



# The TRINAT Trap Program

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## Outline

Limit on Scalar Interaction

Upgraded Experiment and Projected Precision

Limit on Right-Handed Currents

Upgraded Experiment and Projected Precision

Limit on Tensor Interaction

Upgraded Experiment and Projected Precision

## $\beta$ -decay rate (Jackson, Treiman, Wyld 1957):

$$dW = dW_o \left( 1 + \frac{\vec{p}_\beta \cdot \vec{p}_\nu}{E_\beta E_\nu} a_{\beta\nu} + \frac{\Gamma m_e b}{E_\beta} + \frac{\vec{J}}{J} \cdot \left[ \frac{\vec{p}_\beta}{E_\beta} A_\beta + \frac{\vec{p}_\nu}{E_\nu} B_\nu + \frac{\vec{p}_\beta \times \vec{p}_\nu}{E_\beta E_\nu} D \right] \right. \\ \left. + c \left[ \frac{\vec{p}_\beta \cdot \vec{p}_\nu}{3E_\beta E_\nu} - \frac{(\vec{p}_\beta \cdot \vec{j})(\vec{p}_\nu \cdot \vec{j})}{E_\beta E_\nu} \right] \left[ \frac{J(J+1) - 3 \langle (\vec{J} \cdot \vec{j})^2 \rangle}{J(2J-1)} \right] \right)$$

Allows for: V - A, Scalar, Tensor Interactions

Left, Right-handed currents

Time-reversal violation

$a_{\beta\nu}$ ,  $b$ ,  $c$ ,  $A_\beta$ ,  $B_\nu$ ,  $D$ : values predicted by the Standard Model

Recent review: S. Severijns and M. Beck, Rev. Mod. Phys. 78 991 (2006)

**Measurements feasible using Atom traps and Radioactive Beams.**

## Limits on Scalar Boson Interaction

$$dW = dW_o \left( 1 + \frac{\vec{p}_\beta \cdot \vec{p}_\nu}{E_\beta E_\nu} a_{\beta\nu} + \frac{m_e}{E_\beta} b + \frac{\vec{J}}{J} \cdot \left[ \frac{\vec{p}_\beta}{E_\beta} A_\beta + \frac{\vec{p}_\nu}{E_\nu} B_\nu + \frac{\vec{p}_\beta \times \vec{p}_\nu}{E_\beta E_\nu} D \right] \right. \\ \left. + c \left[ \frac{\vec{p}_\beta \cdot \vec{p}_\nu}{3E_\beta E_\nu} - \frac{(\vec{p}_\beta \cdot \vec{j})(\vec{p}_\nu \cdot \vec{j})}{E_\beta E_\nu} \right] \left[ \frac{J(J+1) - 3 \langle (\vec{J} \cdot \vec{j})^2 \rangle}{J(2J-1)} \right] \right)$$

**For pure Fermi  $0^+ \rightarrow 0^+$  decay  $\beta - \nu$  angular correlation:**

$$P(\theta) = 1 + b \frac{m_\beta}{E_\beta} + a_{\beta\nu} \frac{v_\beta}{c} \cos(\theta)$$

$$a_{\beta\nu} = 1 - 4 \frac{g_S^2}{g_V^2} (|a_L^S|^2 + |a_R^S|^2) \quad b = \pm \frac{g_S}{g_V} \frac{\text{Re}(a_{LL} a_R^S)}{|a_{LL}|^2}$$

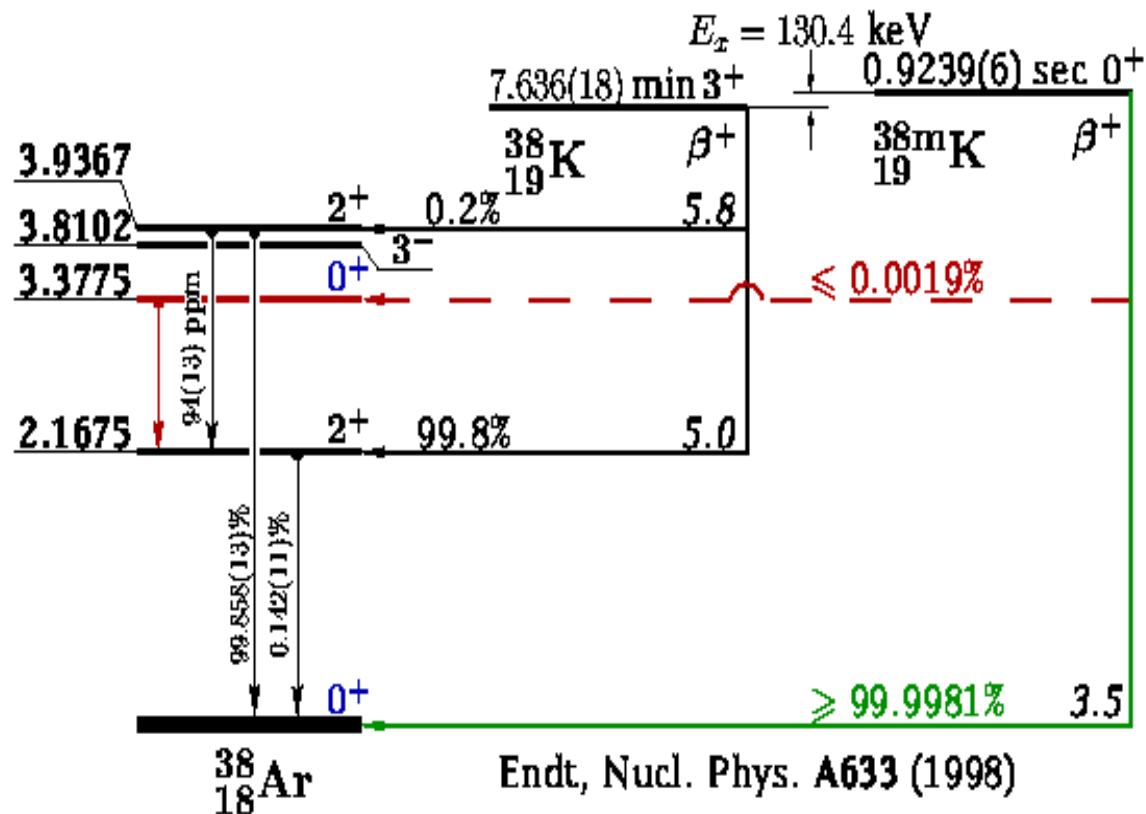
$$a_L^S = A_{LL} + A_{LR} \quad a_R^S = A_{RR} + A_{RL}$$

**SM:  $b = 0$ ,  $a_{\beta\nu} = 1.0$ .**

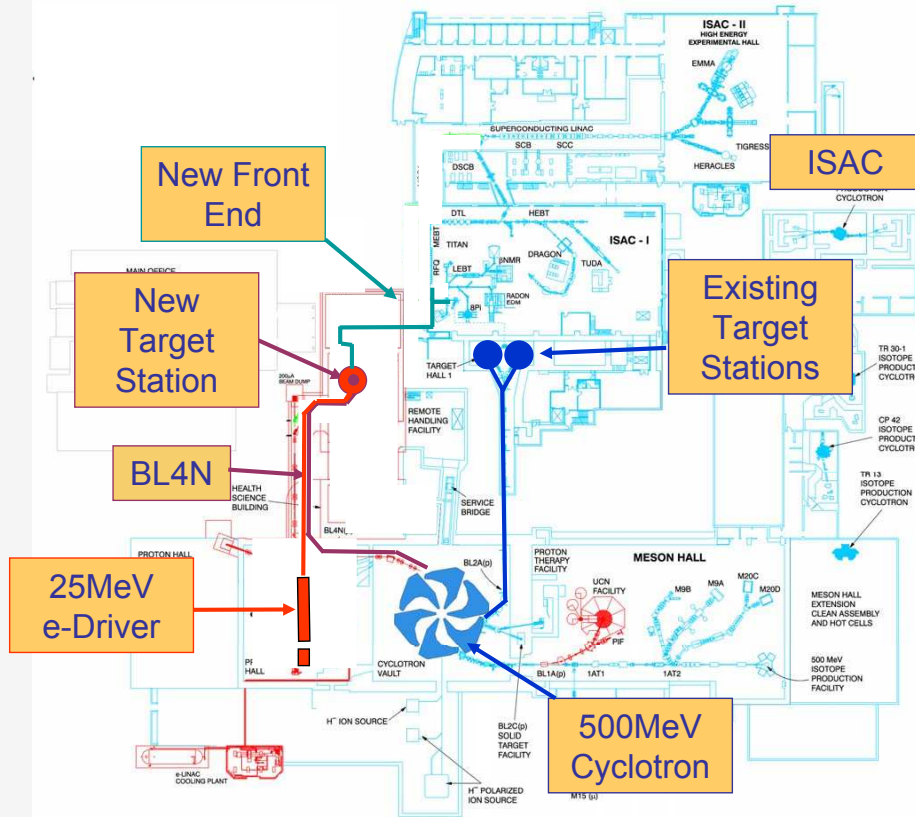
**$C_S + C'_S \sim 0.001$  in MSSM, Profumo et al., PRD 75 075017**

