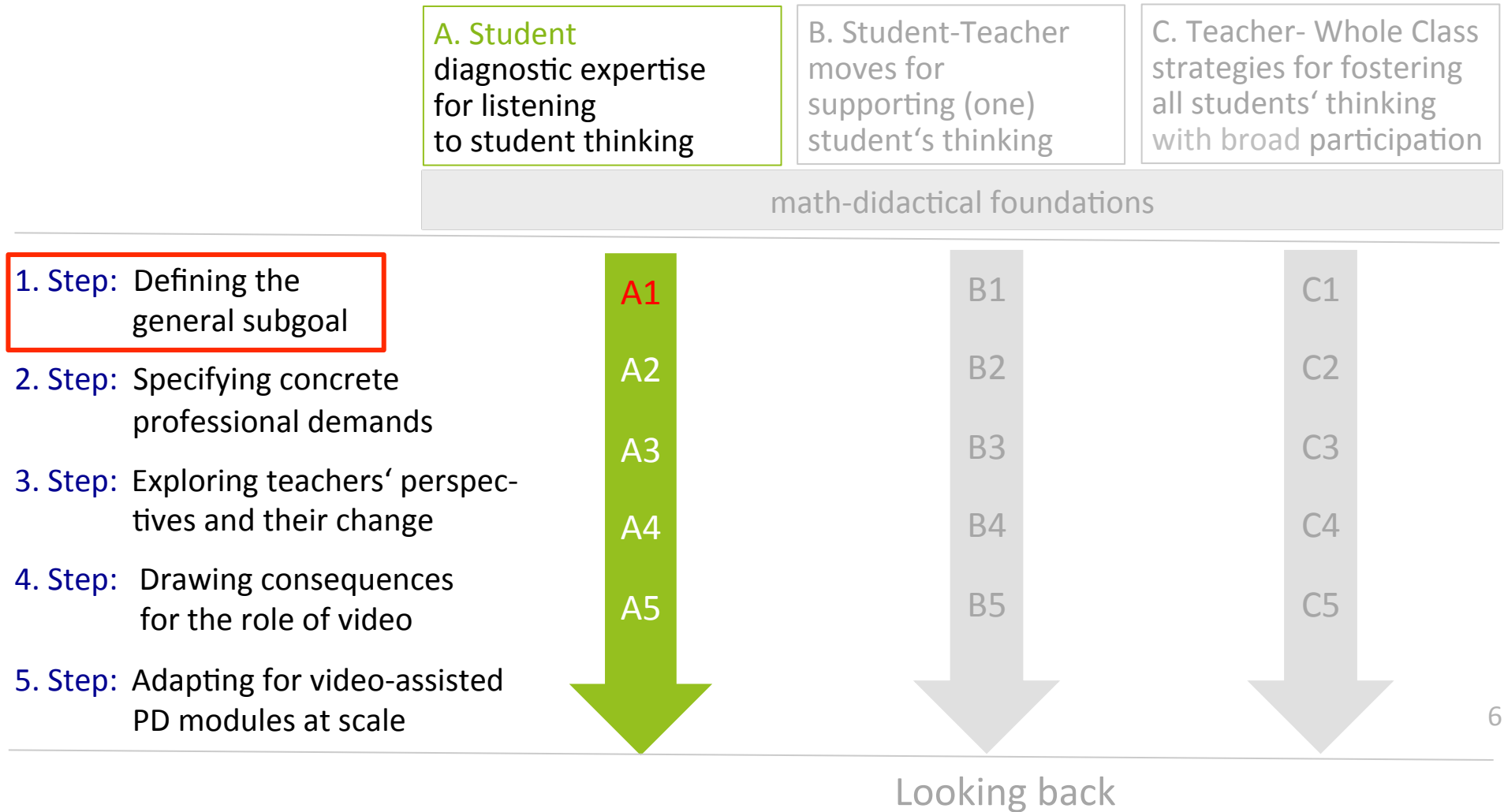
## Steps for each subgoal:

1. Step: Defining the general subgoal
2. Step: Specifying concrete professional demands
3. Step: Exploring teachers' perspectives and their change
4. Step: Drawing consequences for the role of video
5. Step: Adapting for video-assisted PD modules at scale

# Structure of the talk



# Structure of the talk



# A1. Defining the subgoal “diagnostic expertise”

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Diagnostic expertise (Prediger 2010)

(1) Interest in student thinking (not deficit-oriented)

(2) Interpretative attitude: (Jungwirth et al. 2001)

- nondirective listening (Empson & Jacobs 2008)
- decentering the judgments (Arcavi & Schoenfeld 2008)

(3) General knowledge on learning processes

(4) Domain-specific math-didactical knowledge:

- unpacking mathematical aspects (Morris, Hiebert, & Spitzer 2009)
- unpacking didactical aspects (Prediger et al. 2012)

math-didactical categories are needed to see, unpack and decenter thinking

## A2. Specifying concrete professional demands re diagnostic expertise

The african grey parrot can grow up to 40 cm long.  
A flamingo measures about 2 m, thus 200 cm.  
How many times is the flamingo bigger than the grey parrot?

Video Clip 1:  
Anton and  
complementing as subtracting

- 1 A There...  $40 \cdot 200$ ?
- 2 I How did you find that?
- 3 A No, or, I would, or 40 divided by 200.
- 4 A I have to watch, actually. Wait...
- 5 I Yeah, think about it.
- 6 A [*16 sec break*] well, 160, well 1,60 m is he bigger, the Flamingo. I know that.  
I can remember that. [*writes 160*]
- 7 I Yes, write it down, though.
- 8 A And I have calculated this in ...  
Well, I have ... complemented.
- 9 I Mhm.
- 10 A How do you make the complement sign?
- 11 I Either, you can write plus anyway...
- 12 A Ok, I can ... [*writes  $40 + 60 + 100 = 160$* ]

200

(Video by N. Renk 2008, 1:55 min, analysed in Prediger 2009)



