

On sources of ultra-high energy cosmic rays

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Outline:

1. General constraints: 'the sources at the sources'
2. Spectrum, deflection, apparent density: 'the sources on the detectors'
3. Anisotropies (vs chemical composition)



→ ***chemical composition, or rigidity $E/(eZ)$ at a given energy, controls all the phenomenology at ultra-high energies:***

(1) sources of 10^{20} V are much more extreme than sources of 10^{18} V particles:

... e.g., a few candidate sources for 10^{20} eV protons vs *dozens* of candidate sources of 10^{20} eV iron...

(2) light particles leave stronger signatures of their sources:

... e.g., anisotropies at ultra-high energies with deflections of a few deg, vs large deflections for iron-like primaries

... e.g., secondary photons and neutrino signals

GeV photon halo from a UHECR source



→ a possible signature of UHECR acceleration: a gamma-ray halo / secondary flux from a powerful source, from synchrotron radiation of secondary electrons

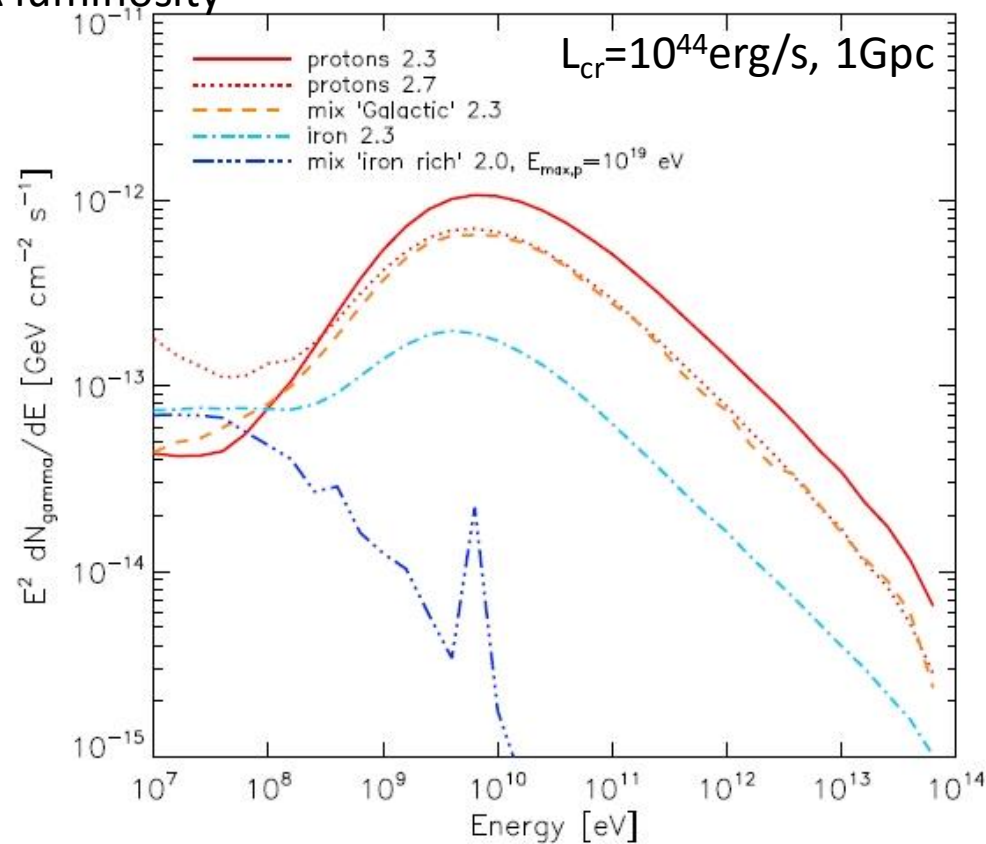
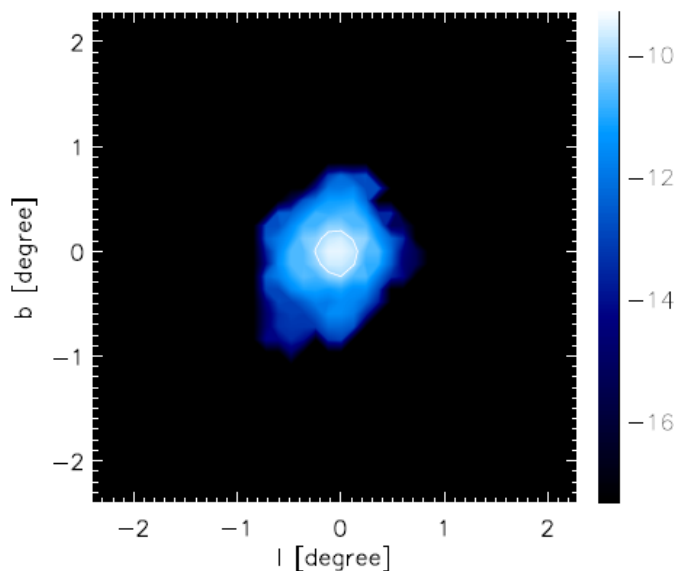
(Aharonian 02, Gabici & Aharonian 05, Kotera+ 11):

**$N + \gamma_{\text{CMB/IRB}} \rightarrow$ e.m. cascade down to GeV-TeV
electron synchrotron to GeV**

→ detection with CTA requires a large CR luminosity

of protons above 10^{19} eV:

$L_{\text{cr}} \sim 10^{46}$ erg/s for a distance 1Gpc...



see also Essey+ 10,11, Murase+ 12



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Acceleration – a luminosity bound



(e.g. Lovelace 76, Norman+ 95, Blandford 00, Waxman 05, Aharonian+ 02, Lyutikov & Ouyed 05, Farrar & Gruzinov 09, M.L. & Waxman 09)

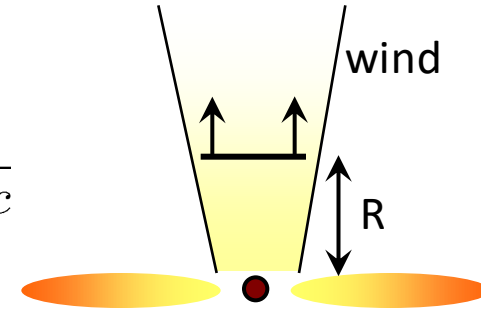
A generic case: acceleration in an outflow

→ acceleration timescale (comoving frame): $t_{\text{acc}} = \mathcal{A} t_g$

$\mathcal{A} \gg 1$, $\mathcal{A} \sim 1$ at most:

- for non-relativistic Fermi I, $\mathcal{A} \sim (t_{\text{scatt}}/t_g) / \beta_{\text{sh}}^2$

→ time available for acceleration (comoving frame): $t_{\text{dyn}} \approx \frac{R}{\beta \Gamma c}$



→ maximal energy: $t_{\text{acc}} \leq t_{\text{dyn}} \Rightarrow E_{\text{obs}} \leq \mathcal{A}^{-1} Z e B R / \beta$

→ ‘magnetic luminosity’ of the source: $L_B = 2\pi R^2 \Theta^2 \frac{B^2}{8\pi} \Gamma^2 \beta c$

→ lower bound on total luminosity: $L_{\text{tot}} \geq 0.65 \times 10^{45} \Theta^2 \Gamma^2 \mathcal{A}^2 \beta^3 Z^{-2} E_{20}^2 \text{ erg/s}$

10^{45} ergs/s is robust:

for $\beta \rightarrow 0$, $\mathcal{A}^2 \beta^3 \geq 1/\beta \geq 1$

for $\Theta \Gamma \rightarrow 0$, $L_{\text{tot}} \geq 1.2 \times 10^{45} \mathcal{A} \beta \frac{\kappa}{r_{\text{LC}}} Z^{-2} E_{20}^2 \text{ erg/s}$

Lower limit on luminosity of the source:

$$L_{\text{tot}} > 10^{45} Z^{-2} \text{ erg/s}$$

low luminosity AGN: $L_{\text{bol}} < 10^{45}$ ergs/s

Seyfert galaxies: $L_{\text{bol}} \sim 10^{43}$ - 10^{45} ergs/s

high luminosity AGN: $L_{\text{bol}} \sim 10^{46}$ - 10^{48} ergs/s

gamma-ray bursts: $L_{\text{bol}} \sim 10^{52}$ ergs/s

⇒ only most powerful AGN jets, GRBs
or young magnetars for UHE protons...
... many (many) others for heavy nuclei?