# Measurement of $\beta - \nu$ Angular Correlation in $^{38m}\text{K} \xrightarrow{\beta^+} ^{38}\text{Ar}$

$$Q(^{38m}\text{K}) = 5.02234(12) \text{ MeV}$$



# Future (2010-2015)



## Proposal:

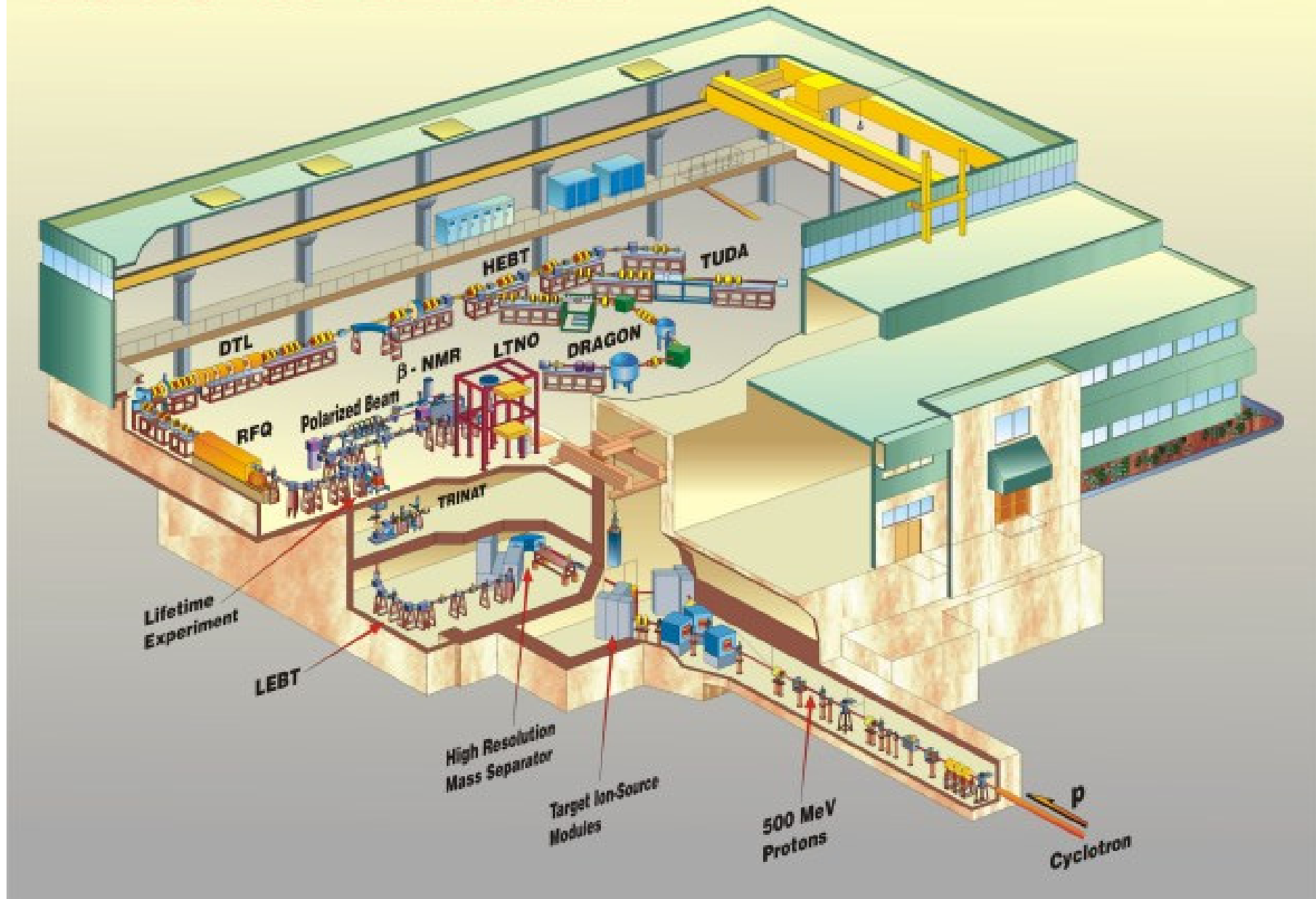
### By 2013:

- Add a 25MeV electron driver to supply electrons to one new target
- Add a new ISAC front-end to deliver a second RIB beam to ISAC

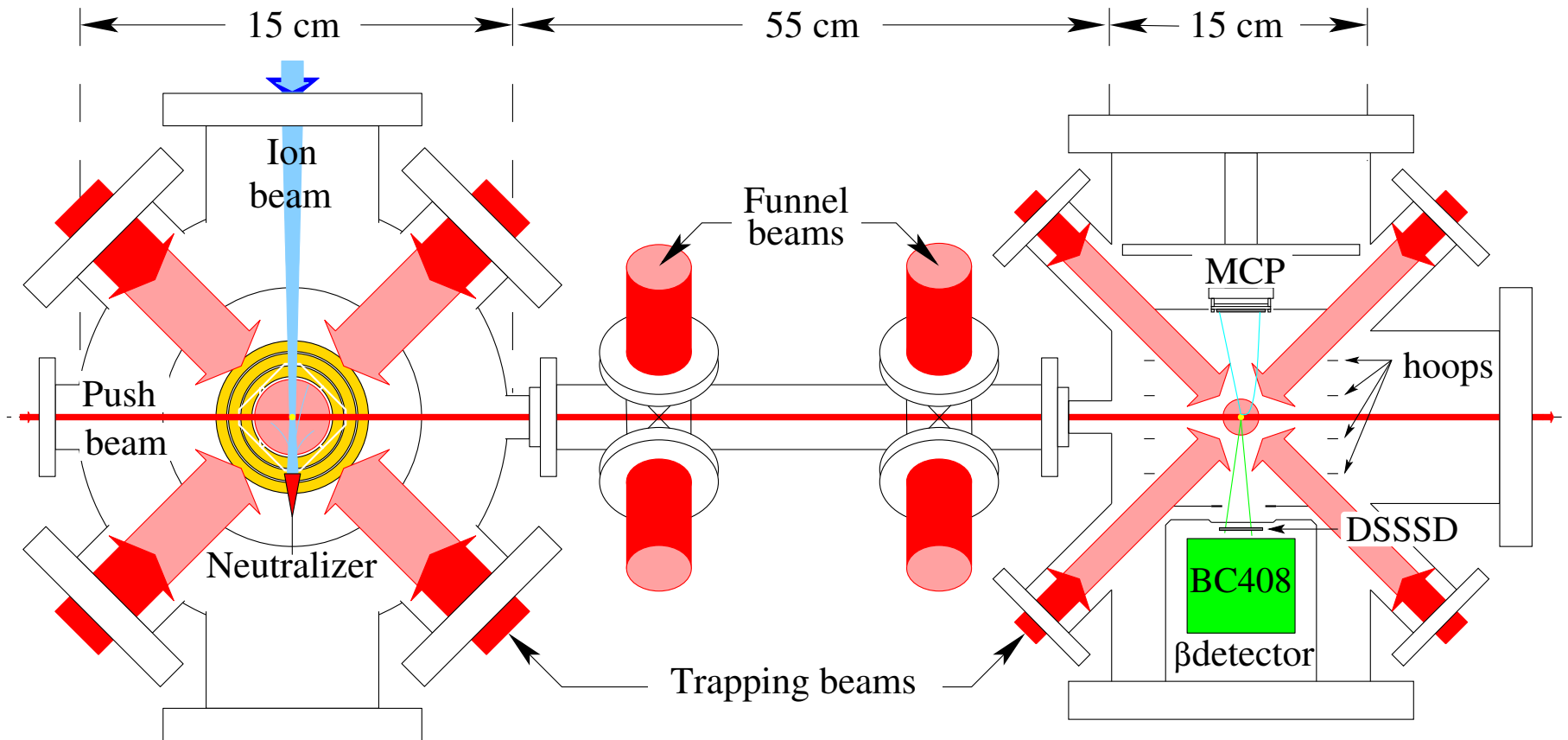
### By 2015:

- Add a new beam line from the cyclotron to deliver 500MeV protons to the new target

# ISAC at TRIUMF



# TRINAT DOUBLE MOT TRAPPING SYSTEM



## Collection chamber

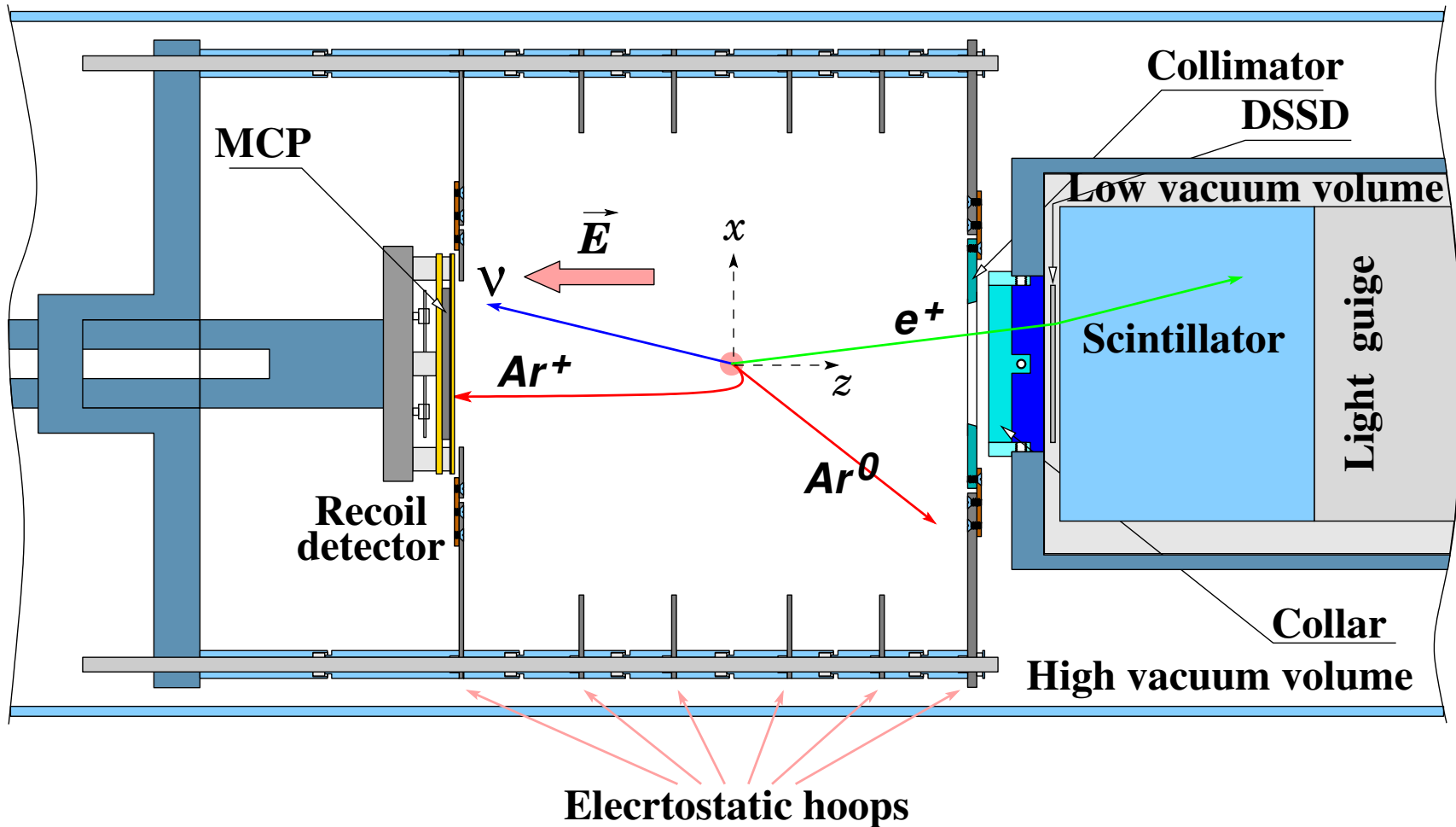
- 95%  $^{38\text{gs}}\text{K}^+$  ( $t_{1/2} = 7.64$  min) + 5%  $^{38\text{m}}\text{K}^+$  ( $t_{1/2} = 0.924$  s)
- neutralization of  $^{38}\text{K}^+$
- vapor cell trap
- $10^{-8}$  Torr
- 0.1% of  $^{38\text{m}}\text{K}$  trapped
- 75% of trapped  $^{38\text{m}}\text{K}$  moved

## Detection chamber

- 100%  $^{38\text{m}}\text{K}$ ,  $t_{1/2} = 0.924$  s
- retrap from atomic beam
- $3 \cdot 10^{-10}$  Torr,  $t_{1/2}^{\text{trap}} = 30$  s
- 0.75 mm FWHM trap size
- 2000 atoms in trap
- photoionization of  $^{38\text{m}}\text{K}$