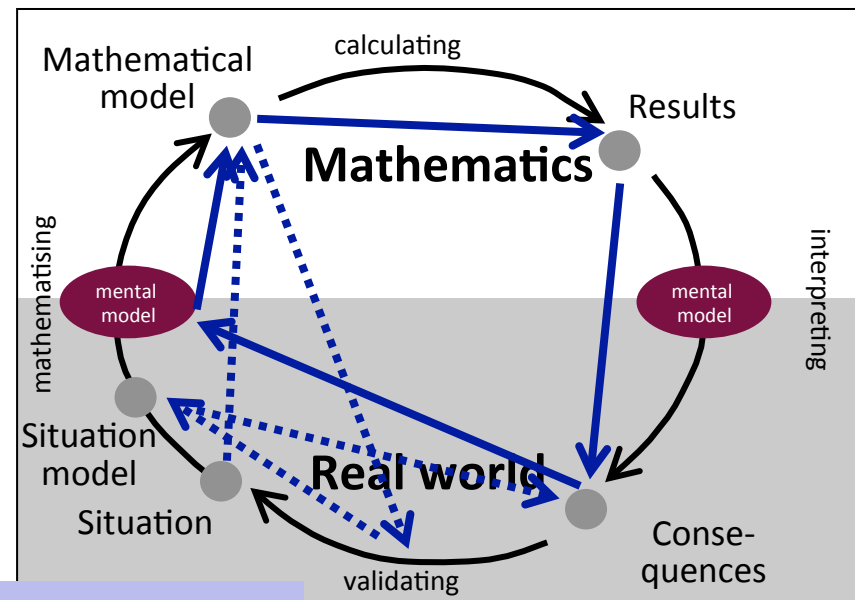
## A2. Specifying concrete professional demands re diagnostic expertise

Video Clip 1: Anton and complementing as subtracting

- 1 A There...40 · 200?
- 2 I How did you find that?
- 3 A No, or, I would, or 40 divided by 200.
- 4 A I have to watch, actually. Wait...
- 5 I Yeah, think about it.
- 6 A [16 sec break] well, 160, well 1,60 m is he bigger, the Flamingo. I know that.  
I can remember that. [writes 160]
- 7 I Yes, write it down, though.
- 8 A And I have calculated this in ...  
Well, I have ... complemented.
- 9 I Mhm.
- 10 A How do you make the complement sign?
- 11 I Either, you can write plus anyway...
- 12 A Ok, I can ... [writes  $40 + 60 + 100 = 160$ ]
- ...
- 19 I Hm, the question was  
"how many TIMES bigger"

$$200 - 40 = 160$$

$$40 + 60 + 100 = \cancel{160} \quad 200$$



Grey parrot 40 cm, Flamingo 200 cm [...] How many times is the flamingo bigger than the grey parrot?

160 cm

## A2. Specifying concrete professional demands re diagnostic expertise – job analysis

### Math-didactical categories for

#### ... unpacking student thinking

- Anton's iterative approach to solution  
 ← cognitive activities in modelling cycle
- formalizing is more difficult for Anton than finding result 160  
 ← missing mental model for complementing as subtracting

#### ... decentering the judgments

- Anton's mathematization is coherent to his individual situation model "determining the distance"
- $40 + 60 + 100 = 160$  as suitable protocol for thinking, but deviant meaning of equal sign

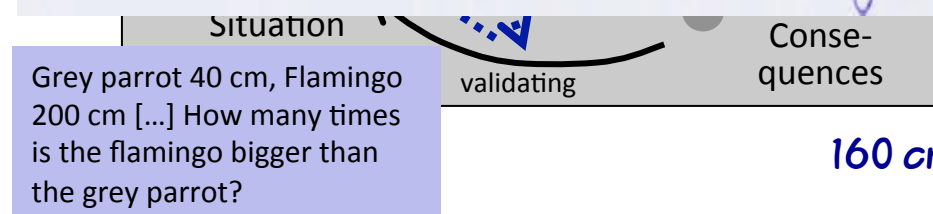
Video Clip 1: Anton and complementing as subtracting

$$200 - 40 = 160$$

$$40 + 60 + 100 = \cancel{160} \quad 200$$

- in fehlt die Grundvorstellung „wie viel mal größer“  $\hat{=}$  dividieren  
 - ~~er~~ er benutzt dann seine Grundvorstellung „wie viel größer“  $\hat{=}$  Addieren

Verarbeitet sein Modell in das richtige Ergebnis



(modelling cycle: Pollack 1979, situation model: Reusser 1898, model: Fischbein 1989)

## A3. Exploring diagnostic judgments and their change

Sample of the study: n = 160 prospective math teachers (year 1 and 3)

Design:

Pre-Investigation

Video Clip 1: Anton and complementing as subtracting

160 written diagnostic judgments for Anton's process

Intervention: 20 min lecture

Math-didactical categories for ... unpacking student thinking

- modelling cycle
- mental model for division, subtraction, ...

... decentering the judgments

- individual situation model
- meanings

Post-Investigation

Video Clip 1: Anton and complementing as subtracting

160 written diagnostic judgments for Anton's process

## A3. Exploring diagnostic judgments and their change – selected findings

### Pre-Investigation

Video Clip 1: Anton  
and complementing  
as subtracting

160 written diagnostic judgments  
for Anton's process

### Intervention: 20 min lecture

Math-didactical categories for  
... unpacking student thinking

- modelling cycle
- mental models for  
division, subtraction, ...
- ... decentering the judgments
- individual situation model
- meanings

### Post-Investigation

Video Clip 1: Anton  
and complementing  
as subtracting

160 written diagnostic judgments  
for Anton's process

Unpacking: Focus on mental aspects,  
not only superficial aspects: 64 %

Activating categories, e.g.  
identify Anton's mathematizing: 46 %



80 %



61 %

first findings of ongoing data analysis:

- teacher's diagnostic judgments can deepen when they activate didactical categories
- the activation can be promoted by a (minimal!) input of categories

## A4. Drawing consequences for the role of video

- videos have a high potential to promote teachers' reflection about student thinking (Sherin et al. 2009, and others)
  - but videos are not self-containing, due to need to focus attention on crucial aspects
  - for this purpose, math-didactical categories are necessary (Prediger 2010 JMTE)
- combine videos with substantial input in PD

### Math-didactical categories for

#### ... unpacking student thinking

- modelling cycle
- mental models for division, subtraction, ...

#### ... decentering the judgments

- individual situation model
- meanings

## A5. Adapting for video-assisted PD modules at scale

Formerly: spontaneous joint analysis of self-made videos

- advantage: mobilizes highest individual involvement
- risk: not all PD facilitators see crucial aspects ad hoc
- limit: spontaneous discussion cannot cover all topics systematically

### Consequences

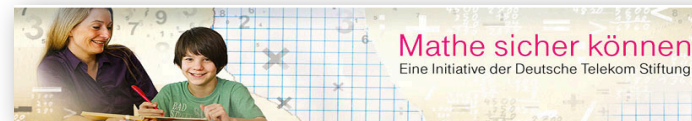
- more prepared video material with comments on meta-level
- systematic coverage of didactical categories for all crucial mathematical topics  
(← build coherent content-based programs, cf. Marongelle et al. 2013)

### Examples from Dortmund projects

- preservice



- inservice



# A5. Ac

www.kira.tu-dortmund.de

## KIRA - Kinder Rechnen Anderen

Beispiele | Material | Aktivitäten

Eingelogggt: tudortmund  
[ausloggen](#)