General principles of particle acceleration

Standard lore:

→ Lorentz force: $\frac{d\mathbf{p}}{dt} = q \left(\mathbf{E} + \frac{\mathbf{v}}{c} \times \mathbf{B} \right)$

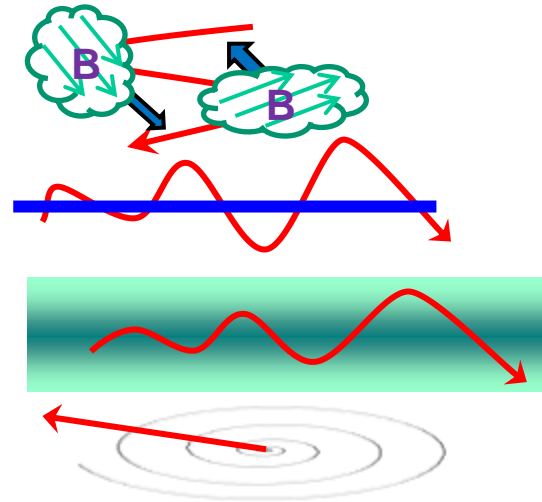
Ideal MHD: $\mathbf{E}_{|p} \simeq 0$ in plasma rest frame

→ \mathbf{E} field is 'motional', i.e. if plasma moves at velocity \mathbf{v}_p : $\mathbf{E} \simeq -\frac{\mathbf{v}_p}{c} \times \mathbf{B}$

→ need some force or scattering to push particles across \mathbf{B}

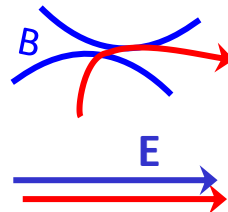
→ lower bound to acceleration timescale: $t_{acc} = \frac{p}{\beta_p e B} = \frac{t_g}{\beta_p}$

- examples:
- turbulent Fermi acceleration
 - Fermi acceleration at shock waves
 - acceleration in sheared velocity fields
 - magnetized rotators



Beyond MHD:

- examples:
- reconnection
 - gaps



Acceleration – a luminosity bound



A generic case: acceleration in an outflow

(e.g. Lovelace 76, Norman+ 95, Blandford 00, Waxman 05, Aharonian+ 02, Lyutikov & Ouyed 05, Farrar & Gruzinov 09, M.L. & Waxman 09)

→ acceleration timescale (comoving frame): $t_{\text{acc}} = \mathcal{A} t_g$

→ $\mathbf{A} \gg 1$ in most acceleration scenarios:

e.g. in Fermi-type, $\mathbf{A} \sim$ interaction time / energy gain

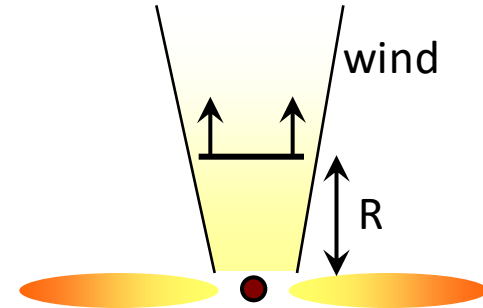
sub-relativistic Fermi I: $\mathcal{A} \sim (t_{\text{scatt}}/t_g)/\beta_{\text{sh}}^2$
and $t_{\text{scatt}} > t_g$ (saturation: Bohm regime!)

sub-relativistic stochastic: $\mathcal{A} \sim (t_{\text{scatt}}/t_g)/\beta_A^2$

sub-relativistic reconnection flow: $\mathcal{A} \sim 10/\beta_A$ (on reconnection scales)

relativistic Fermi I: $\mathcal{A} \sim t_{\text{scatt}}/t_g$ in shock frame, much more promising?

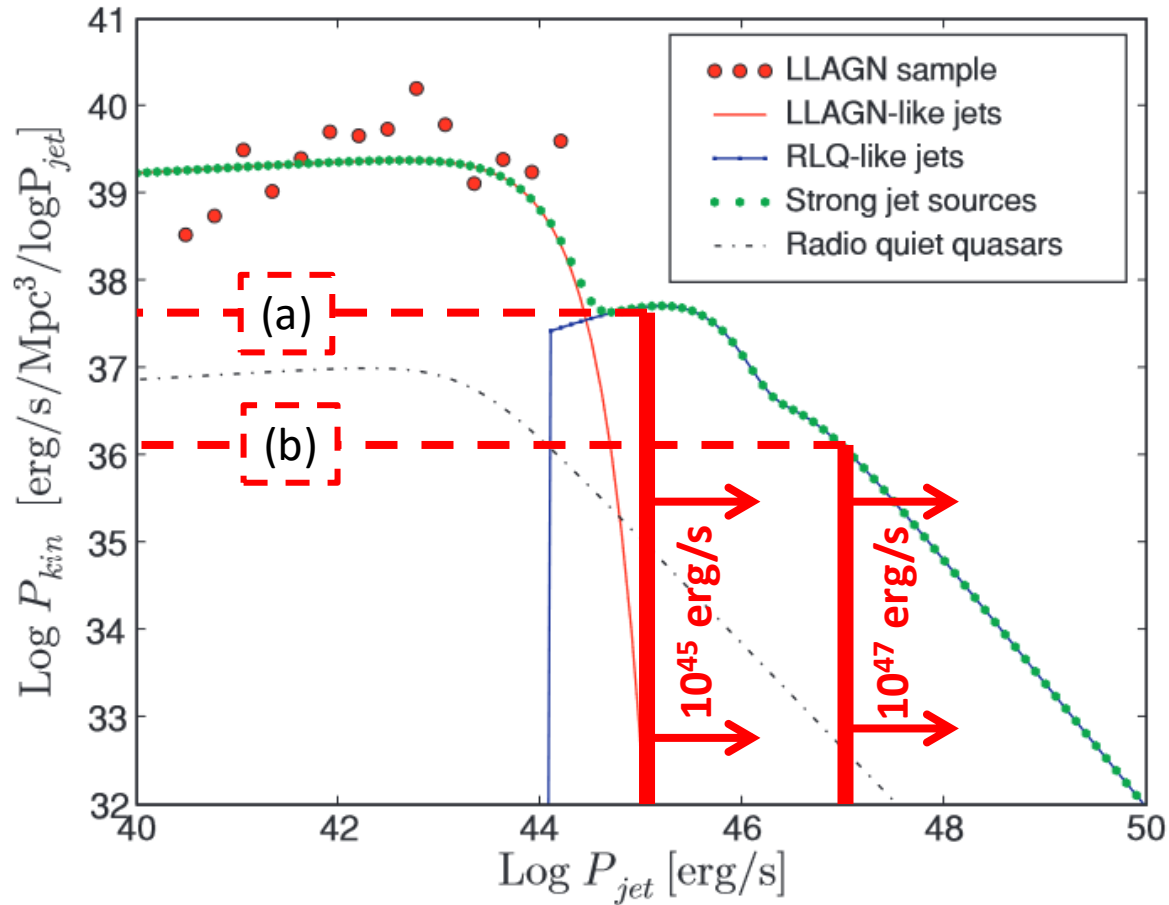
relativistic reconnection: $\mathcal{A} \sim 10$ (on reconnection scales)