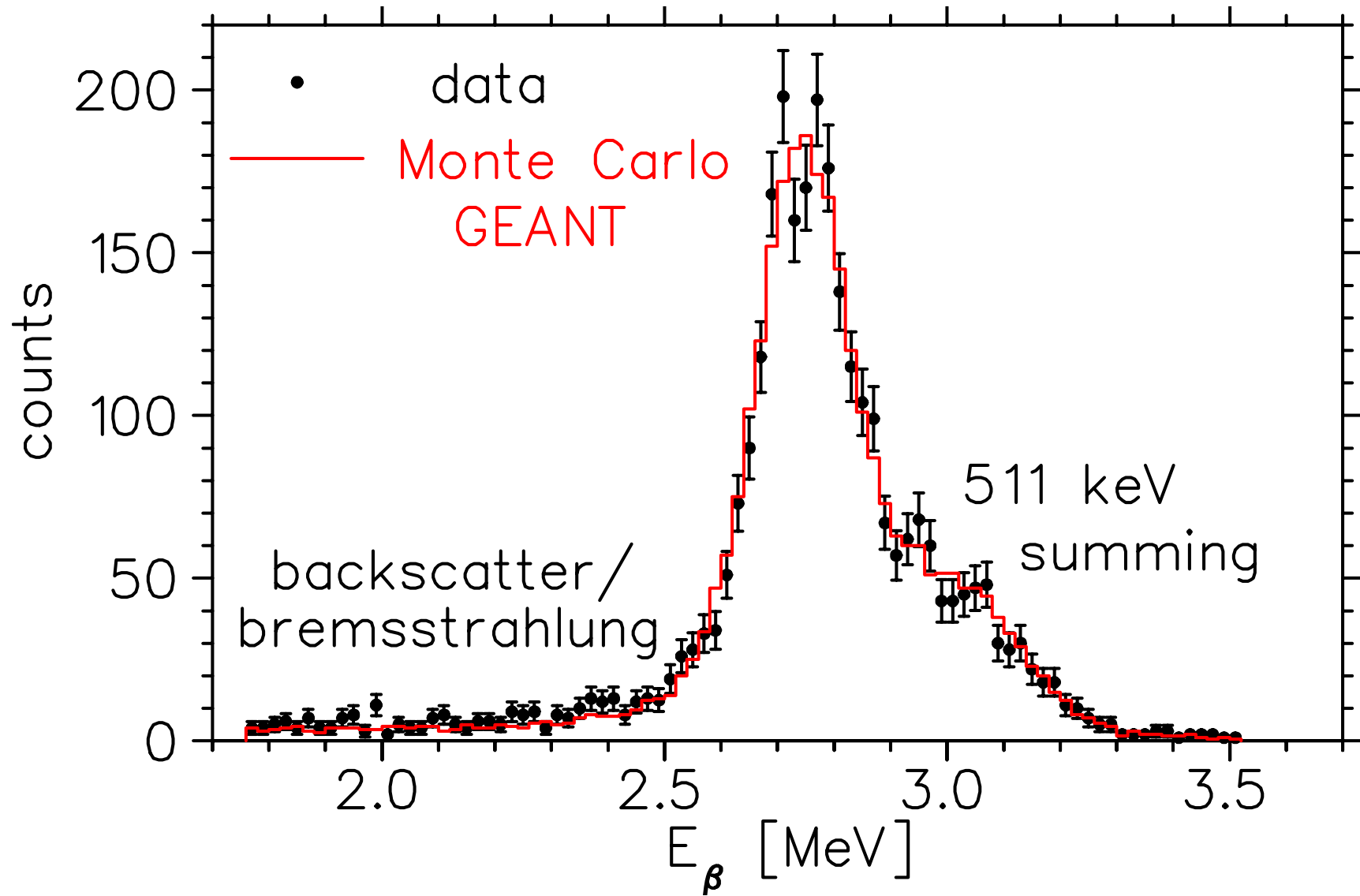


# TRINAT DETECTION SYSTEM FOR $^{38}\text{mK}$ DECAY



- High recoil collection and detection efficiencies due to  $E$ -field
- Coincident detection of  $e^+$  and recoils back-to-back
- Position information both from  $e^+$  and recoil detectors
- Possibility to measure  $p_e$  and  $p_{recoil}$  and using them to determine  $p_\nu$ .
- Chamber geometry suppresses recoiling ion detection from decays on walls and electrostatic hoops

# Exploiting over-determined kinematics



Results: A. Gorelov *et al.*, PRL 94, 142501 (2005)

$$P(\theta) = 1 + b \frac{m_\beta}{E_\beta} + a_{\beta\nu} \frac{v_\beta}{c} \cos(\theta)$$

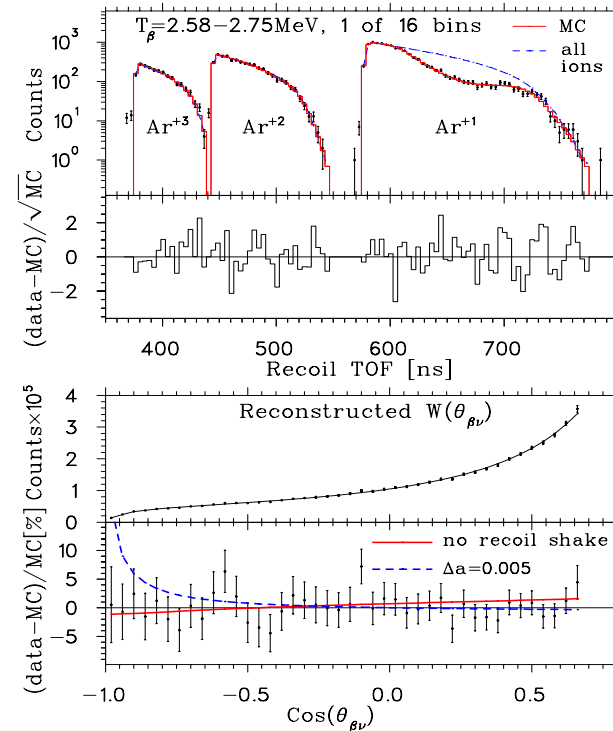
For  $|b| < 0.04$ ,  $\langle E_\beta \rangle = 3.3$  MeV

Define:

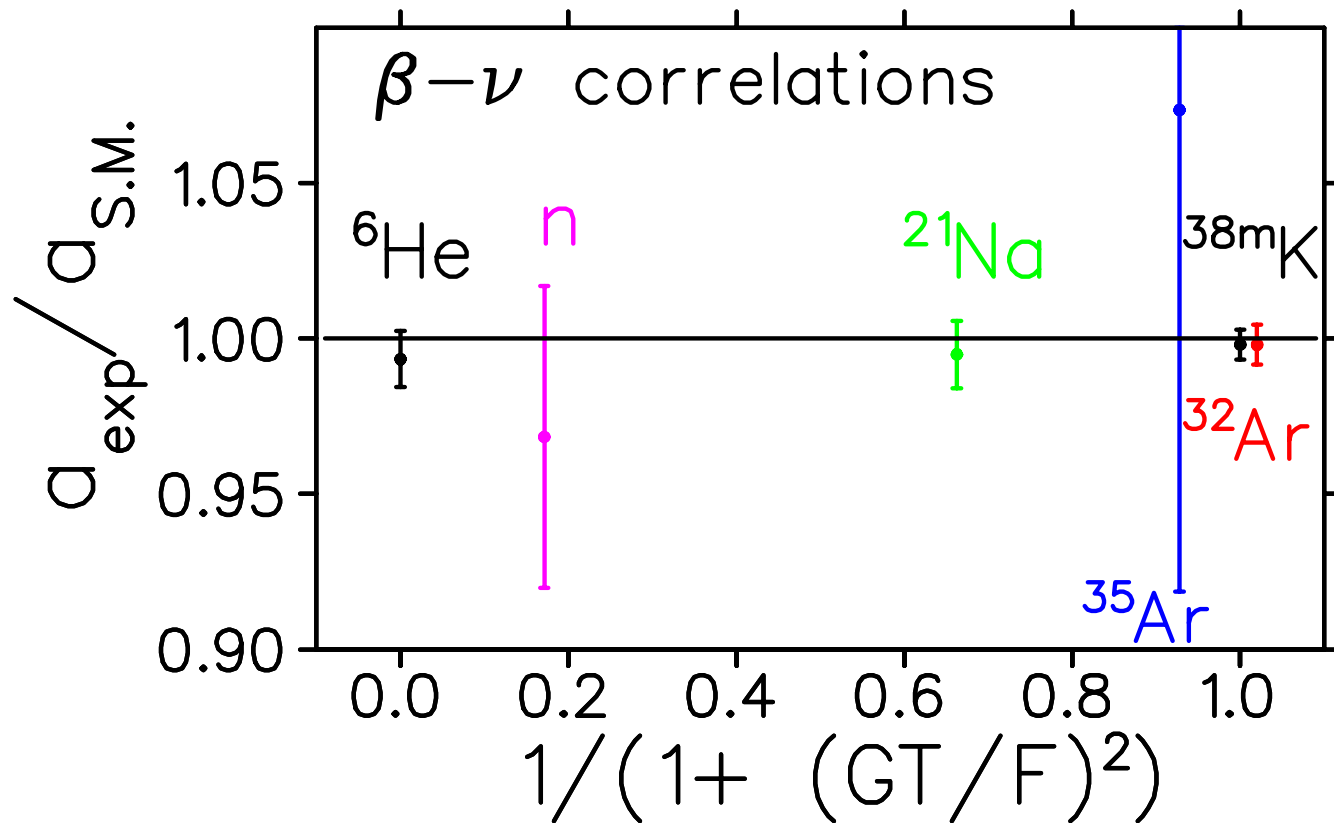
$$\tilde{a} = \frac{a_{\beta\nu} m_\beta}{1 + b \langle E_\beta \rangle}$$

$$\tilde{a} = 0.9981 \pm 0.0030^{+0.0032}_{-0.0037}$$

In agreement with the Standard Model.



## Summary of results for a



$^{32}\text{Ar}$ : E. G. Adelberger et al., Phys. Rev. Lett. 83, 1299(1999)