» Home » Material » Arithmetik bis zum 2. Schuljahr » Aufteilen und Verteilen

### Example: partitive and quotitive models for division

#### Grundvorstellungen der Division – Aufteilen und Verteilen

*Divisionsaufgaben können mit zwei verschiedenen Grundvorstellungen bearbeitet werden. Je nach Aufgabenformat liegt es nahe aufteilend oder verteilend eine Lösung zu ermitteln, aber auch Zahlenwerte können einen Einfluss auf die Wahl der Grundvorstellung haben. Hier bekommen Sie die Gelegenheit, den Unterschied zwischen aufteilendem und verteilendem Rechnen selbst zu erkunden, Vorgehensweisen von Kindern zu beobachten und zu hinterfragen.*

1. Ein Missverständnis zwischen den Grundvorstellungen
2. Hintergrundwissen zu den Grundvorstellungen der Division
3. Eigene Erkundung der Grundvorstellungen
4. Kinder lösen Aufteil- und Verteilungsaufgaben
5. Wenn der Kontext und die Zahlenwerte miteinander konkurrieren
6. Weitere Forschungsbefunde zum aufteilenden und verteilenden Rechnen
7. Verwandte Themen
8. Zitierte Literatur
9. Weiterführende Literatur

1. Ein Missverständnis zwischen den Grundvorstellungen

 Lina wurde zu Beginn des 3. Schuljahrs die kontextfrei dargebotene Aufgabe  $60:4$  gestellt. Ihr Lösungsansatz bestand zunächst darin, die Zahl zu suchen, deren Vierfaches 60 ergibt: Sie begann mit 20, probierte es dann mit 18 und 21 und versuchte es anschließend mit 16. An dieser Stelle setzt der folgende Gesprächsausschnitt ein. [...]

L: Ähm, 16 mal ... äh, 16 mal 4 ist ... 4 Zehner sind erst mal wieder 40, dann 46 und plus 4 ... 50 ... 52 plus 6 sind 58 ... passt auch nicht.  
I: Wieso hast du gerade plus 6 gesagt?  
L: Was, wo?  
I: Du hast gerade plus 6 gesagt. 52 plus 6 sind 58.  
L: Ja.  
I: Wieso 6?  
L: Weil ich da noch einmal ... ich hatte ja 16 mal 4 gerechnet. Da muss ich noch eine 6 dazurechnen. Weil ich erst die ganzen vier Zehner gemacht habe und dann die Sechser.

Aim: enhancing diagnostic expertise in preservice teacher education covering all relevant arithmetic topics  
Implementation: Platform and DVD used by more than 50 universities in D, CH, A

(KIRA, Selter, Götze et al. 2007-2011)

# A5. Adapting for video-assisted PD modules at scale

Topic specific categories  
typical mistakes

Possible backgrounds      Hints for helping activities

Mathe sicher können  
Eine Initiative der Deutsche Telekom Stiftung

Handreichungen für ein Diagnose- und Förderkonzept zur Sicherung mathematischer Basiskompetenzen

Brüche, Prozente, Dezimalzahlen

Cornelsen

UNTERRICHTSENTWICKLUNG AUF SCHULEBENE

Basiskompetenzen > Fortbildungsmaterial

**FORTBILDUNGSMATERIAL**

**Fortbildungskonzeption**

Neben den Schüler- und Lehrermaterialien werden im Projekt 'Mathe sicher können' Fortbildungsmaterialien entwickelt und erprobt, welche über die Sicherung von Basiskompetenzen informieren. Ziel ist es dabei einerseits, das Anliegen des Projekts auf Vorträgen und Tagungen einer breiten Öffentlichkeit bekannt zu machen. Andererseits werden ebenso Materialien für Multiplikatorinnen/Multiplikatoren und Fortbildnerinnen/Fortbildner entwickelt, um eine breite Implementation der entstehenden Ideen zu ermöglichen.

**Überblick über die Fortbildungskonzeption und die entstehenden Materialien**

Das Fortbildungskonzept umfasst drei Nachmittage mit jeweils drei Stunden. Die drei zugehörigen Fortbildungsmodule haben folgende Schwerpunktsetzungen:

Fortbildungsmodul 1: Überblick  
 Fortbildungsmodul 2: Diagnose  
 Fortbildungsmodul 3: Förderung

Written material plus selected videos

Aim: PD at scale for inservice teachers for fostering low achieving students

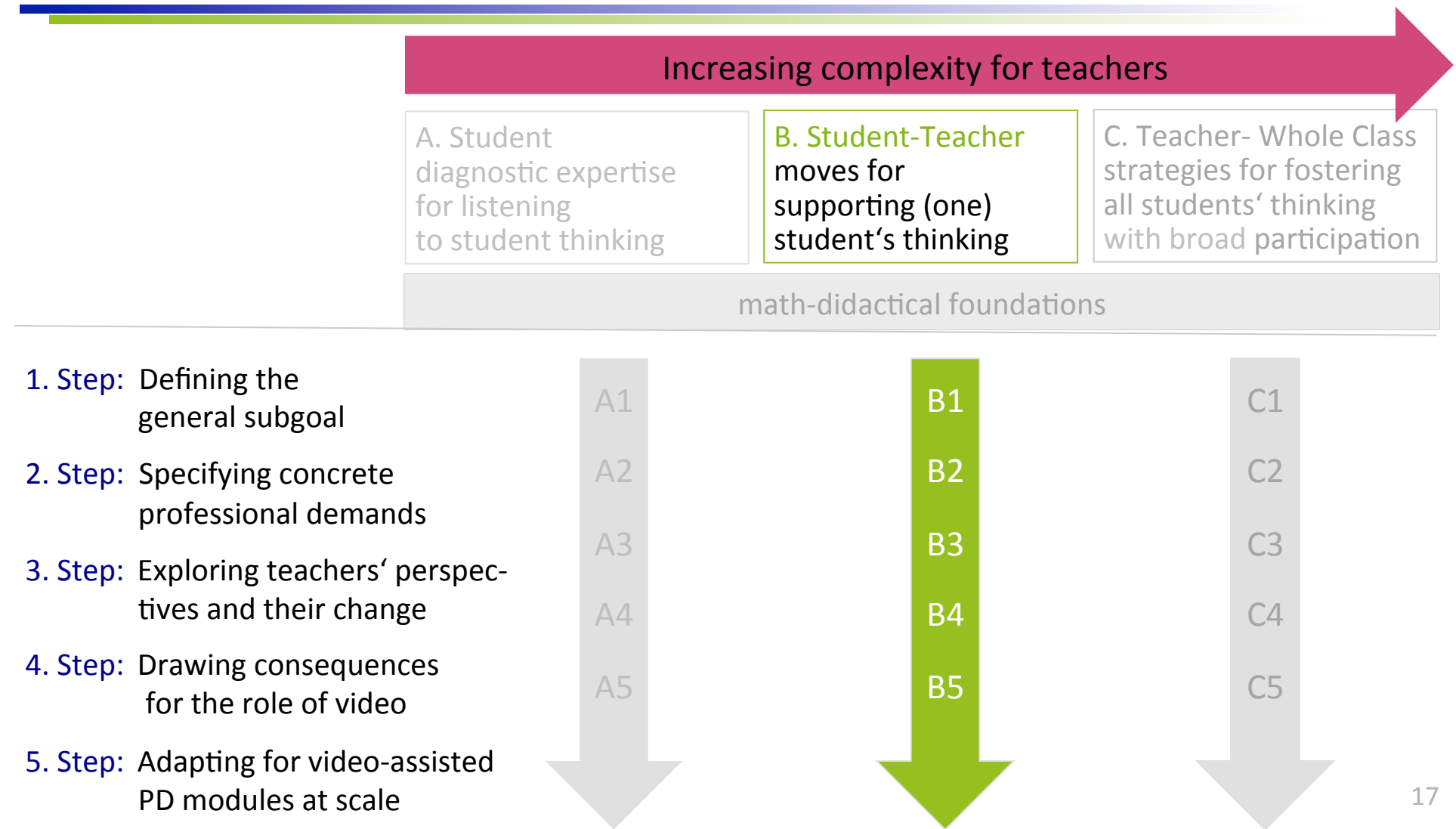
Implementation (starts Feb 2014) in 4 states, 65 schools with 20 multipliers