... comparing t_{acc} and t_{dyn} bounds the luminosity of the source to reach UHE:

$$L_{\text{tot}} \geq 0.65 \times 10^{45} \Theta^2 \Gamma^2 \mathcal{A}^2 \beta^3 Z^{-2} E_{20}^2 \text{ erg/s}$$

Körding+07: energy input of radio-galaxies



(a): energy input of $10^{45} \text{ erg}/\text{Mpc}^3/\text{yr}$... density $0.5 \cdot 10^{-7} \text{ Mpc}^{-3}$

(b): energy input of $3 \cdot 10^{43} \text{ erg}/\text{Mpc}^3/\text{yr}$... density $10^{-11} \text{ Mpc}^{-3}$

... to match the flux above 10^{19} eV : input rate needed $10^{44} \text{ erg}/\text{Mpc}^3/\text{yr}$ (Katz+ 09)

Extreme acceleration, but also high output



Energy output of a source:

→ to match the flux above 10^{19} eV, $\dot{u}_{\text{UHECR}} \sim 10^{44}$ erg/Mpc³/yr (Katz+ 10)

→ per source, assuming it is steady: $L_{\text{UHECR}} \sim 10^{43} n_{-7}^{-1}$ erg/s (n in Mpc⁻³)

→ per transient source: $E_{\text{UHECR}} \approx 10^{50}$ erg \dot{n}_{-6}^{-1} (\dot{n} in Mpc⁻³yr⁻¹)

e.g.:

→ radio-galaxies with $L > 10^{45}$ erg/s, a few % efficiency

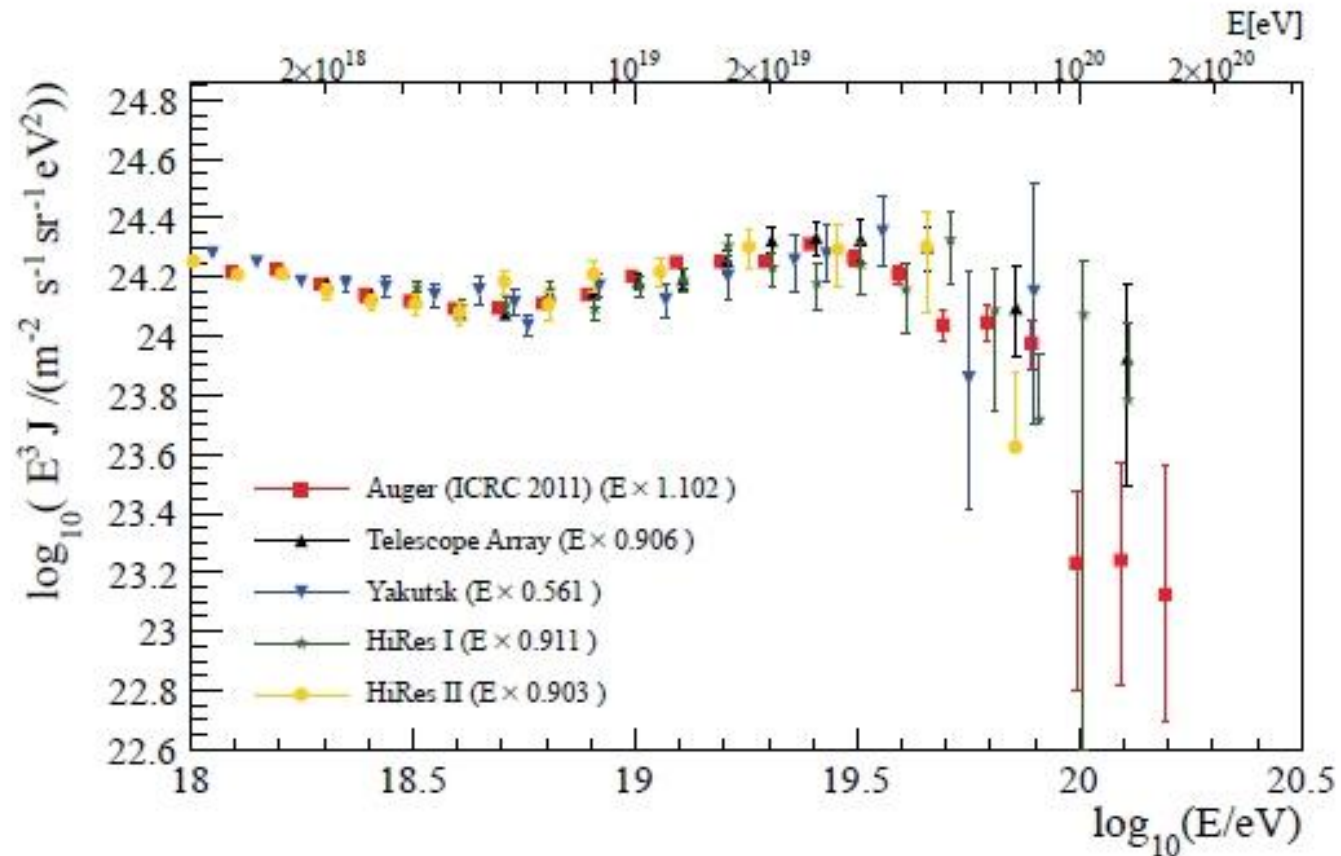
→ for the whole radio-galaxy population, $nL \sim 3 \cdot 10^{47}$ erg/Mpc³/yr, typically from sources with $L \sim 10^{43}$ erg/s...

... if injecting CNO to match flux at 10^{19} eV and if metallicity is \sim solar, requires an overall efficiency in high energy CR of a few percent!

if one wants nuclei at $>E$ to circumvent luminosity bound, accounting for the protons accelerated to $>E/Z$ requires an energy input higher by M_p/M_Z ...

for reference, solar composition means:

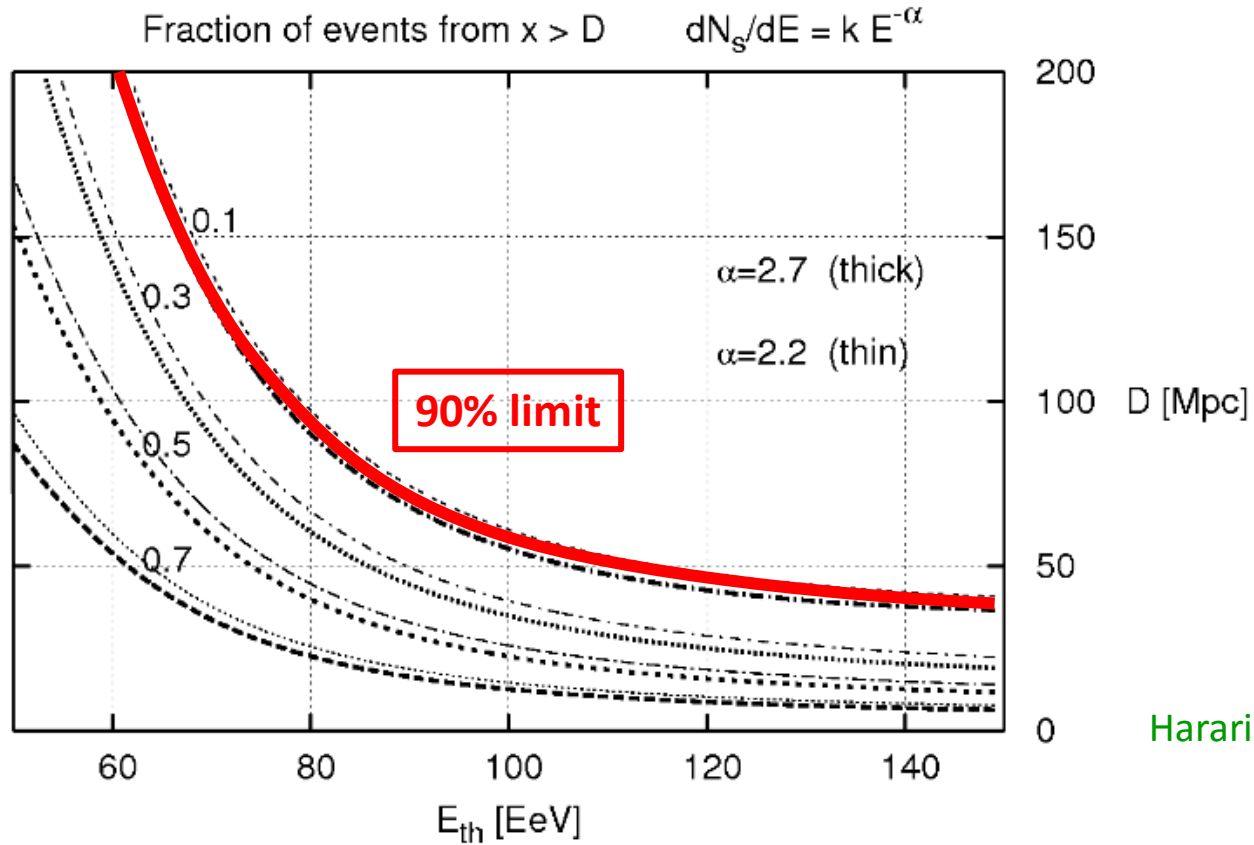
$$\left. \frac{M_{\text{H}}}{M_{\text{CNO}}} \right|_{\odot} \sim 70, \quad \left. \frac{M_{\text{H}}}{M_{\text{Si-group}}} \right|_{\odot} \sim 1000, \quad \left. \frac{M_{\text{H}}}{M_{\text{Fe-group}}} \right|_{\odot} \sim 500$$



→ above $\sim 5 \cdot 10^{19}$ eV, the CMB becomes opaque to UHE protons due to pion production, with energy loss length $\sim 100\text{Mpc}$... and to nuclei through photodisintegration...

→ matches well the cut-off seen by HiRes, Auger, TA at high energies...
... but this cut-off could also represent the maximal energy at acceleration...

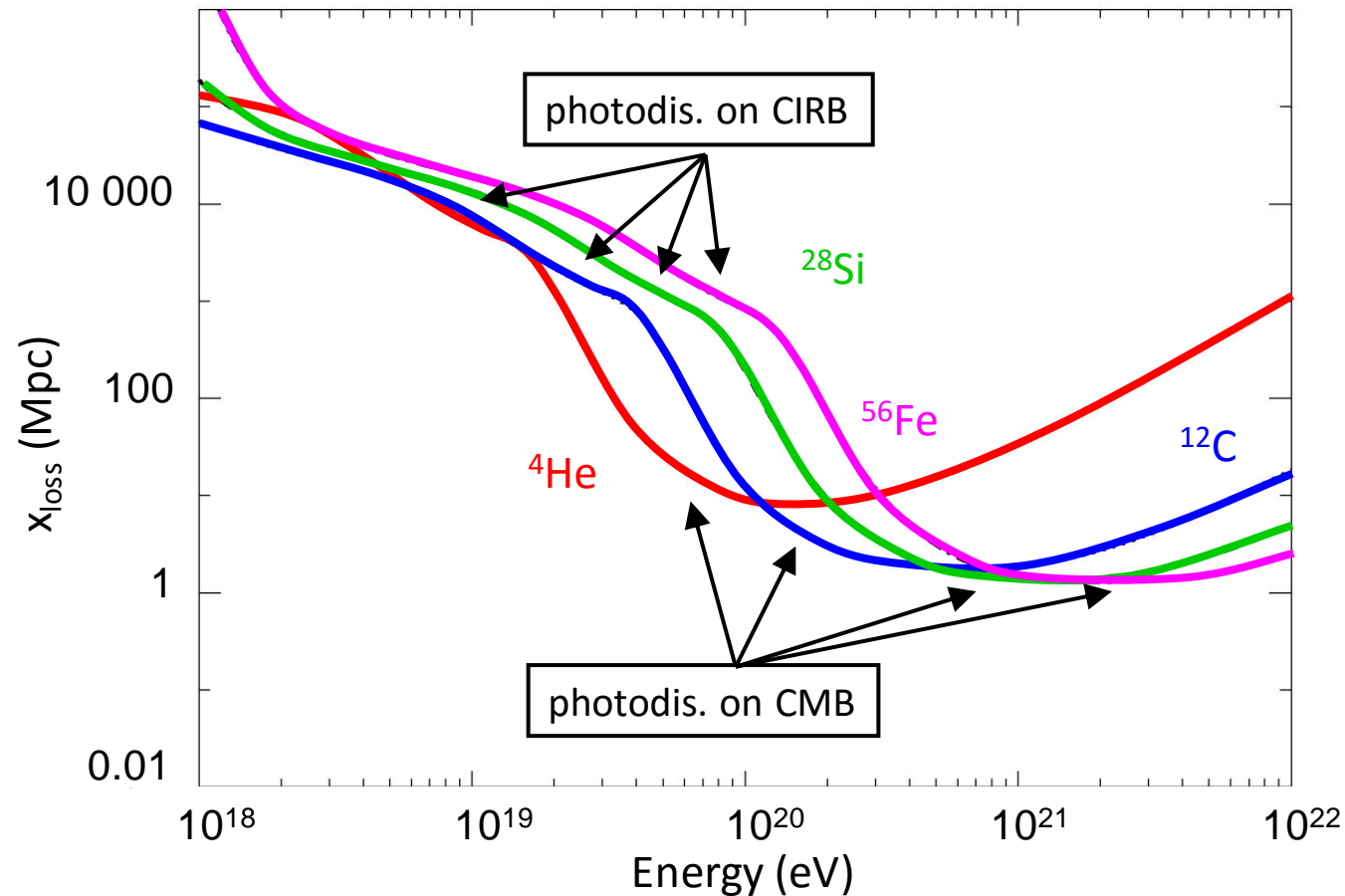
Greisen-Zatsepin-Kuzmin cut-off



Harari+ 06

→ at $6 \cdot 10^{19}$ eV, 90% of protons come from within 200Mpc...

→ at 10^{20} eV, 90% of protons come from within 60Mpc...