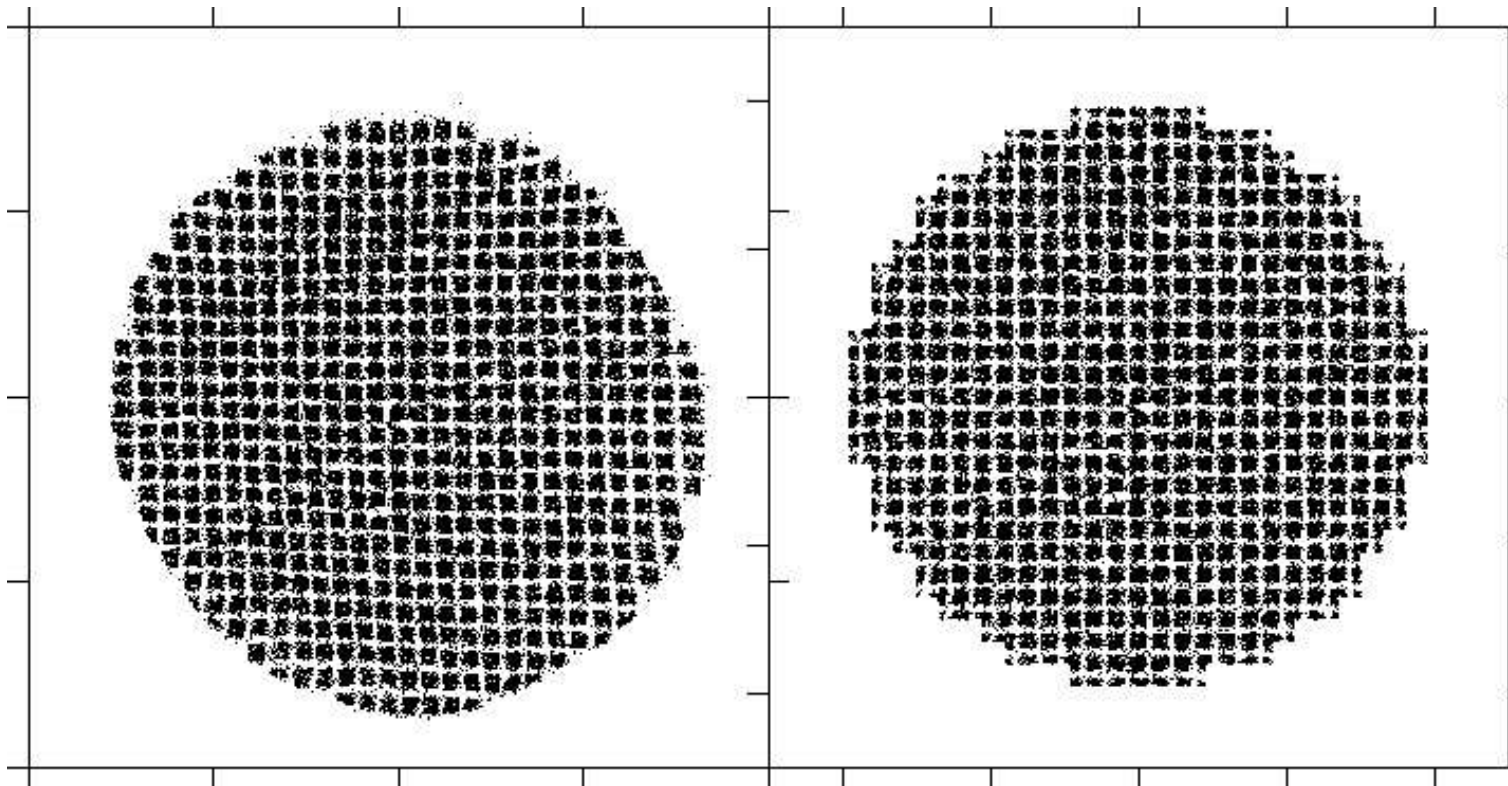
$^{38m}\text{K}$ : A. Gorelov et al., PRL 94, 142501 (2005)

$^{21}\text{Na}$ : P.A. Vetter et al., Phys. Rev. C77, 035502 (2008)

# Upgraded System for $^{38m}\text{K}$ decay measurement

- Reduce all systematic and statistical errors:
- New, larger MCP detector and  $\beta$  telescope - near 100% acceptance for ions. Improved low  $E_\beta$  detection for Fierz term measurement.
- Time and momentum focusing for better resolution and charge state separation.
- Higher beam intensity:  $40\mu\text{A}$  vs.  $1\mu\text{A}$  in previous experiment.
- New chamber design to accomodate all the above.

# RECOIL DETECTOR SPATIAL CALIBRATION



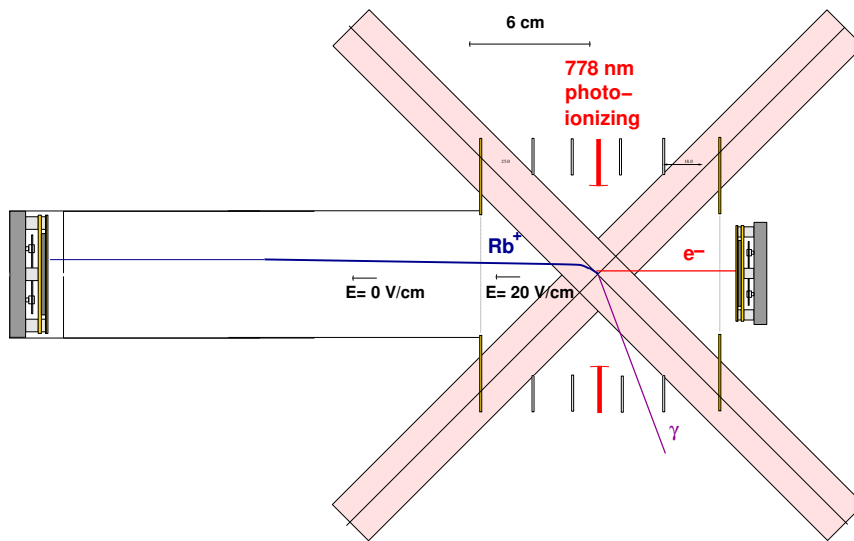
Calibration performed with precise mask (2mmx2mm hole, 1mm strip) and  $^{148}\text{Gd}$  source. Evaluated resolution 0.25mm.

# Time Focussing: $p_{recoil}$ FROM 2% I.C. DECAY OF $^{86m}\text{Rb}$

K,L  $e^-$

$p = 920,932 \text{ keV/c}$

$\Delta p/p \approx 0.03$



6-

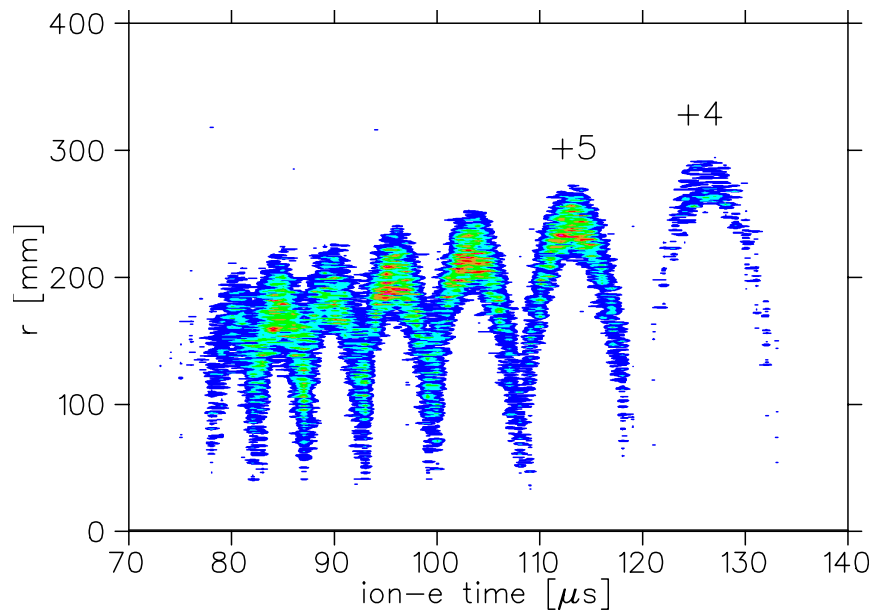
1.0 m

1.0 m

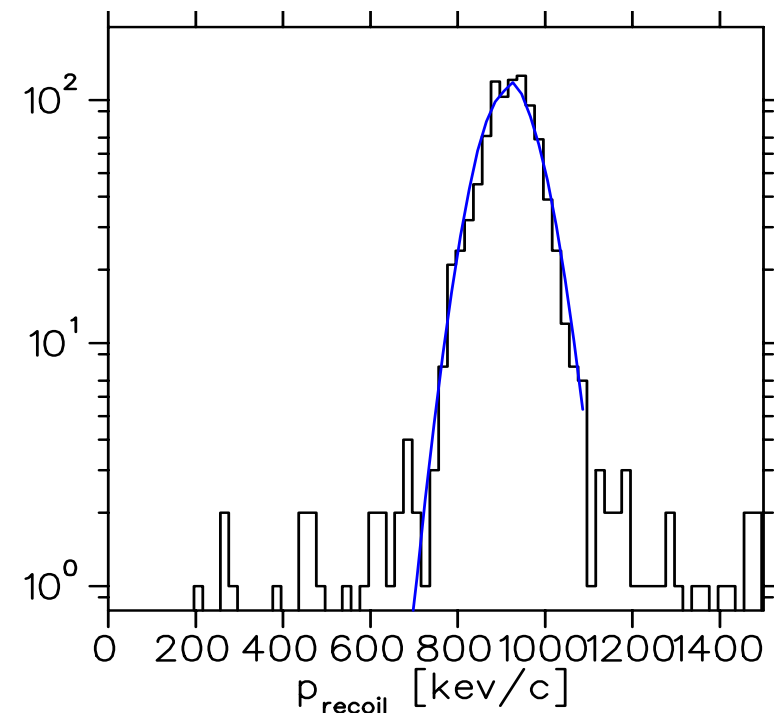
556 keV

2-

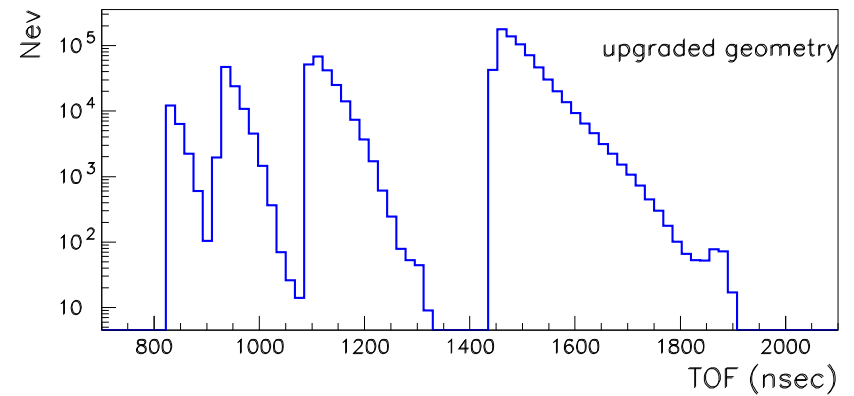
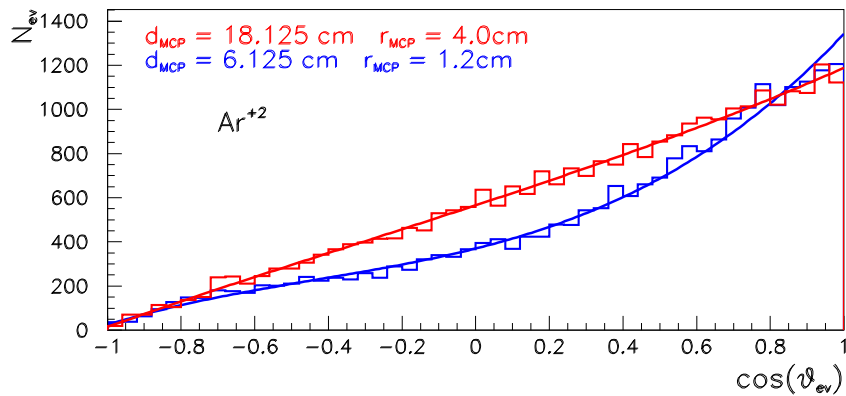
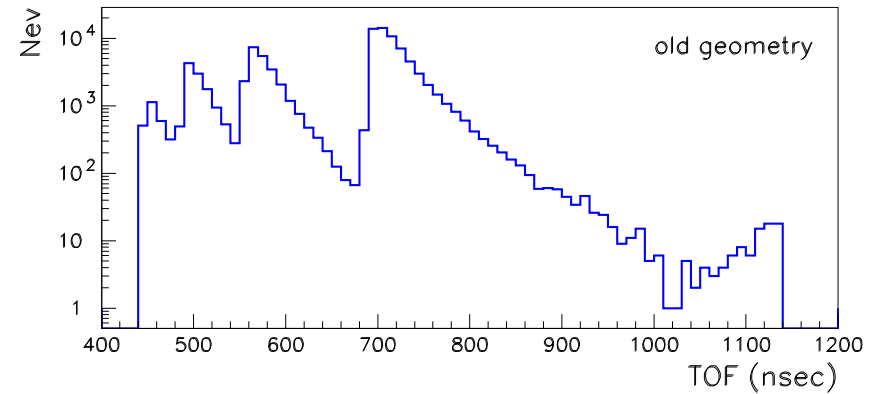
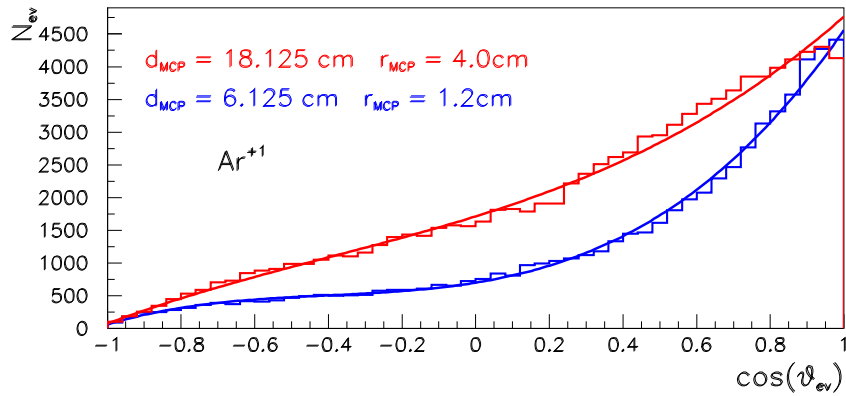
$^{86}\text{Rb}$