later further federal states

(Prediger, Selter et al. 2010-2017)



# Structure of the talk



## B1. Defining the subgoal “moves for supporting one student’s thinking”

- empirical result of classroom studies: (Cobb & Bauersfeld 1995, Clarke et al. LPS ) teacher-student interaction follows typical pattern with varying impact on students’ cognitive involvement
- teachers shall become aware and learn to apply moves that support student’s thinking, e.g.
  - initial posing
  - eliciting student thinking
  - rephrase, revoice, ...
  - leading
  - rejecting

B. Student-Teacher moves for supporting (one) student’s thinking

B1

B2

B3

B4

B5

(Sleep & Boerst 2013)

## B4. Using video for becoming aware of supportive moves

Method “headstand”:

- first, consider a problematic video
- then, derive DOs and DON'Ts for supportive moves

(Clarke & Hollingsworth 2000)



Experience:

- implicit knowhow of teachers can be made explicit
- works with every teacher group and every facilitator

but only for evident moves, **not for more subtle situations**

*Goal: support the individual process of thinking without disturbing it*

*DOs:*

- *give enough time to reflect*
- *pose open questions*
- *elicit longer utterances*
- *...*

*DON'Ts:*

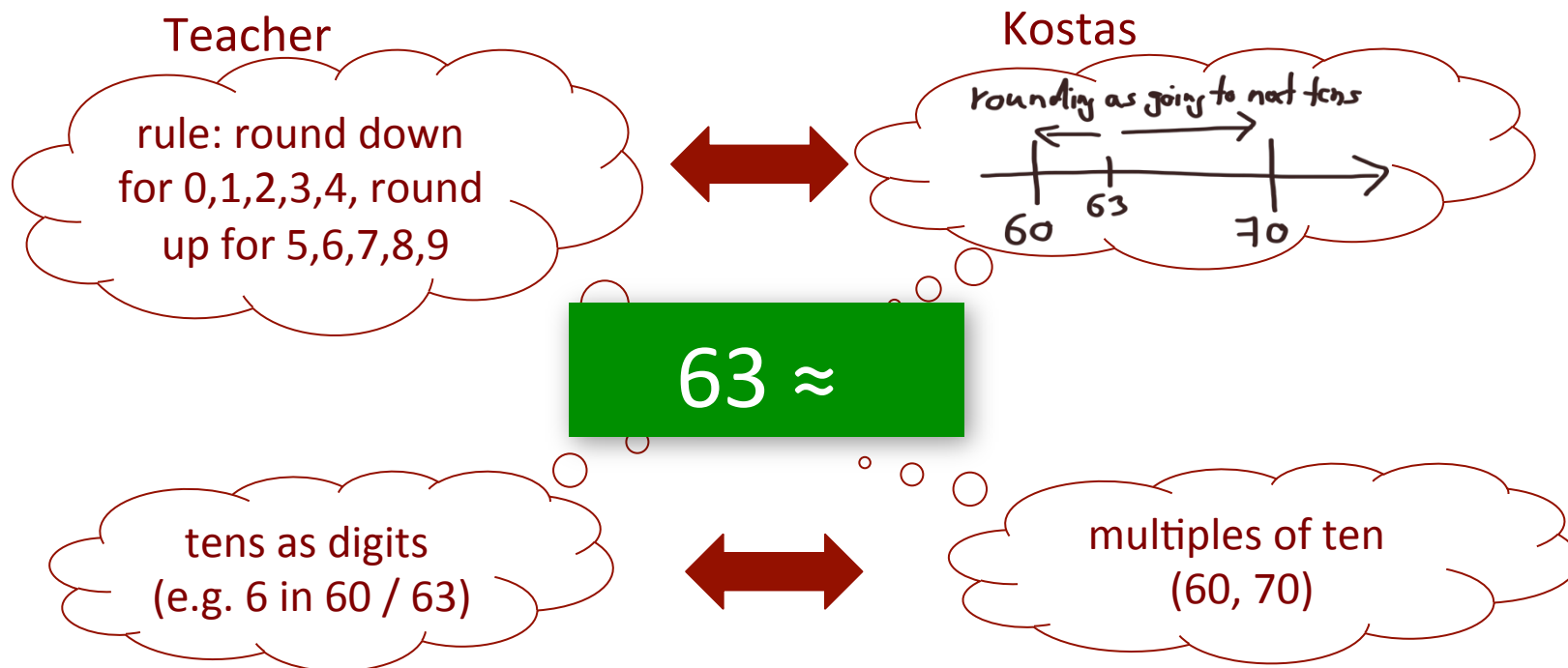
- *impose teacher's train of thought*
- *help without understanding*
- *evaluate every utterance*
- *...*

Example for a list collected in a teacher group

## B2. Supportive moves – Specifying professional demands

- Same procedure: job analysis (Bass & Ball 2004)
- Video Clip 2:  
classroom interaction with one student, Grade 5
- Content: how to explain the procedure of rounding, e.g.  $63 \approx 60$ ?

Video Clip 2:  
Mr. Maler, Kosta  
and rounding 63



# B2. Supportive moves – Specifying professional demands

Video Clip 2:  
Mr. Maler, Kosta  
and rounding 63

Teacher KOSTAS.

SIXTY.

Kostas

Teacher SIXTY. [to the class] Can we WRITE this down?

← rhetorical questions

[Shouts out different answers]

Class

Teacher NO?