→ iron horizon is comparable to that of protons... while intermediate mass nuclei are more fragile, with smaller horizons...

→ in practice: **expect either protons or heavy (Si-Fe-?) nuclei at the highest energies**



Propagation – transport in extra-galactic magnetic fields

Ultra-high rigidities: $r_L \simeq 100 \text{ Mpc } Z^{-1} \left(\frac{E}{10^{20} \text{ eV}} \right) \left(\frac{B}{1 \text{ nG}} \right)^{-1}$

if B follows large scale structure:

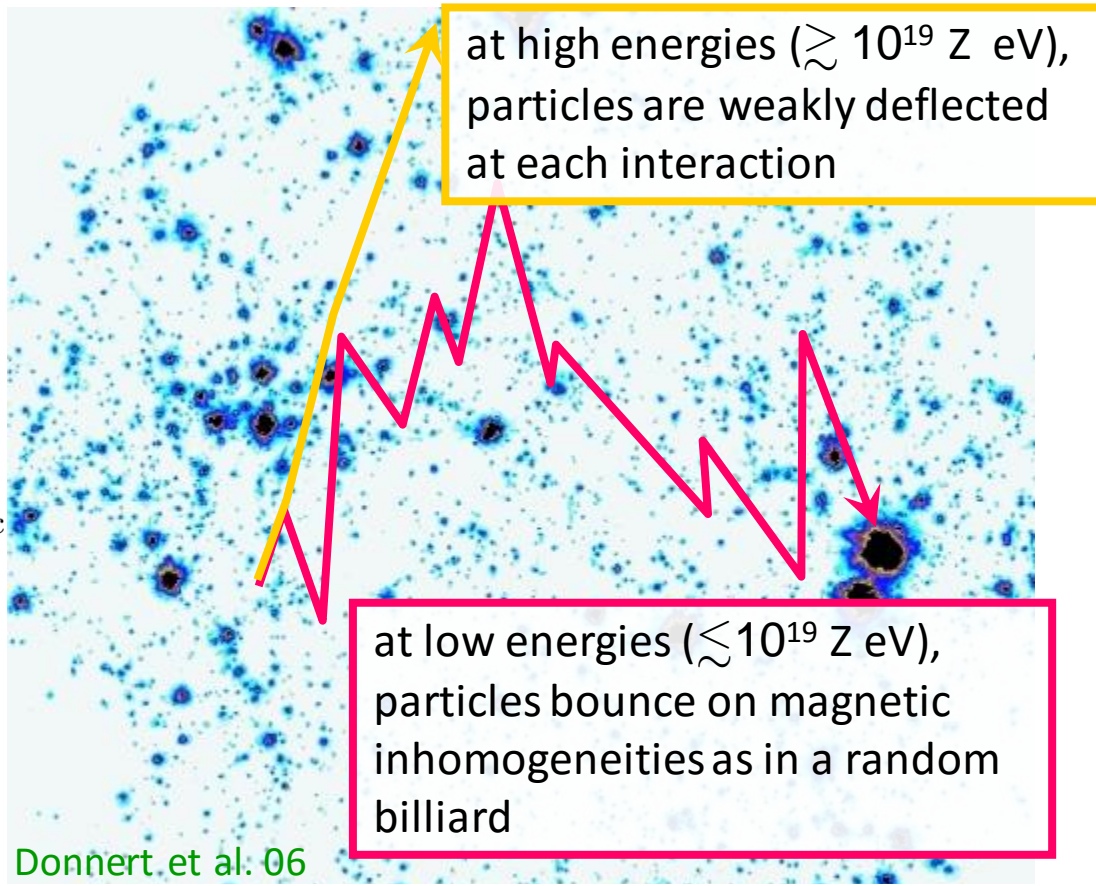
→ particles of different energies probe different structures...

→ at high energies, few interactions with small deflection:

$$\delta\theta_i \sim 1.7^\circ Z E_{20}^{-1} B_{-8} \lambda_{100\text{kpc}}^{1/2} R_{1\text{Mpc}}^{1/2}$$

per interaction, with typical mfp $\sim 30\text{Mpc}$ (Kotera & ML 08)

⇒ a few deg total at $Z 10^{20}$ eV over 100 Mpc...



at high energies ($\gtrsim 10^{19} Z$ eV), particles are weakly deflected at each interaction

at low energies ($\lesssim 10^{19} Z$ eV), particles bounce on magnetic inhomogeneities as in a random billiard

Donnert et al. 06

→ deflection in Galactic magnetic field: a few degrees at $Z 10^{20}$ eV, with direction dependent magnitude...

Expected angular deflection



Integrating over all sources at a given energy:

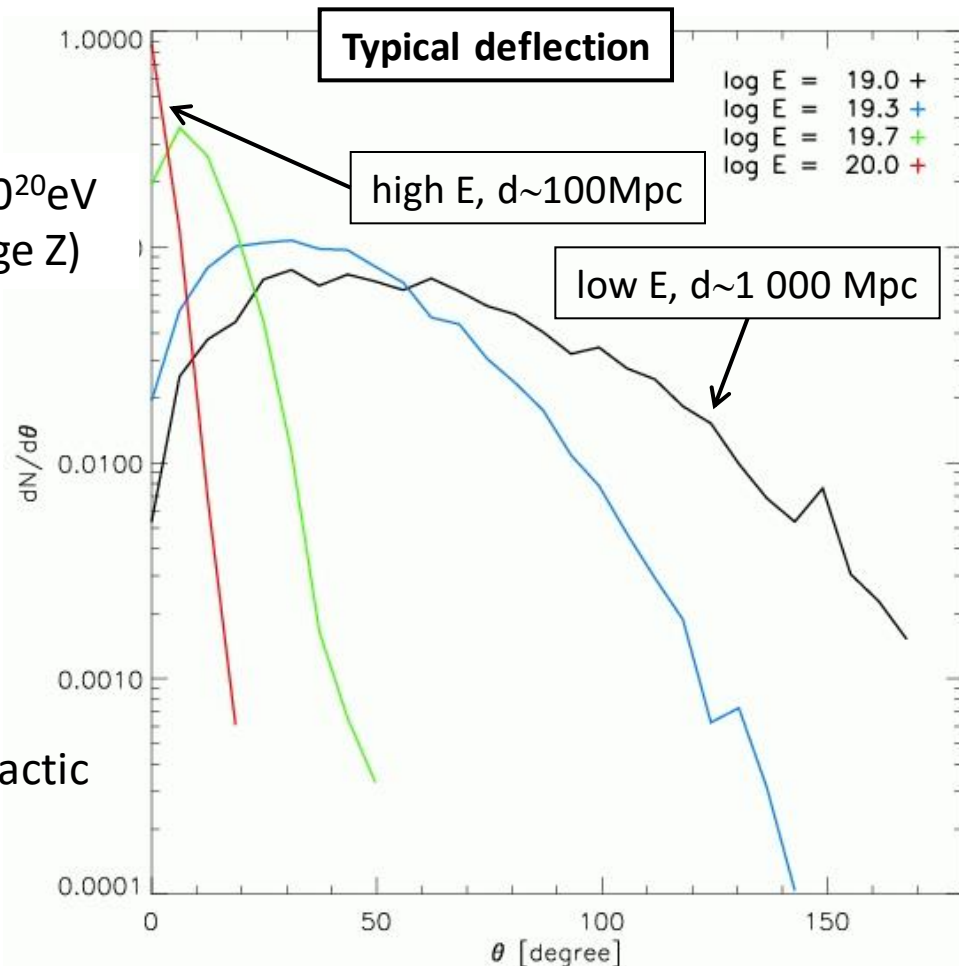
→ note that most of the flux comes from $I_{\max}(E)$ (→ Olbers' paradox!)

$$F(< l) = \int_{r \leq l} d^3r n_{\text{source}} \frac{\dot{N}_{\text{UHECR}}}{4\pi r^2} = n_{\text{source}} \dot{N}_{\text{UHECR}} l$$

⇒ expect a few degrees for protons at 10^{20} eV
 (... Z times more for heavy nuclei of charge Z)

⇒ near isotropy for $E \lesssim 3 \cdot 10^{19} Z$ eV...
 ... small deflection above $5 \cdot 10^{19} Z$ eV

→ deflection of similar magnitude in Galactic magnetic field...