counts



## Simulations for $^{38m}\text{K}$ decay



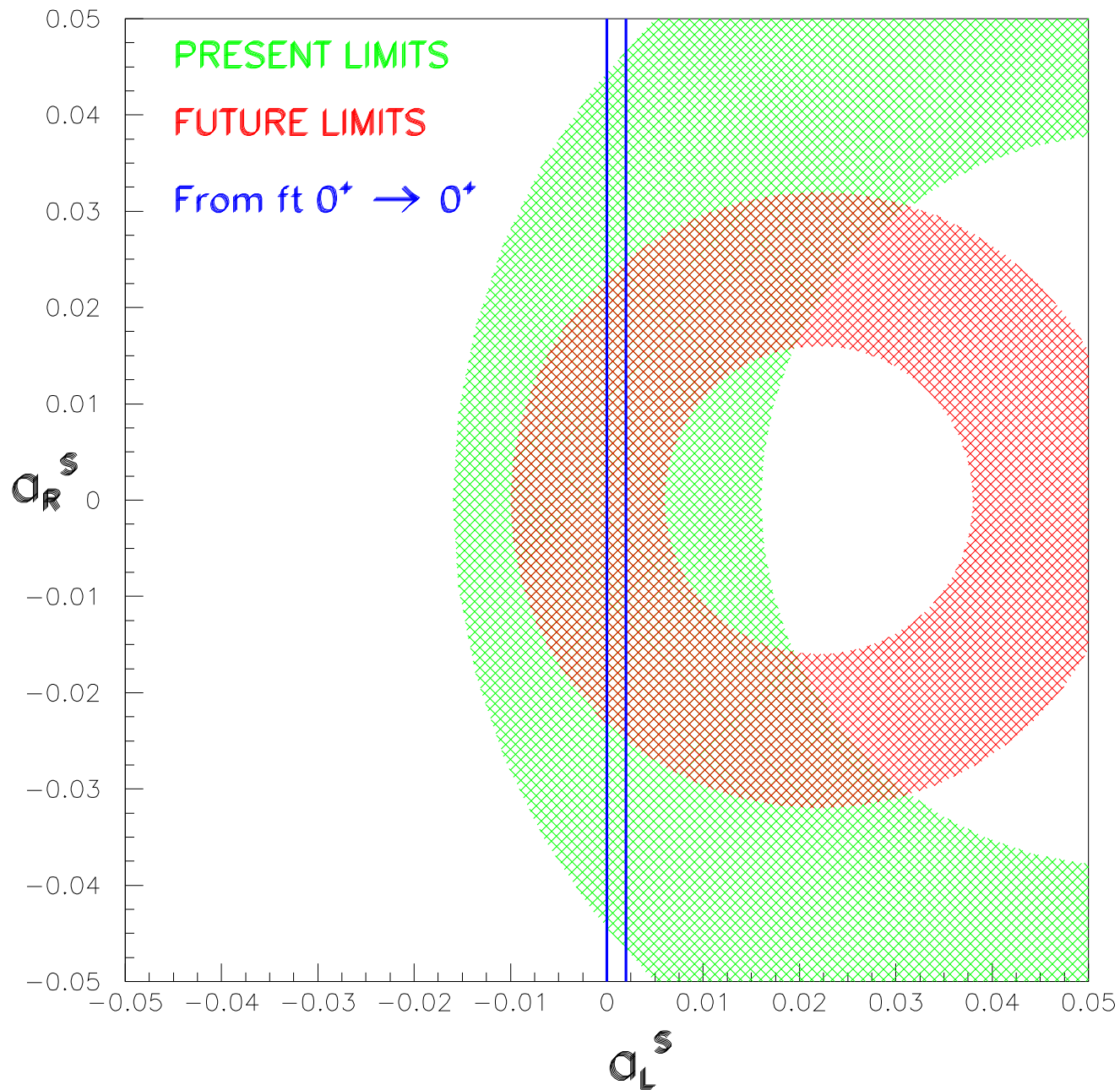


# PRESENT AND PLANNED ERRORS ( $^{38m}\text{K}$ decay)

	PRESENT	FUTURE
<b>Applied electric field</b>		
E-field non-uniformity	0.0010	0.0003
E-field/trap size	0.0012	0.0004
<b>Beta-detector response</b>		
Energy calibration	0.0016	0.0008
Line shape tail/total	0.0013	0.0003
511keV Compton summing	0.0002	0.0004
<b>Recoil Detector efficiency</b>		
MCP incident recoil angle	0.0006	0.0004
MCP incident ion energy	0.0010	0.0003
<b>Prompt peak</b>	0.0009	
<b>Transverse trap position</b>	+0.0000 -0.0004	
<b>Electron shake-off</b>	+0.0000 -0.0015	0.0003
<b>Total systematic error</b>	+0.0030 -0.0034	0.0012

- **Most errors determined by statistics-limited data evaluation.**
  - Further improvements: use all kinematic information.
    - Extend analysis to lower  $E_\beta$  to measure  $b$ .

# Limits on Scalar Interaction



## Polarization Observables

$$dW = dW_o \left( 1 + \frac{\vec{p}_\beta \cdot \vec{p}_\nu}{E_\beta E_\nu} a_{\beta\nu} + \frac{\Gamma m_e}{E_\beta} b + \frac{\vec{J}}{J} \cdot \left[ \frac{\vec{p}_\beta}{E_\beta} A_\beta + \frac{\vec{p}_\nu}{E_\nu} B_\nu + \frac{\vec{p}_\beta \times \vec{p}_\nu}{E_\beta E_\nu} D \right] \right. \\ \left. + c \left[ \frac{\vec{p}_\beta \cdot \vec{p}_\nu}{3E_\beta E_\nu} - \frac{(\vec{p}_\beta \cdot \vec{j})(\vec{p}_\nu \cdot \vec{j})}{E_\beta E_\nu} \right] \left[ \frac{J(J+1) - 3 \langle (\vec{J} \cdot \vec{j})^2 \rangle}{J(2J-1)} \right] \right)$$

$$\text{Asymmetry} = \frac{\sigma(\uparrow) - \sigma(\downarrow)}{\sigma(\uparrow) + \sigma(\downarrow)}$$

$\vec{J} \parallel \vec{P}_\beta \implies$  measure  $A_\beta$  ( $\beta$  singles or coin. with recoil)

$$\vec{J} \perp \vec{P}_\beta, \quad \vec{P}_\nu = \vec{P}_R - \vec{P}_\beta \implies dW \propto \frac{\vec{J}}{J} \cdot \left[ B_\nu \vec{P}_R + D \frac{(\vec{P}_\beta \times \vec{P}_R)}{E_\beta} \right]$$

Measure  $B_\nu$  from Recoil Asymmetry in  $\vec{P}_R \parallel \vec{J}$  plane

Measure  $D$  from Recoil Asymmetry in  $\vec{P}_R \perp \vec{J}$  plane

## Right-handed Currents

$$|W_L \rangle = \cos\zeta |W_1 \rangle - \sin\zeta |W_2 \rangle$$

$$|W_R \rangle = \sin\zeta |W_1 \rangle + \cos\zeta |W_2 \rangle$$

**Define:**  $x = (M_L/M_R)^2 - \zeta$  and  $y = (M_L/M_R)^2 + \zeta$

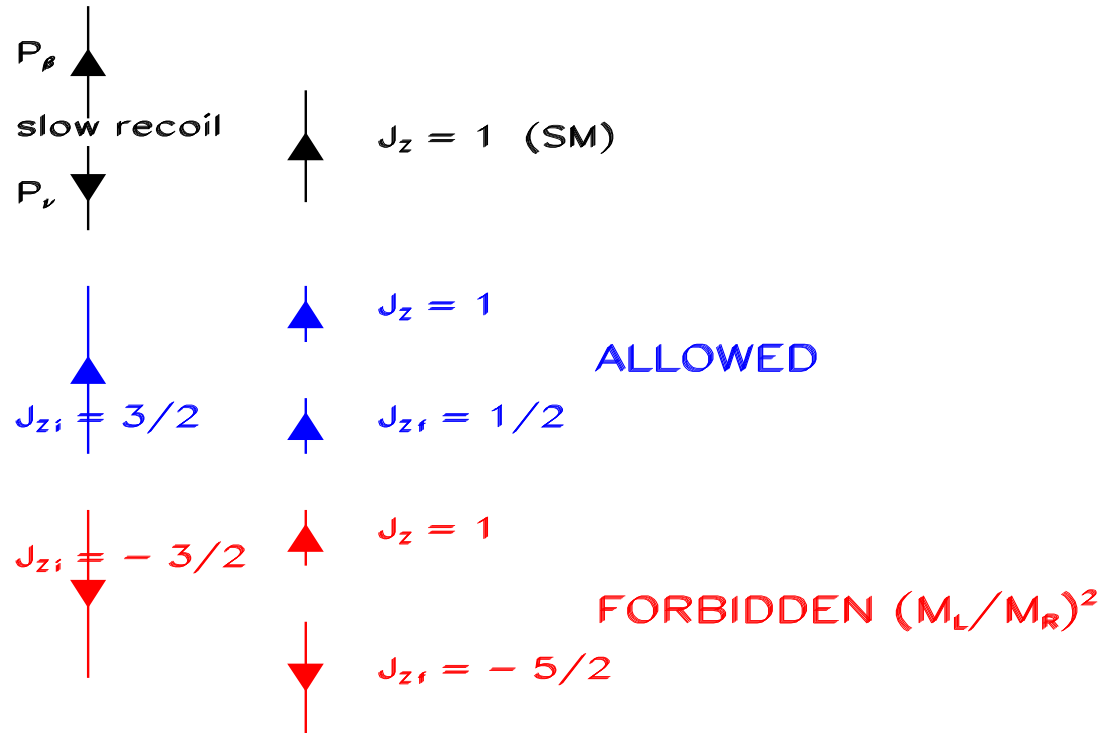
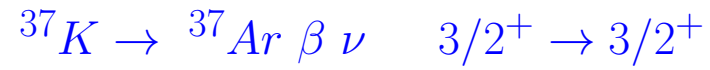
$$\lambda \equiv g_A M_{GT} / g_V M_F$$

$$A_\beta = \frac{-2\lambda}{1 + \lambda^2} \left[ \frac{\lambda(1 - y^2)}{5(1 + y^2)} - (1 - xy) \sqrt{\frac{3(1 + x^2)}{5(1 + y^2)}} \right]$$

$$B_\nu = \frac{-2\lambda}{1 + \lambda^2} \left[ \frac{\lambda(1 - y^2)}{5(1 + y^2)} + (1 - xy) \sqrt{\frac{3(1 + x^2)}{5(1 + y^2)}} \right]$$

$$R_{slow} \equiv \frac{dW(\vec{J} \cdot \vec{p}_\beta = -1)}{dW(\vec{J} \cdot \vec{p}_\beta = +1)} = \frac{1 - a - 2c/3 - (A + B)}{1 - a - 2c/3 + (A + B)} = y^2$$