[Shouts out different answers]

Class

Teacher Hm, LOOK. I'm WRITING it down, Kostas, and now YOU convince us, why the sixty can stand there and why this is CORRECT.

← eliciting longer answers

°hhh. Well, if you are rounding DOWN the sixty-three on TENS; then it comes, it gets, there must be ALWAYS a zero at the end, it MUST be, when you are rounding.

Kostas

Teacher On TENS yes.

← eliciting longer answers

And then there, if you take AWAY the three and shift the ZERO to it. So, you could DO that, but actually it's WRONG. You just have to round down and nea.. nearest number with a ZERO you have to write there.

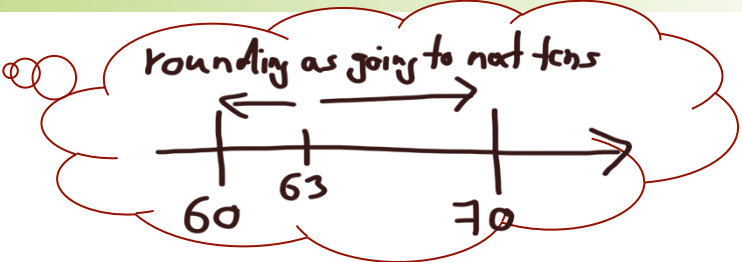
Kostas

Our way of presenting → transcripts to teachers

# B2. Supportive moves – Specifying professional demands

Video Clip 2:  
Mr. Maler, Kosta  
and rounding 63

unexpectedly,  
answer goes back to meaning



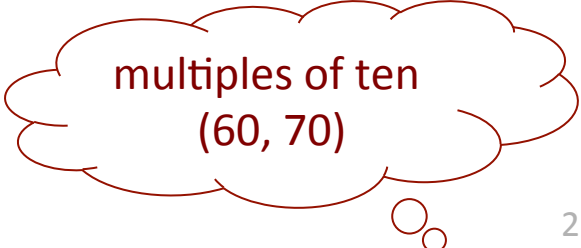
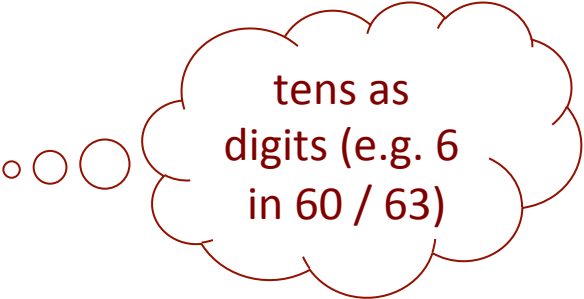
Yes, it is a SIXTY, isn't it?

Student

Teacher

KAY, I think I already UNDERSTOOD SOME parts,  
of what you wanted to explain;  
so FIRST of all I filtered OUT, you rounded on TENS;  
what does that mean HERE, if you are rounding on TENS,  
what ARE the TENS here actually?  
  
Can you show that simply once in the front, Kostas?  
I am not completely sure, if you DID round on tens;

← subtle rejection of answer



## B2. Supportive moves – Specifying professional demands

Video Clip 2:  
Mr. Maler, Kosta  
and rounding 63

Teacher

But now there is an ABOUT there and you already implied WHY; but does any of you know a RULE, HOW one has to proceed here, and when one here, when the ten stays the SAME? In this case, and the place BEHIND, which is rounded, goes to ZERO? Ha; [4.5 sec. break] Katja.

← making expectations more explicit

With zero one two three FOUR you are rounding down and with five six seven eight NINE you are rounding (up).

Katja

← answer refers to procedural rule

Teacher

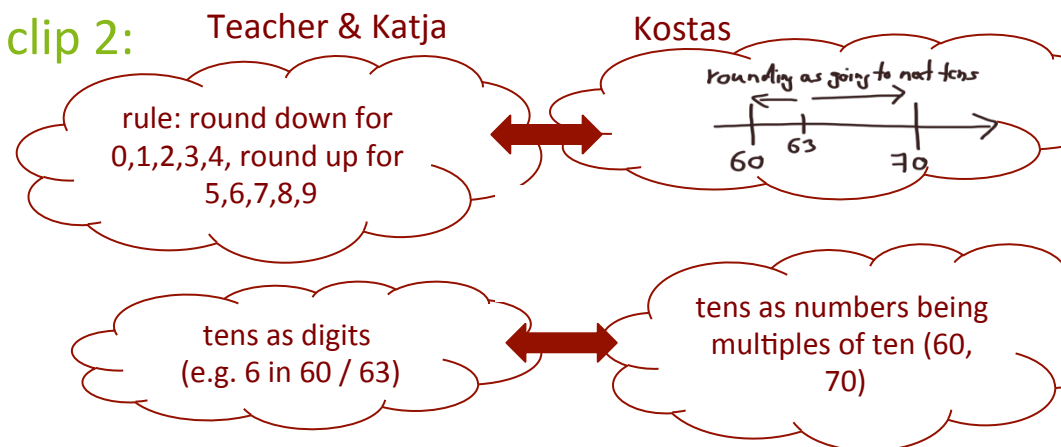
Has EVERYBODY understood that?

← implicit but very positive evaluation

## B2. Supportive moves – Specifying professional demands

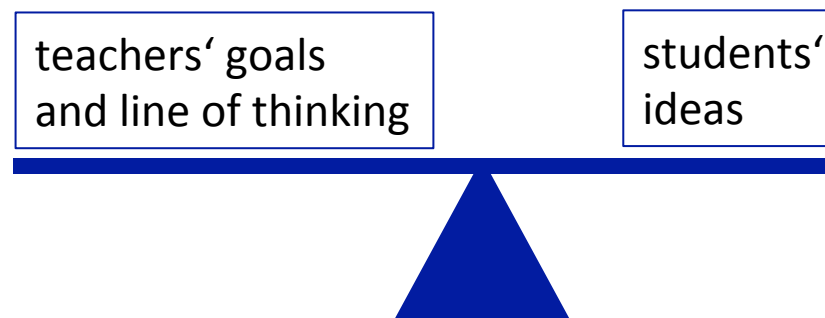
### Math-didactical foundation of video clip 2:

- what is a suitable explanation in explanations?
- rules versus representations?
- core arithmetic concepts: numbers versus digits?



### Supportive moves should:

- engage students into longer explanations
- mark (in-)correctness without ashaming
- do justice to valuable mathematical ideas of students
  - ← diagnostic competence
- manage a difficult balance:
- ...





## B3. Exploring professional perspectives and their development in group discussions

---



### Aim of the qualitative study:

- explore professional perspectives on interactions and supportive moves
- and how these perspectives develop within a discussion

### Methods:

- data gathering: video-stimulated group discussions with 6 groups of 4-6 practicing teachers (90 min each)
- qualitative data analysis: categories for teachers' patterns of perception, interpretation and evaluation of interactions and supportive moves

Video Clip 2:  
Mr. Maler, Kosta  
and rounding 63

## B3. Exploring professional perspectives and their development in group discussions



what does the teacher want?

how do students' answers fit to expectations?