Small angular deflection



→ at high $E/Z \sim 10^{20}$ eV, expect only a few degree deflection over maximal distance:

$$\delta\theta \sim 2^\circ Z \left(\frac{E}{10^{20} \text{eV}} \right)^{-1} \left(\frac{d}{100 \text{ Mpc}} \right)^{1/2} \quad (\times \text{ uncertainty on } B, \lambda)$$

(Waxman&Miralda-Escudé 96)

... small deflection gives rise to a significant time delay τ with respect to photon arrival time and dispersion of arrival times $\Delta\tau \sim \tau$:

$$\tau \sim 10^5 \text{ yrs} \left(\frac{\delta\theta}{2^\circ} \right)^2 \left(\frac{d}{100 \text{ Mpc}} \right) \quad (\times \text{ uncertainty on } B, \lambda)$$

... implying an apparent effective density for transient sources:

$$n_{\text{eff}} = \dot{n} \Delta\tau \sim 10^{-4} \text{ Mpc}^{-3} \left(\frac{\dot{n}}{10^{-9} \text{ Mpc}^{-3} \text{ yr}^{-1}} \right) \left(\frac{\Delta\tau}{10^5 \text{ yrs}} \right)$$

... or 10s of sources in the GZK horizon at 10^{20} eV, but 10^7 sources in the Hubble volume ...

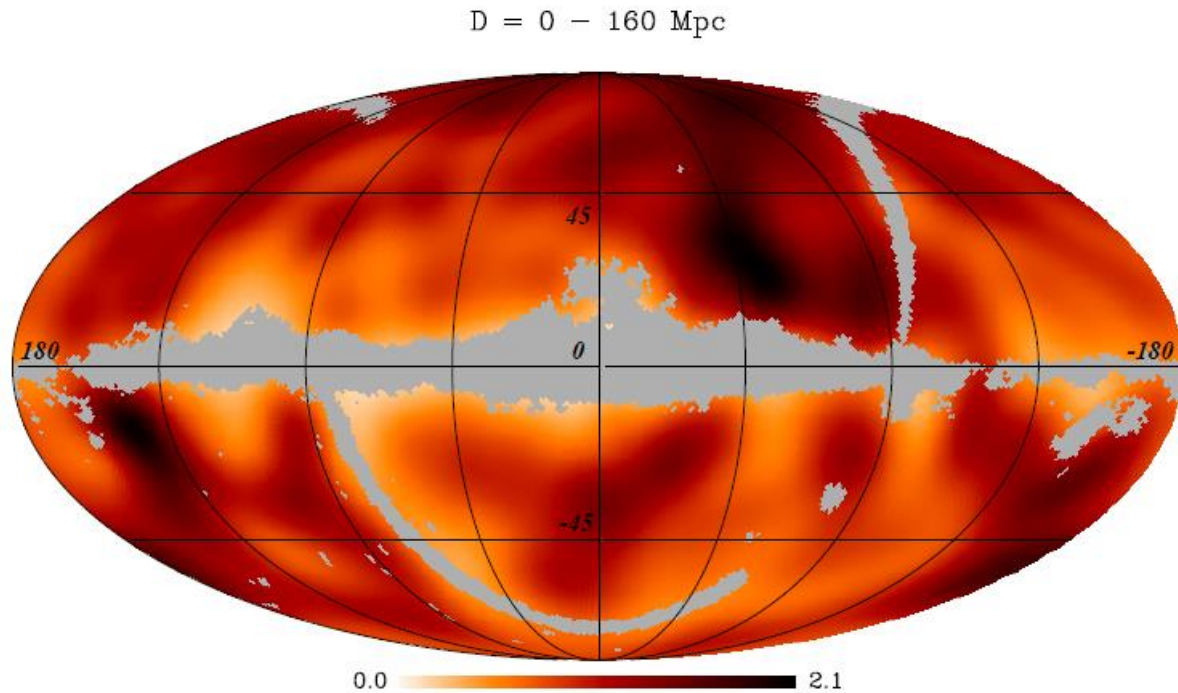
→ **Auger 2013**: absence of multiplets constrains the apparent density:

$$n \gtrsim 0.5 - 1 \times 10^{-4} \text{ Mpc}^{-3} \quad (\text{assuming } \delta\theta < 10^\circ \text{ at } >60 \text{ EeV})$$

Small angular deflection and correlations to catalogs



→ if sources follow large scale structure, correlations remain weak for energies > 50 EeV because of large integration depth (+deflection):



Kotera+ML08

column density of galaxies in PSCz survey integrated up to 160Mpc

→ [Kashti+Waxman 08](#), [Oikonomou+13](#): need 300 events above 40EeV to achieve 99%cl for negligible angular deflection

→ [Auger 15](#): no clear indication of correlation with large scale structure (600 events above 40EeV)

Large angular deflection



→ at low $E/Z \sim 10^{18}$ eV, expect strong deflection and diffusion once $d > l_{\text{scatt}}(E)$...

... observational constraint on source density relaxed... 1 source within 50Mpc:

$$n \gtrsim 10^{-6} \text{ Mpc}^{-3}$$

... possible existence of a magnetic horizon (for steady sources only)

$$r_{\text{horizon}} \sim \sqrt{cl_{\text{scatt}}/H_0} \sim 60 \text{ Mpc } l_{\text{scatt},1\text{Mpc}}^{1/2} < n^{-1/3}?$$

(ML 05, Aloisio+ 05)

... weak anisotropies if any: a weak dipole from nearby sources? (Harari+ 15)