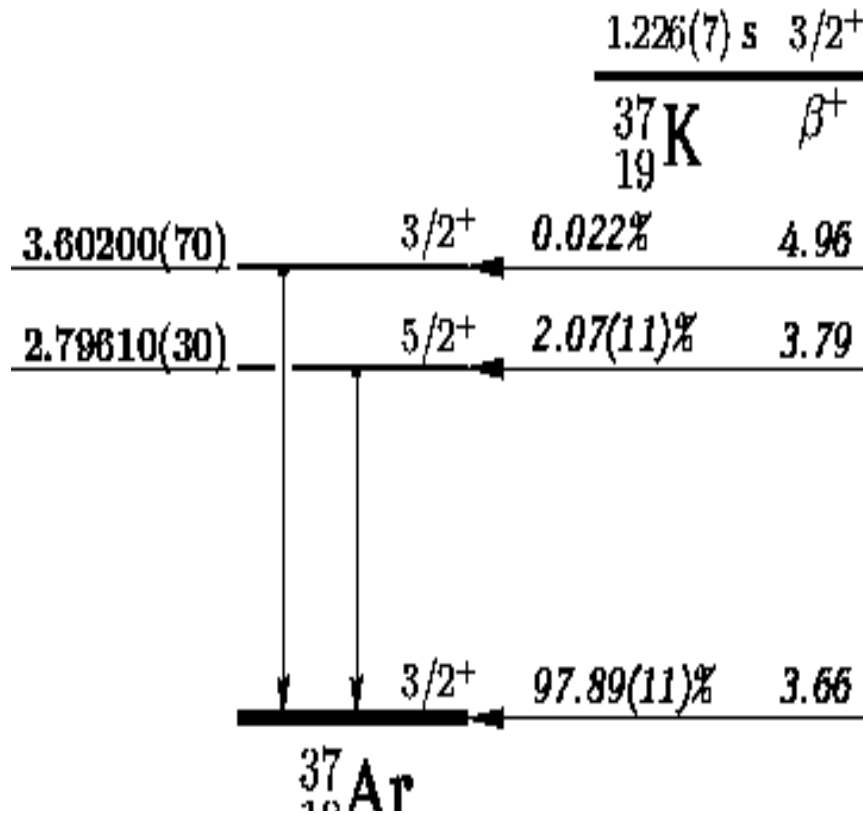
# The $R_{slow}$ Concept



# Measurement of $\beta - \nu$ Angular Correlation

in Polarized  $^{37}\text{K} \xrightarrow{\beta^+} ^{37}\text{Ar}$

More precise determination of decay branching ratios underway in Texas A & M University



$$Q(^{37}\text{K}) = 5.1265(15) \text{ MeV}$$

$$M_{GT}/M_F = -0.5754(16)$$

Hagberg et al.,  
Phys. Rev. C 56 (1997)

Coefficients of  $\beta - \nu$  Angular Correlation  
in Polarized  $^{37}\text{K} \xrightarrow{\beta^+} ^{37}\text{Ar}$

Calculated with the Standard Model assuming  
 $\lambda \equiv g_A M_{GT} / g_V M_F = -0.5754 \pm 0.0018$

Maximal Parity Violation

observable	$a_{\beta\nu}$	$A_\beta$	$B_\nu$	$c$
value	<b>0.6683</b>	<b>-0.5702</b>	<b>-0.7692</b>	<b>0.1990</b>
error <sup>1</sup>	<b>0.0013</b>	<b>0.0005</b>	<b>0.0013</b>	<b>0.0008</b>

<sup>1</sup> Due to error in  $\lambda$

$$b = D = R_{slow} = 0$$

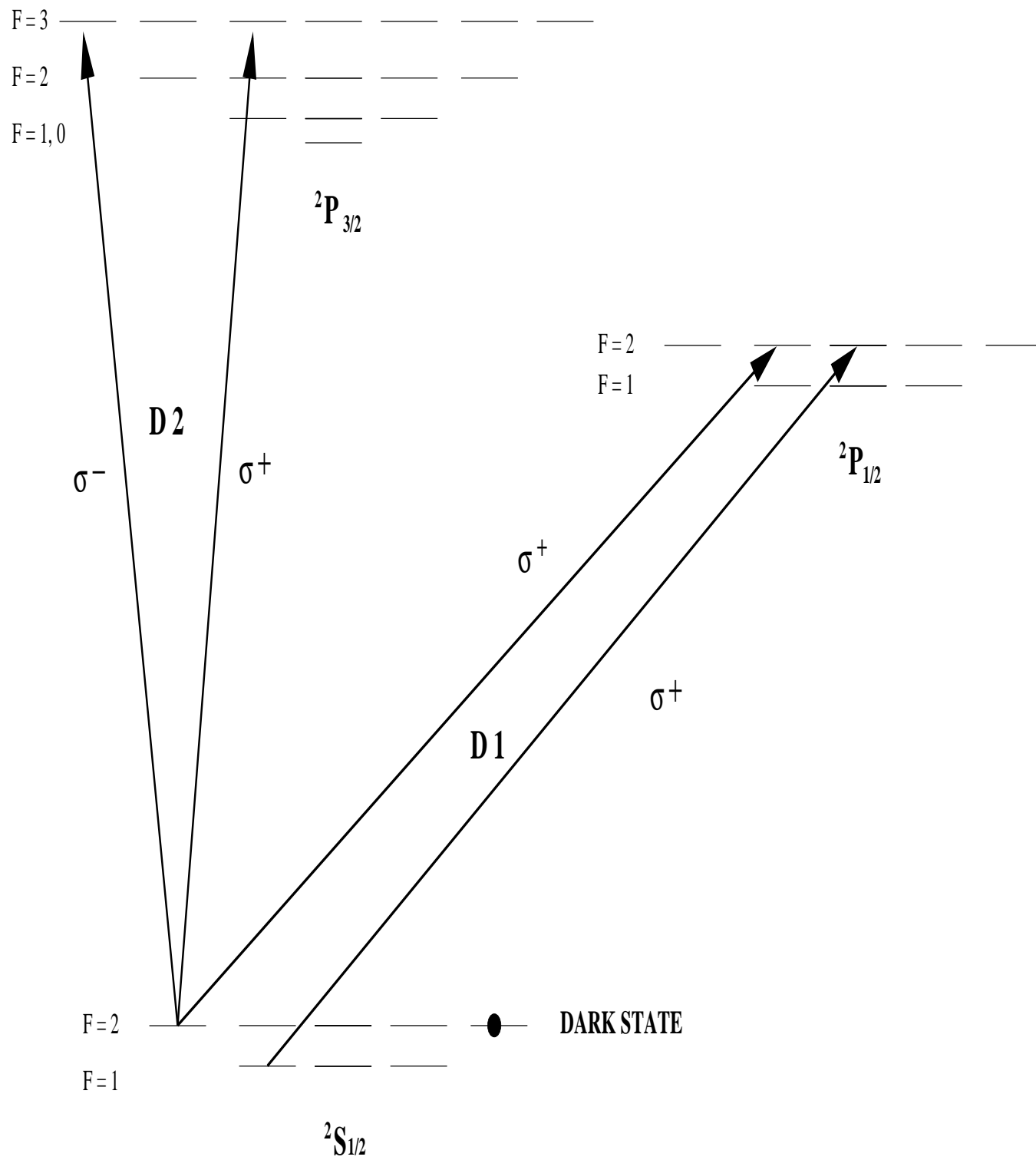
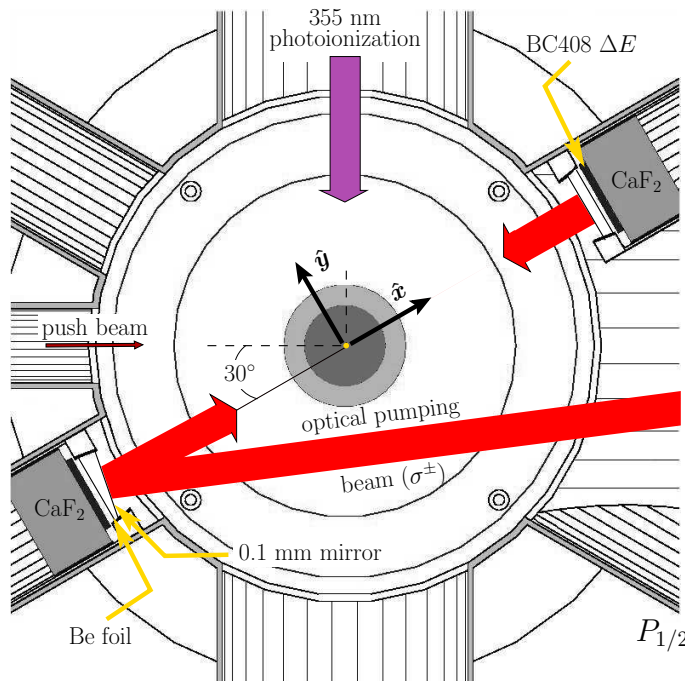