°hhh. Well, DOWN the sixty-three on TENS; then there must be ALWAYS a zero at the end, it MUST be, when you are rounding. And then there, if you take AWAY the three and shift the ZERO to it. So, you could DO that, but actually it's WRONG. You must have to round down and nearest number with ZERO you have to write there.

Kostas does not speak straightly

Video Clip 2:  
Mr. Maler, Kosta  
and rounding 63

Kostas' earlier explanation

Teacher

But now there is an ABOUT there and you already implied WHY; but does any of you know a RULE, HOW one has to proceed here, and when one here, when the ten stays the SAME? In this case, and the place BEHIND, which is rounded, goes to ZERO? Ha; [4.5 sec. break] Katja.

With zero one two three FOUR you are rounding down and with five six seven eight NINE you are rounding (up).

Katja

Teacher

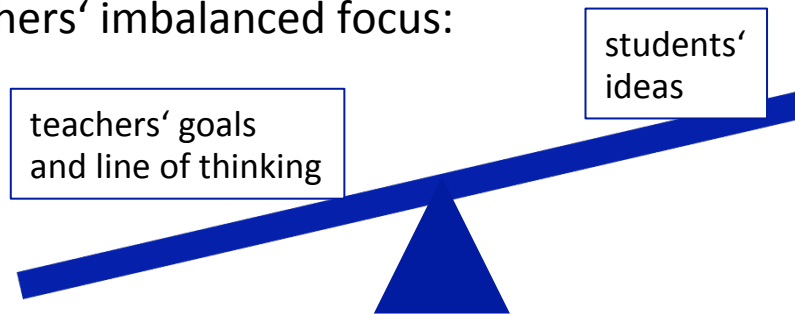
Has EVERYBODY understood that?

## B3. Exploring professional perspectives and their development in group discussions



Selected results (of the ongoing analysis, cf. Vogler 2014)

teachers' imbalanced focus:



Video Clip 2:  
Mr. Maler, Kosta  
and rounding 63

- formal aspects (behaviour, language etc.) seem to be more important than content
- few focus on math-didactical foundation
- but also resources for becoming aware of deeper phenomena

potential for change of focus

- discussion slowly shifts the focus towards students
- but only if moderated into this direction

## B4. Drawing consequences for the role of video in PD

**Chances of video-use:** (often shown, e.g. Clarke & Holingsworth 2000, Sherin 2004)

- raising awareness on relevance and effects of interactional moves
- evident interactional moments can be exploited by teachers in PD on their own (example headstand)

**Challenges for video-use:**

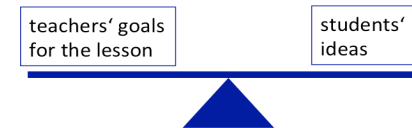
- teachers' selected focus
- no exploitation of potentials without discussion  
→ careful moderation by the PD facilitators is needed to
- shift into a balance of focus
- offer categories for reflection
- make explicit the subtle, implicit mechanisms of IRE-sequences

(Mehan 1979, Voigt 1995)



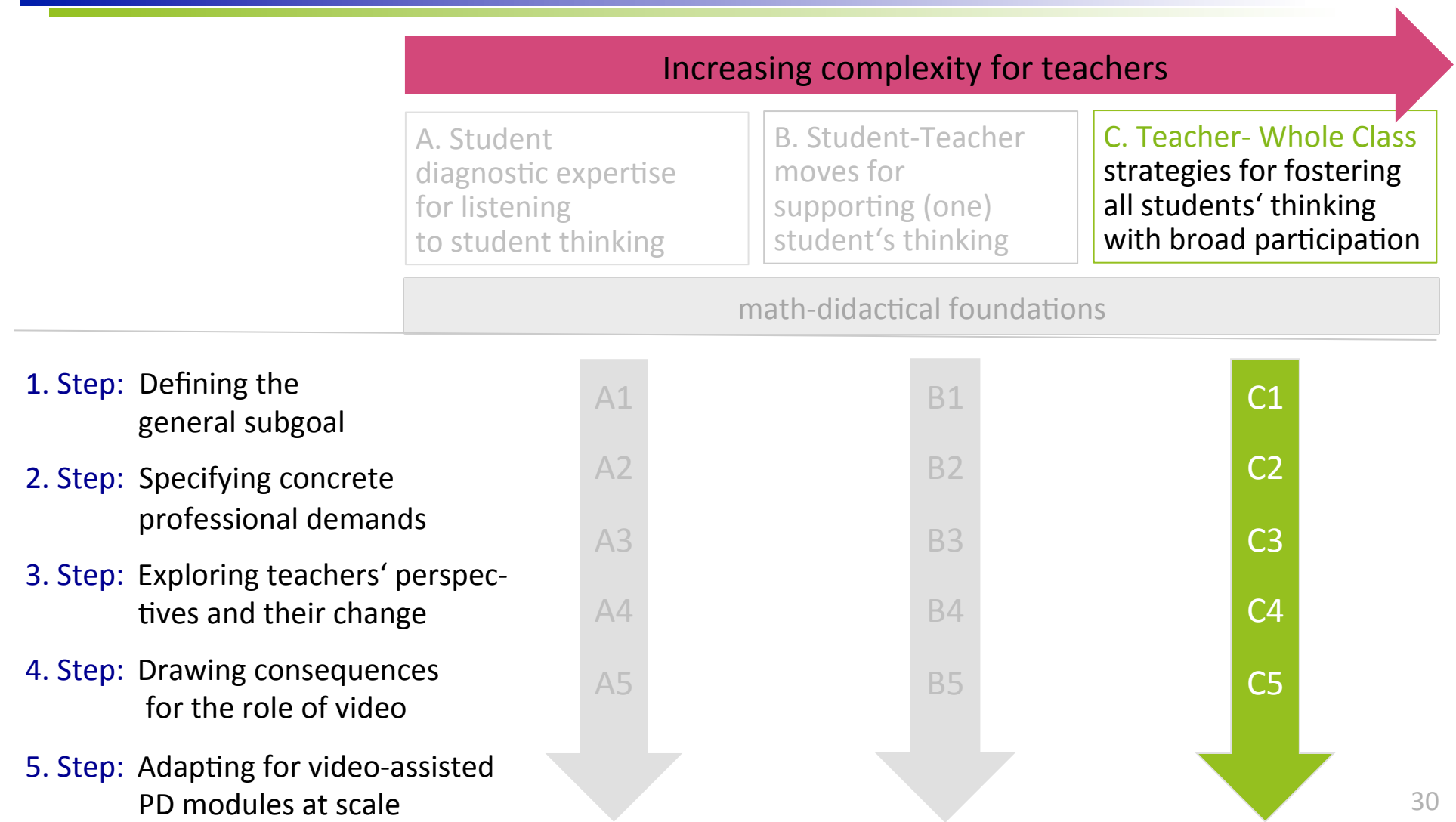
## B5. Adapting for video-assisted PD modules at scale