Auger, ICRC2015

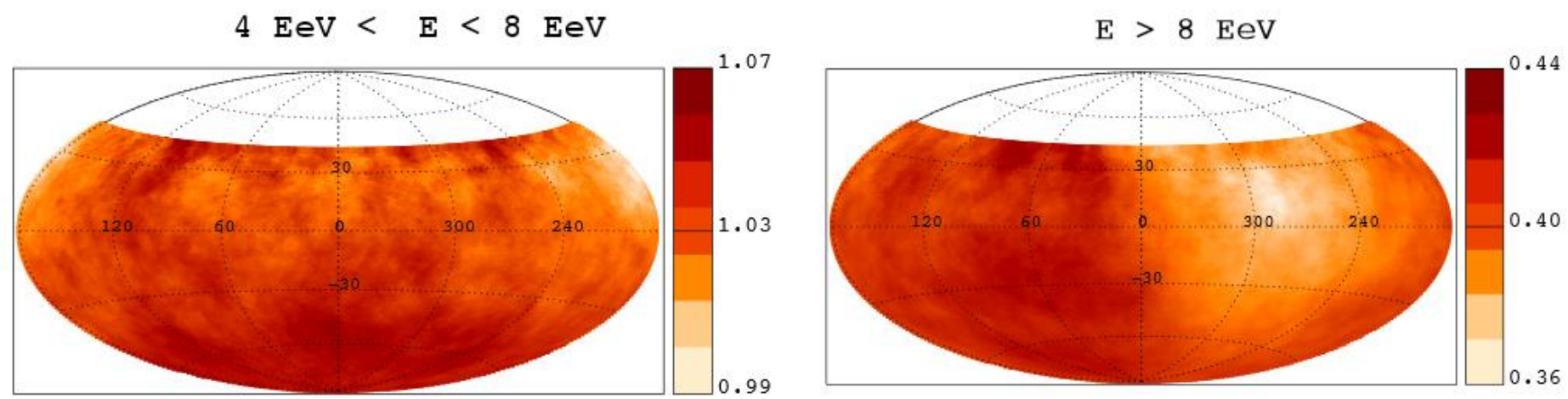


Figure 2: Sky map in equatorial coordinates of flux, in $\text{km}^{-2} \text{yr}^{-1} \text{sr}^{-1}$ units, smoothed in angular windows of 45° radius, for observed events with energies $4 < E < 8 \text{ EeV}$ (left) and $E > 8 \text{ EeV}$ (right).

Pierre Auger Observatory 2015 dipole above 8 EeV: amplitude 7%

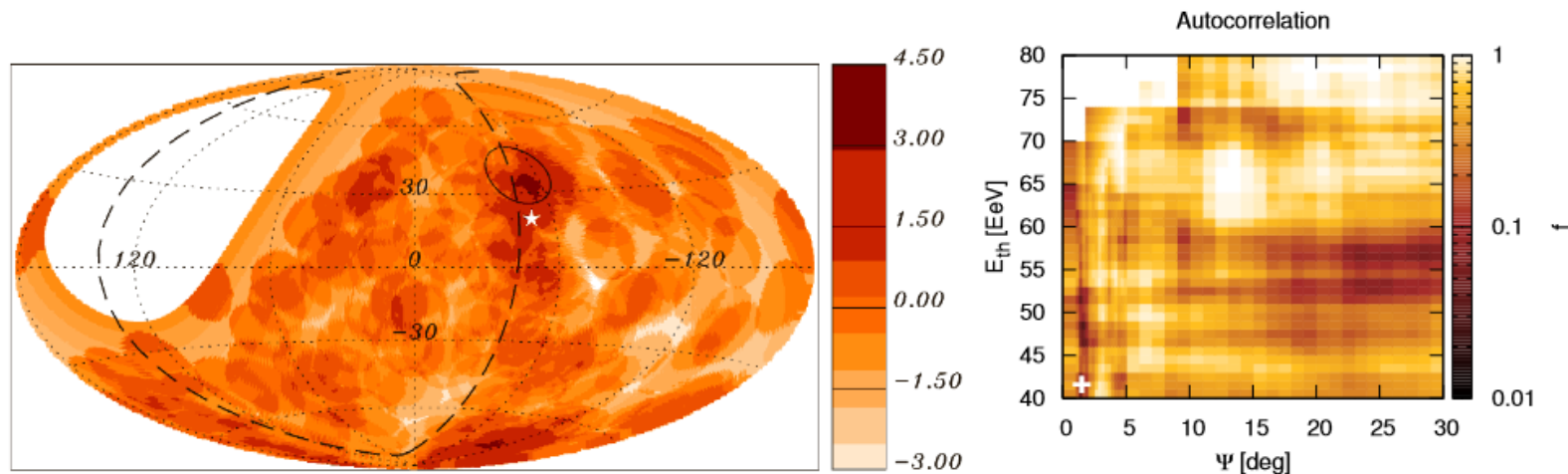
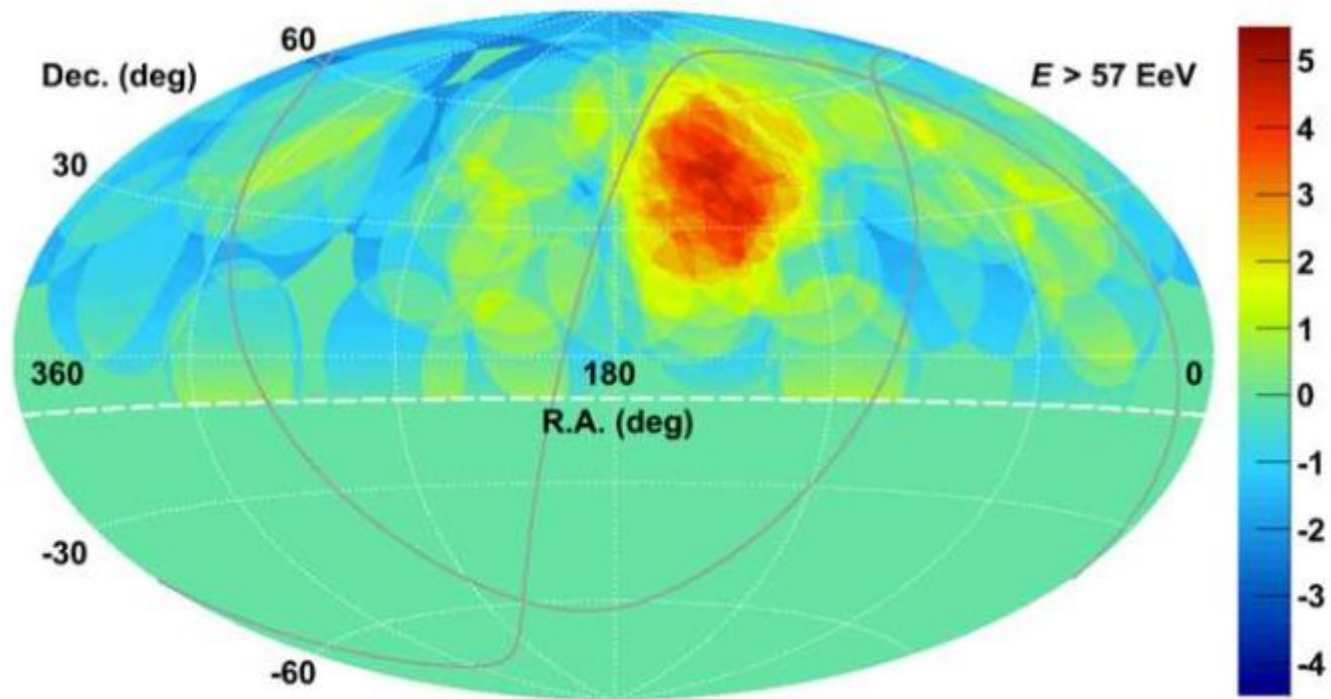


Figure 1: *Left:* map in galactic coordinates of the Li-Ma significances of excesses in 12° -radius windows for the events with $E \geq 54$ EeV. Also indicated are the Super-Galactic Plane (dashed line) and Centaurus A (white star). *Right:* Fraction f obtained in the autocorrelation of events versus ψ and E_{th} , white cross indicating the minimum.

Pierre Auger Observatory 2015 anisotropy map: consistent with isotropy...