Figure 1: Hyperfine level scheme of the  $2S_{1/2}$  ground



# Optical Pumping



$\hat{x}$  = polarization axis  
 $\hat{y}$  = phoswich detector axis  
 $\hat{z}$  = MCP –  $\beta$ -telescope axis

can monitor  
 atomic fluorescence  
 via photoions



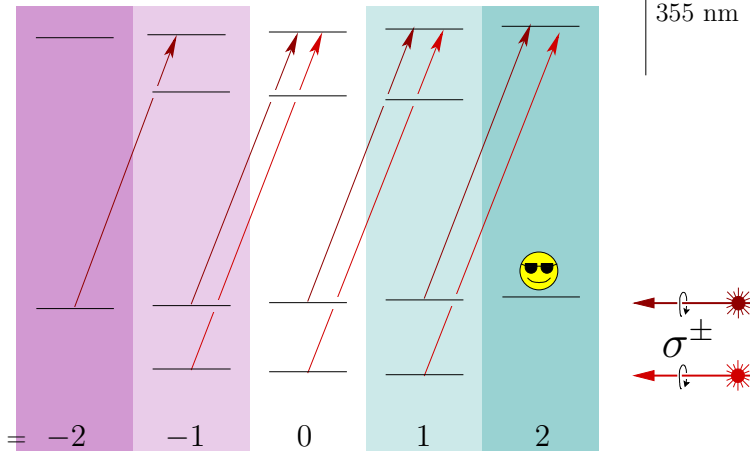
$$\vec{F} = \vec{I} + \vec{J}$$

$$I = \frac{3}{2}$$

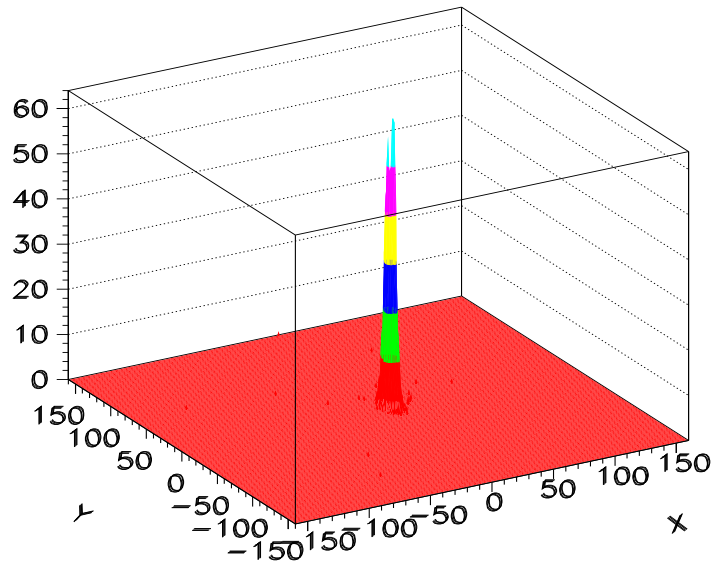
$$J = \frac{1}{2}$$

$$\vec{B}_{OP} = 2.5 \text{ G}$$

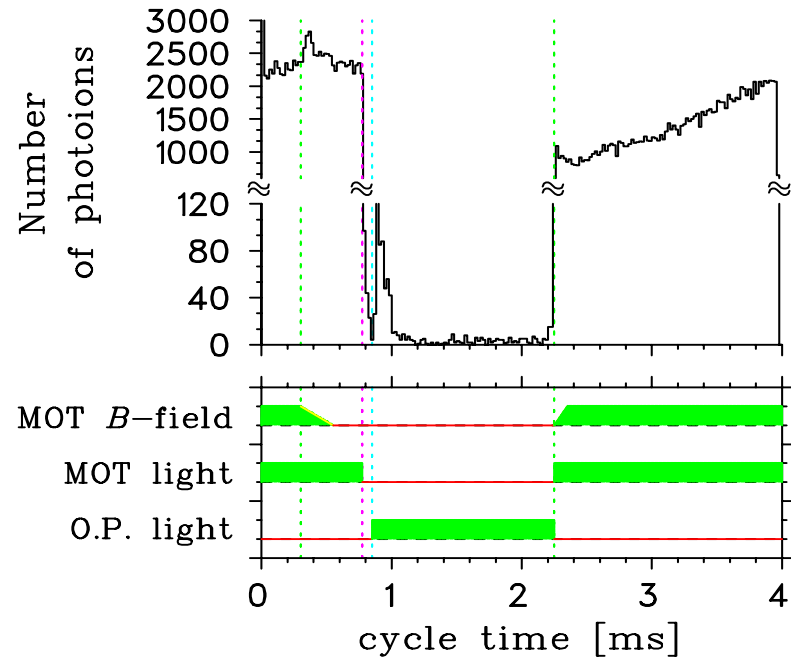
$$m_F = -2, -1, 0, 1, 2$$



# Determination of the Polarization

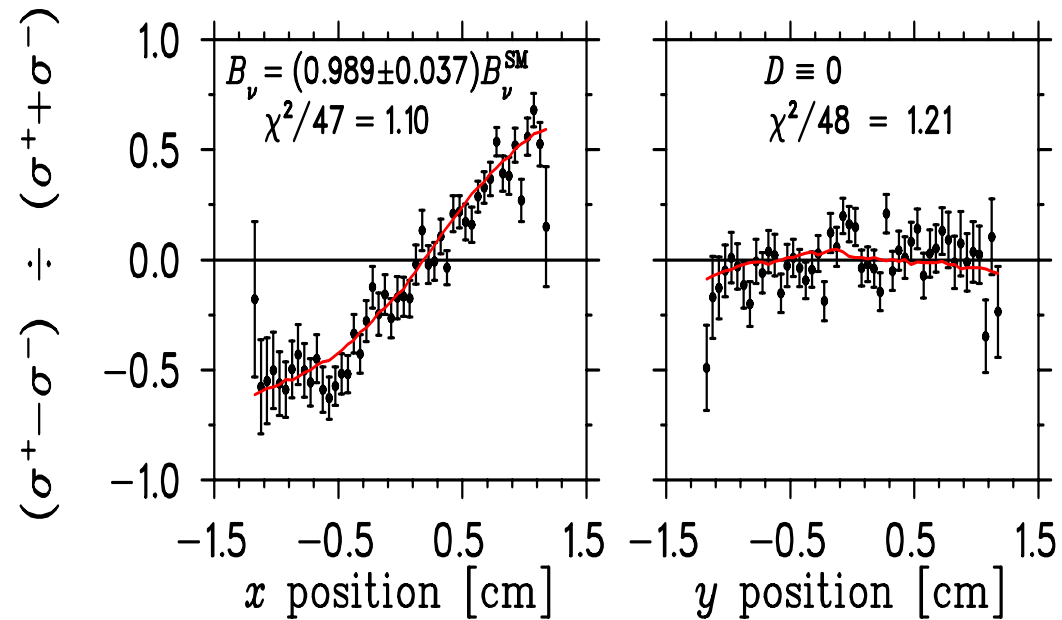


Photoions detected in MCP



Trap Cycle

Measure  $B_\nu$  from Recoil Asymmetry in  $\hat{x} - \hat{z}$  plane  
 Measure  $D$  from Recoil Asymmetry in  $\hat{y} - \hat{z}$  plane



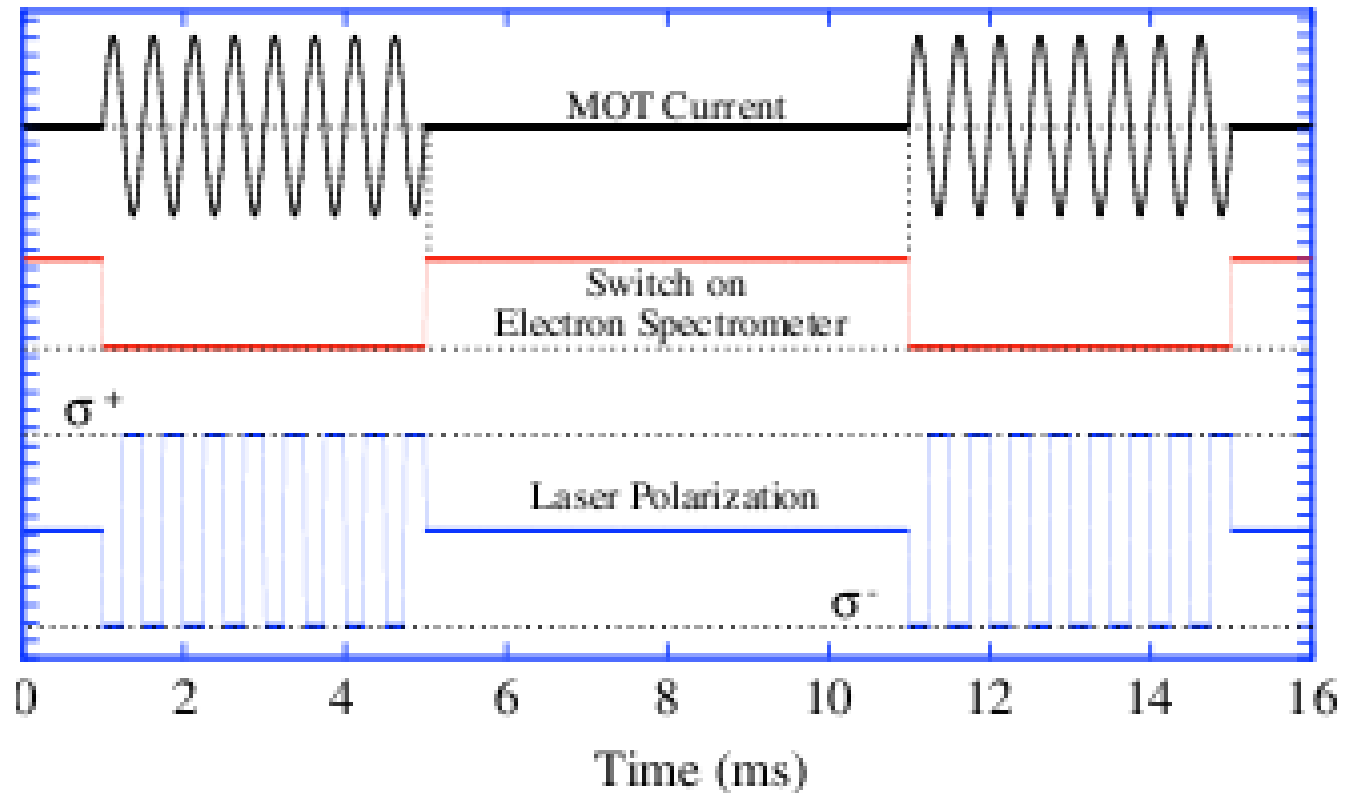
$$B_\nu = 0.755 \pm 0.020(\text{stat}) \pm 0.013(\text{syst})$$