- videos of evident interactions can easily be used in PD since teachers can make sense of them alone
- for more subtle phenomena,
  - a facilitation pathway must be developed for capturing the subtle background
  - facilitators must be sensitized not for simple rules (“you must always value students’ ideas”)
  - but for difficulties of balancing different aims
- teachers’ typical perspectives must be taken into account already in planning of video materials and their embedding
- for this, systematic comparison of subgoals with teachers’ perspectives have to be conducted (← educational reconstruction, Duit, Gropengießer & Kattmann 2005, Komorek et al. 2013)



more research needed

# Structure of the talk



## C1. Defining the general subgoal „fostering broad participation“

B. Student-Teacher moves for supporting (one) student's thinking

C. Teacher- Whole Class strategies for fostering all students' thinking with broad participation

- supporting one student's thinking needs supportive moves
- involving the whole class into the discourse needs an overall choreography
- typical challenges:
  - how to deal with multiple student solutions?
  - how to built upon individual ideas for constructing meanings?
  - how to deal with only partially correct ideas?

C1

C2

C3

C4

C5

## C2. Specifying concrete professional demands

(Grade 5, video clip 3 from project Interpass, Prediger & Erath 2014)

Video Clip 3:  
Mr. Schroedinger  
and the average

Calculate the average pocket money  
15 € / 15 € / 20 € / 40 € / 15 € /  
30 € / 15 € / 30 € / 0 € / 20 €

What does each step mean  
in the procedure  
for calculating the average?

Meaning of the average ← Teacher's headline

200 : 10  
= 20

↑  
Kain's solution

6  
+ 15  
+ 20  
+ 40  
+ 25  
+ 30  
+ 15  
+ 30  
+ 0  
+ 20  

---

200

← Konstantin's solution

Video starts when students  
had written their answers  
and teacher builds upon it



## C2. Specifying concrete professional demands

Calculate the average pocket money

15 € / 15 € / 20 € / 40 € / 15 € /  
30 € / 15 € / 30 € / 0 € / 20 €

Video Clip 3:  
Mr. Schroedinger  
and the average



(Grade 5, video clip from project Interpass, Prediger & Erath 2014)

## C2. Specifying concrete professional demands

Video Clip 3:  
Mr. Schroedinger  
and the average

Teacher

What is more HANDY in the way Konstantin wrote it [*points at writings on the blackboard*] than in Kain's way? I KNOW, there is missing a small step here, but what is more handy in THIS version here [*points at Konstantin's calculation*] than in THIS one. [11.5 sec. break]  
Evan, you're looking COMPLETELY puzzled now; like you wanted to SAY, it's different but ANYWAY no idea;

← comparing  
two solutions

no IDEA;

Evan

Teacher

hm\_hm; it's not yet CLEAR what they are doing and WHY;  
[*points at the two calculations*]

no IDEA;

Evan

Teacher

OKAY, [2.5 sec. break] Nahema;

← allowing not to know

With Kain's way, you have to calculate it all in your HEAD, and Konstantin has a more HANDY because he calculated all one BELOW the other, that was EASIER.

Nahema

Summed up in a written way.

Eric

## C2. Specifying concrete professional demands

Video Clip 3:  
Mr. Schroedinger  
and the average

Teacher

EXACTLY. As a START, you can say what these two hundred here, what else these two HUNDRED indicate. [*points at the result of the calculation*]  
Then it's possibly going to be clearer soon for Evan, WHAT one has to do. WHAT else do these two hundred indicate? [*4.5 sec break*] Lilja. [*4.7 sec break*] What does one KNOW, what do these two HUNDRED indicate?

← new task:  
meaning of average

How much MONEY this is all calculated together.

Lilja

Teacher

[*writes on the blackboard:*]

Meaning of the average

$$\begin{array}{r} 200 : 10 \\ = 20 \end{array}$$
$$\begin{array}{r} 6 \\ + 15 \\ + 20 \\ + 40 \\ + 25 \\ + 30 \\ + 15 \\ + 30 \\ + 0 \\ + 20 \\ \hline 200 \end{array}$$

That is how much all kids have together

← treating the  
incomplete solution  
as a first step  
in the procedure

You see, THIS is very important at the first step that you have THIS value.

## C2. Specifying concrete professional demands

Video Clip 3:  
Mr. Schroedinger  
and the average

Teacher: Well, I just asked Lilja what these two HUNDRED mean; she described it COMPLETELY correct. Now, what do these TWENTY Euro tell us that come out here and that also got out here at Kain's? Two hundred Euro, all kids have together who told their pocket money. Now, what do these TWENTY Euro tell us?

It's *the* [expressed in wrong grammatical gender: *das Durchschnitt*] AVERAGE of the money.

Dilai

Teacher correcting → without ashaming: Hm, the [expressed in correct grammatical gender: *der Durchschnitt*] AVERAGE of the money. Eric.

It's the average of the POCKET money that all have APPROXIMATELY.

Eric

Teacher [writes on the blackboard:]

Meaning of the average

①  $200 : 10 = 20$

②  $200 : 10 = 20€$

The average-money that all have approximately

That is how much all kids have together

$$\begin{array}{r}
 + 6 \\
 + 20 \\
 + 20 \\
 + 20 \\
 + 20 \\
 + 20 \\
 + 20 \\
 + 20 \\
 + 20 \\
 + 20 \\
 + 20 \\
 \hline
 200
 \end{array}$$

Larissa, is this calculation UNDERSTANDABLE so far?

[pretending enthusiasm] YES.