... a slight excess close to Cen A direction, but significance not below 1%



Telescope Array 2014 anisotropy map – Li-Ma excess significance:

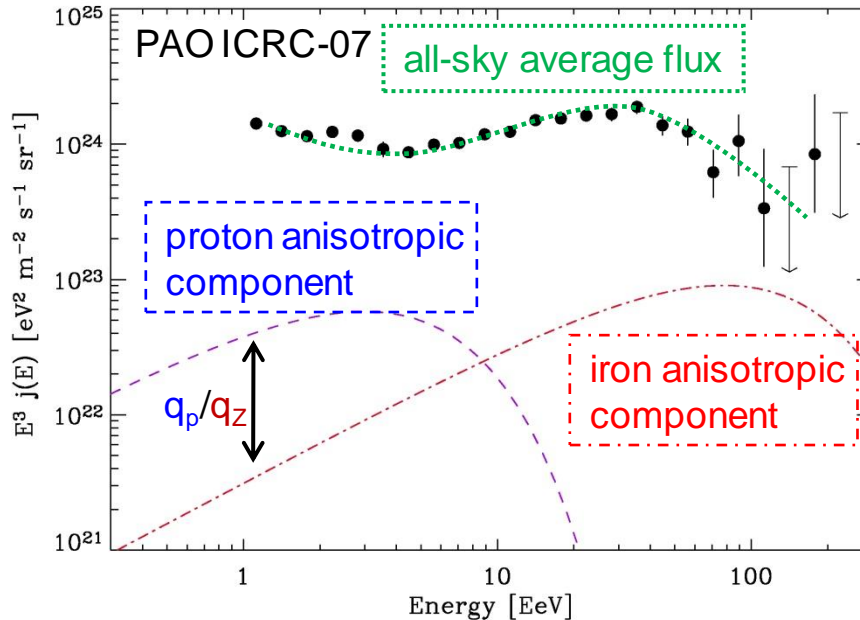
... a hot-spot seen with a (post-trial) significance of 3.4 sigma...

Anisotropies vs heavy composition at UHE



→ if anisotropic signal $>E$ is due to heavy nuclei, then one should detect a stronger anisotropy signal associated with protons of same magnetic rigidity at $>E/Z$ eV...

argument independent of intervening magnetic fields... (M.L. & Waxman 09)



- injection shaped by rigidity, $s=2$:

$$E_{\max} \propto Z$$
- composition: $q_p/q_{\text{Fe}} = 1/0.06$ as in sources of GCR

→ signal-to-noise at low energy vs that at high energy:

$$S/N|_p (> E/Z) \simeq \underbrace{\alpha_{\text{loss},Z}}_{> 1} \underbrace{Z^{-0.85}}_{< 1} \underbrace{\frac{N_p}{N_Z}}_{\gg 1} S/N|_Z (> E)$$

$$\underbrace{\hspace{10em}}_{\gg 1}$$

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$\gg 1$

→ if anisotropies are seen at $>E$, say >50 EeV, but not at any E/Z , with $Z \sim 6-26$, then the following assertions cannot hold simultaneously:

- (1) the anisotropy signal at $>E$ is real (=not a statistical accident)
- (2) the composition at energies $>E$ is heavy: O, Si, Fe...
- (3) the sources have a "reasonable" metallicity $N(Z>6)/N(Z=1) \ll 1$

⇒ if anisotropies are not statistical accidents, there exist GZK protons, or the source metallicity is extraordinarily large...

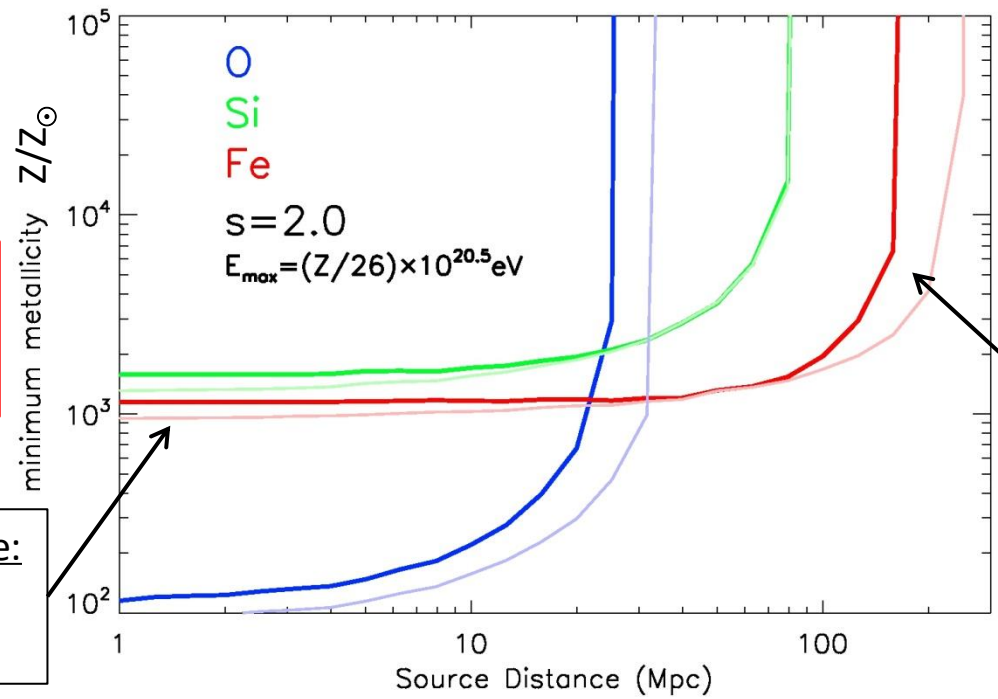
*NB: does not depend on spectral index of injection spectrum...
only assumption: particle spectra are shaped by rigidity...*



Anisotropies vs heavy composition at UHE

→ taking into account photodisintegration, nuclei with energy $>2E$ produce protons with energy $>E/Z$, which add up to the anisotropy signal... Liu+ 13

$$S/N|_p (> E/Z) \simeq Z^{-0.85} A \left[\frac{M_p}{M_Z} + 2^{1-s} f_{\text{photodis.}} (> 2E) \right] S/N|_Z (> E)$$



minimum Z/Z_{solar} to ensure: $S/N_p (E/Z) < S/N_Z (E)$

close-by source: no photo-dis. $Z \rightarrow p$

remote source: secondary p's from photo-dis. of $>2E$ nuclei produce anisotropies at E/Z

Liu+ 13

→ anisotropies at E could thus be produced by heavy nuclei **only** if the source metallicity:
 if Fe at UHE: $Z \gtrsim 1000 Z_{\odot}$; if Si at UHE: $Z \gtrsim 1600 Z_{\odot}$; if O at UHE: $Z \gtrsim 100 Z_{\odot}$
 ... sources with such high metallicities?



→ (Robust) Constraints on the sources of ultra-high energy cosmic rays:

→ highly powerful sources (from theory): $L \gtrsim 10^{45} \text{ erg/s } Z^{-2} \mathcal{A}^2 E_{20}^2$

→ injection rate (from exp.): $\dot{i} \sim 10^{44} \text{ erg Mpc}^{-3} \text{ yr}^{-1}$

→ large apparent density (from exp.): $n \gtrsim 10^{-6} - 10^{-4} \text{ Mpc}^{-3}$

→ Composition controls the phenomenology of this field:

→ experimentally: strong signatures from protons, weak signatures from heavies

→ theoretically: restricted landscape for proton sources, enlarged for heavies

→ Existence of anisotropies at GZK energies (if confirmed) constrains composition:

→ either protons at GZK, or an extremely metal-rich source with $Z > 100 Z_{\odot}$