Larissa

Teacher: FIRST think about WHAT everybody has together [points at Konstantin's written addition] and THEN afterwards coming up with such a sharing? [points at Kain's division]

## C2. Specifying concrete professional demands

Video Clip 3:  
Mr. Schroedinger  
and the average

- math-didactical foundation: (Erath & Prediger 2014)
  - not only calculation, but also meanings for the average
  - distinguish meaning and rule for procedure as different epistemic modes
  - meanings for each step in the calculation procedure for the average
- interaction:
  - many students involved
  - interaction builds with many answers
- teacher's evaluation of students' partial answers:
  - evaluated as intermediate step, not as wrong
  - combined for complete calculation procedure

Meaning of the average

①  $200 : 10 = 20$

②  $200 : 10 = 20 \text{ €}$

The average money that all have approximately

That is how much all kids have together

“orchestrated explaining” as a joint practice with broad participation (Morek 2012)

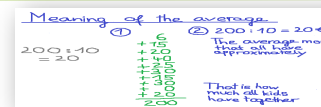
### C3. Exploring teachers' perspectives and their change

Video Clip 3:  
Mr. Schroedinger  
and the average

Prospective teachers'  
discussion and  
written reflections

math-didactical foundations:

(Erath & Prediger 2014)



- not only calculation, but also meanings for the average
- distinguish meaning and rule for procedure as different epistemic modes
- meanings for each step in the calculation procedure for the average

interaction:

- many students involved
- interaction builds with many answers

teacher's evaluation of students' partial answers:

- evaluated as intermediate step, not as wrong
- combined for complete calculation procedure

- die Wissensfacetten "Anleitung" und "Bedeutung" werden miteinander verknüpft  
→ Schüler verstehen was und warum sie rechnen ✓

didactical categories can be applied

Schüler fühlt sich nicht zurückgewiesen, traut sich auch weiterhin aktiv im Unterricht mitzuarbeiten

subtle evaluations not identified  
→ need to be analysed together

“orchestrated explaining“ as a joint practice with broad participation (Morek 2012)

## C4. Drawing consequences for the role of video

- ‘good practice’ videos can be used in PD, but necessitate systematic reflections, especially for more subtle aspects

## C5. Adapting for video-assisted PD modules at scale

different strategies in different projects:

- best practice classrooms with comments in project PikAS; e.g. for new classroom methods etc. (Selter et al. 2009-2016)
- for more subtle aspects: authentic, non-polished videos for my KOSIMA and MuM-projects (Prediger in progress)
- background and reflections are most crucial, no video without discussions



# Looking back: Double research-base for design

Research on student thinking and classroom interaction

**A. Student**  
diagnostic expertise  
for listening  
to student thinking

**B. Student-Teacher**  
moves for  
supporting (one)  
student's thinking

**C. Teacher- Whole Class**  
strategies for fostering  
all students' thinking  
with broad participation

$\alpha$  and  $\Omega$ : math-didactical foundations (PCK & MFT)

1. Step: Defining the general subgoal
2. Step: Specifying concrete professional demands
3. Step: Exploring teachers' perspectives and their change
4. Step: Drawing consequences for the role of video
5. Step: Adapting for video-assisted PD modules at scale

A1

Video Clip 1:  
Anton and comple-  
menting as subtracting

Prospective teachers'  
written analysis with  
and without categories

A5

B1

Video Clip 2:  
Mr. Maler, Kostas  
and rounding 63

Practicing teachers'  
group discussion for  
increasing awareness

B5



C1

Video Clip 3:  
Mr. Schroedinger  
and the average

Prospective teachers'  
discussion and  
written reflections

C5



# Looking back: Relevance of math-didactical foundations

too important to be addressed only accidentally, needs systematic coverage

and  $\Omega$ : math-didactical foundations (PCK & MFT)

(Kirsch 1976, van den Heuvel-Panhuizen & Treffers 2009, Shulman 1989, Bass & Ball 2004)

Video Clip 1:  
Anton and complementing as subtracting

- cognitive activities in the modelling cycle
- different mental models (meanings) for subtraction: complementing versus taking away (Selter, Prediger, et al. in ESM2012)
- diverging meanings for the equal sign (Kieran 1981, Prediger JMTE2010)

Video Clip 2:  
Mr. Maler, Kostas and rounding 63

- meanings for rounding  $63 \approx 60$
- representations on the number line
- distinguishing arithmetic core concepts (numbers vs. digits)
- explaining by meanings vs. by rote procedures (Prediger & Erath 2014)

Video Clip 3:  
Mr. Schroedinger and the average

- meanings for the average
- meanings of steps in the calculation procedure for average
- epistemic modes for “explaining” (Prediger & Erath 2014)

## Looking back: possible role of videos for three subgoals

### A. Student

diagnostic expertise  
for listening  
to student thinking

- student videos as object of study

### B. Student-Teacher

moves for  
supporting (one)  
student's thinking

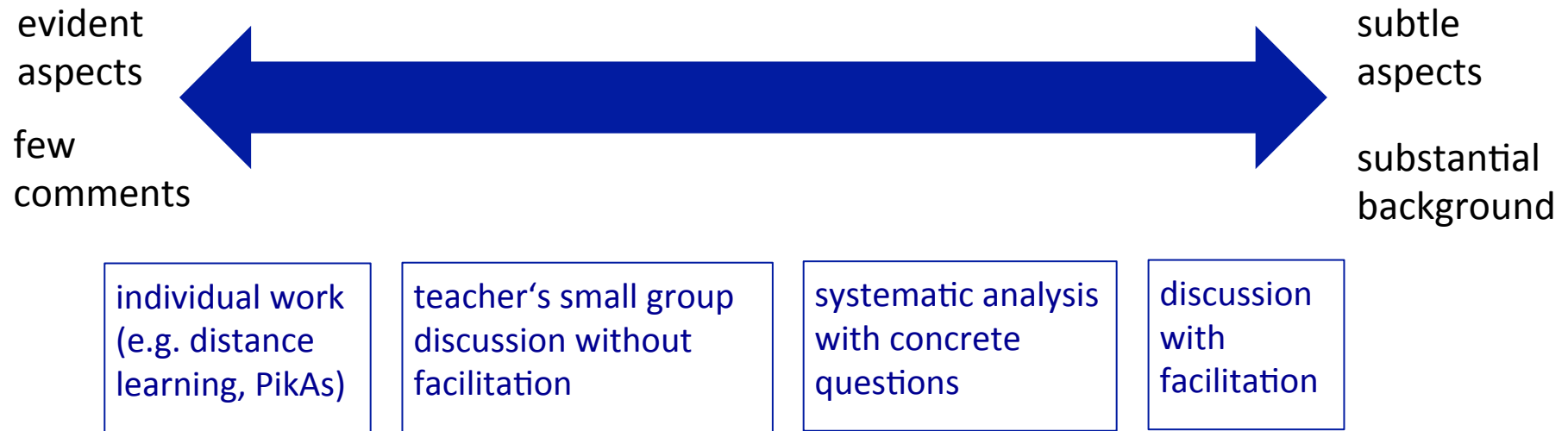
- bad practice for “headstand”:  
making explicit unconsciously known aspects
- complex, subtle practice as starting point for reflection
- own videos as most involving starting point for reflection

### C. Teacher- Whole Class

strategies for fostering  
all students' thinking  
with broad participation

- good and polished practice as model
- good but non-polished practice  
as starting point for reflection

# Looking back: pedagogical settings for the use of videos



*Looking forward to  
four days of further discussion!  
Thank you for your attention!*

Challenges for video-assisted modules in PD at scale

- written materials with substantial activities and background
- self explaining video-assisted moduls
- education of the teacher educators!