**D. Melconian et al. PL B 649, 370 (2007)**

# Upgraded Experimental System

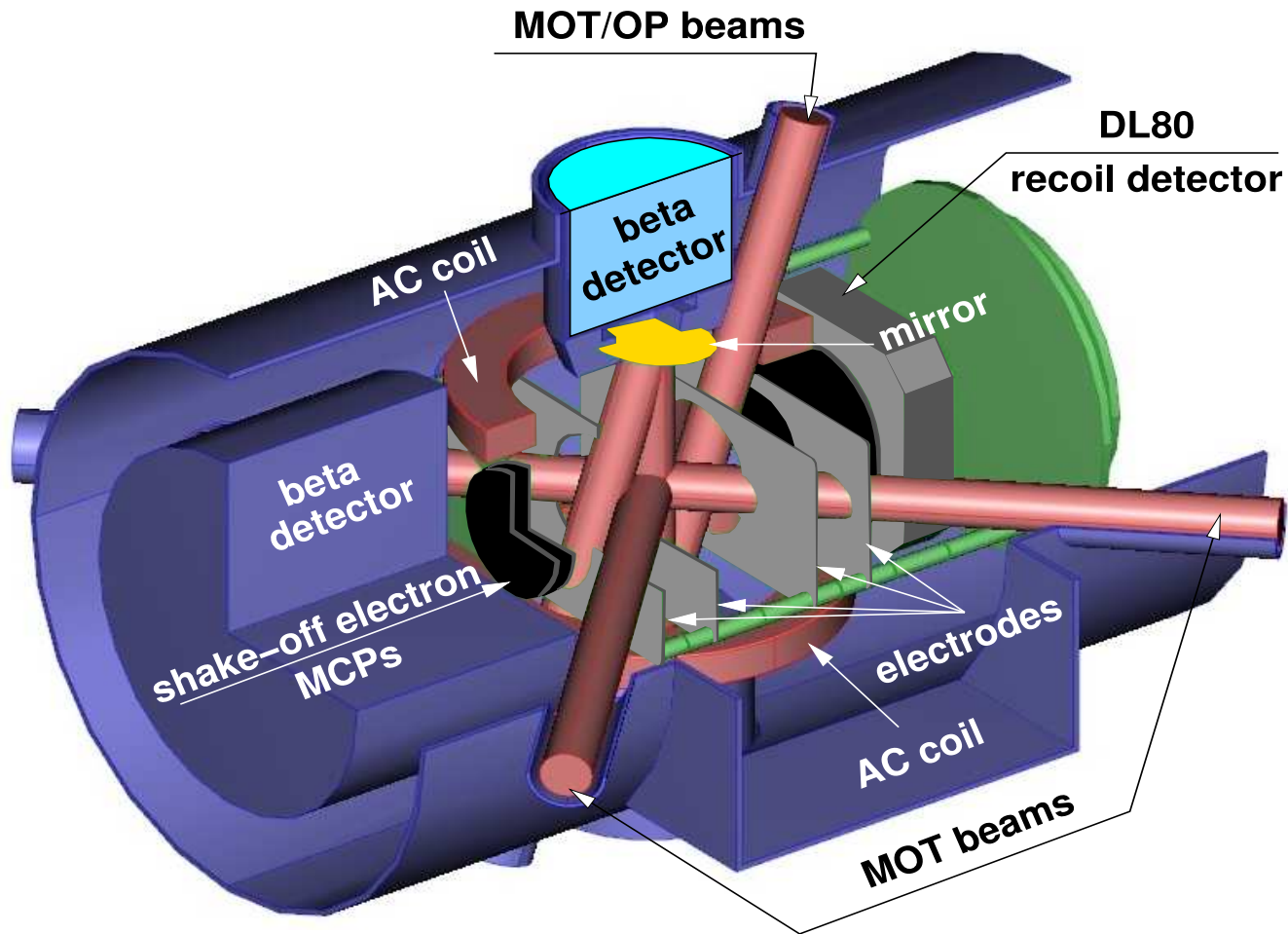
- Reduce all systematic and statistical errors:
- New, larger MCP detector and  $\beta$  telescope - near 100% acceptance for ions. Improved low  $E_\beta$  detection for Fierz term measurement.
- **New polarization detectors with Si MSD and plastic scintillator. Position information and better resolution.**
- Time and momentum focusing for better resolution and charge state separation.
- **Shakeoff electron detection for background suppression.**
- **Better trapping/polarization cycle by using AC MOT.**
- Higher beam intensity:  $40\mu A$  vs.  $1\mu A$  in previous experiment.
- New chamber design to accomodate all the above.

# The principle of AC MOT

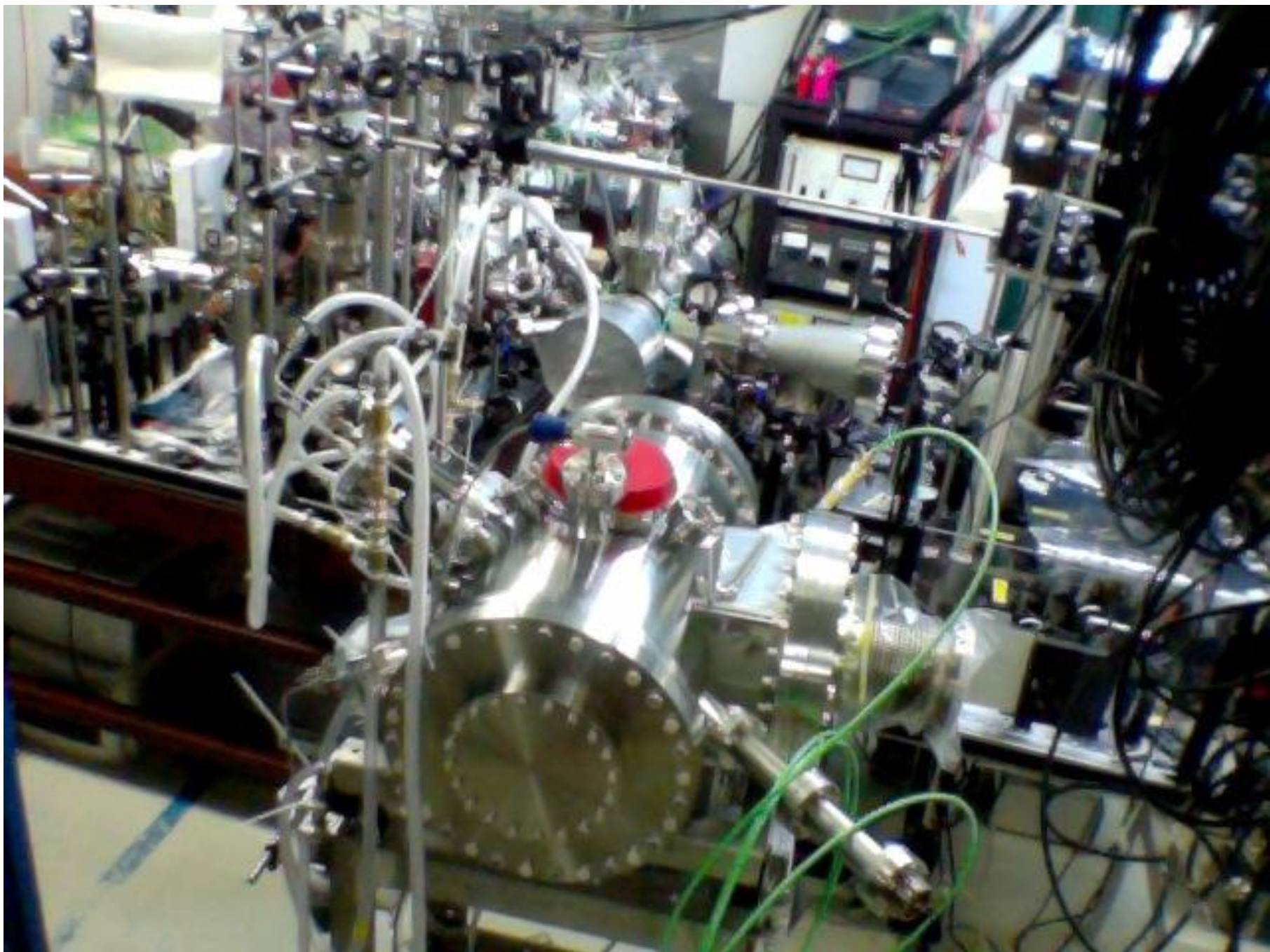


**M. Harvey and A.J. Murray Phys. Rev. Lett. 101, 173201 (2008)**

# NEW DETECTION CHAMBER FOR $^{37}\text{K}$

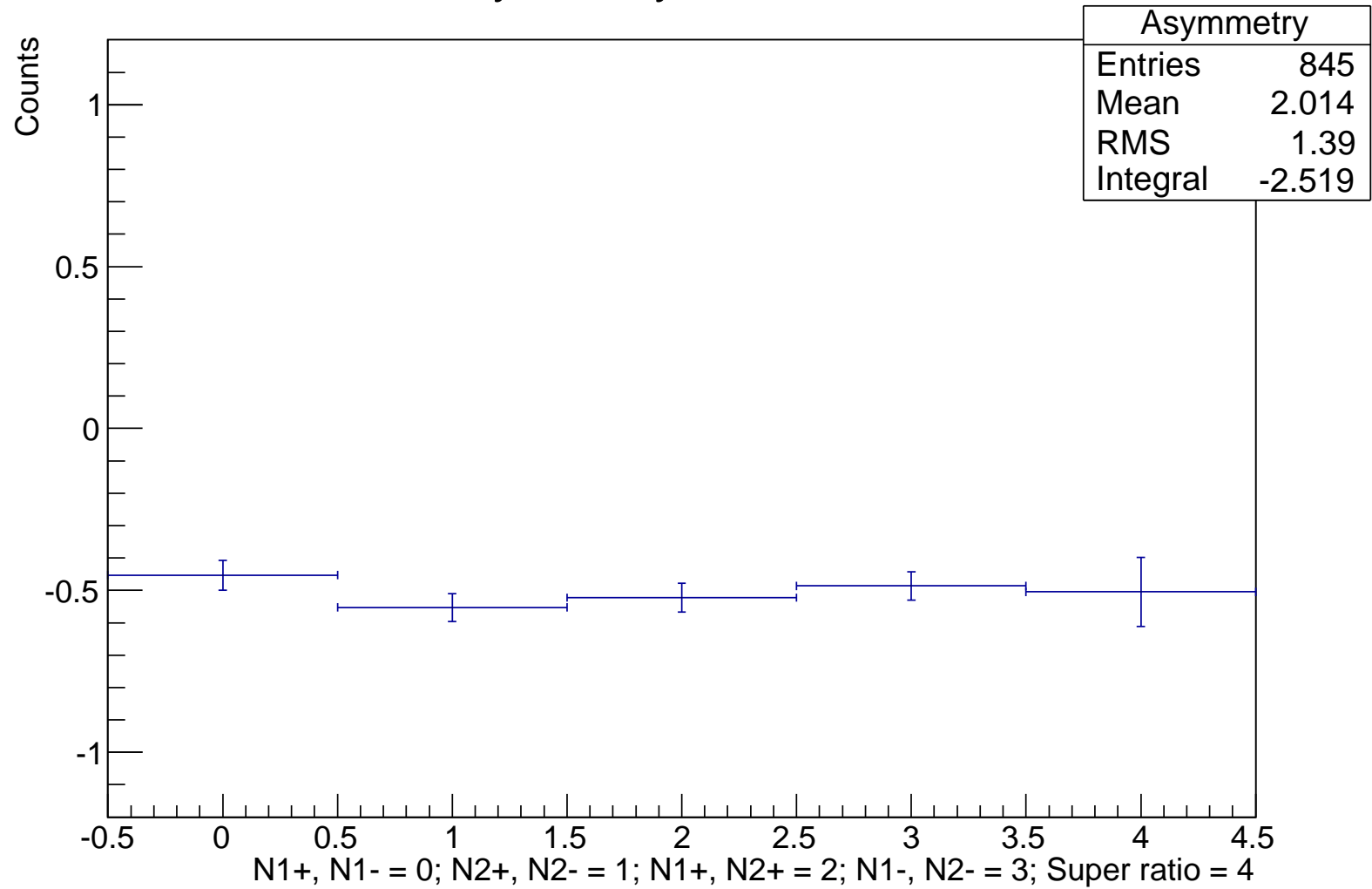


- Position sensitivity on all beta and recoil detectors
- Larger beta and recoil detectors will improve statistics
- AC MOT will speed up switching from MOT cycle to OP cycle
- Improvement of a weak magnetic field during OP will improve polarization
- Coincidences with shake off electron MCP will reduce background for competitive measurements of beta asymmetry



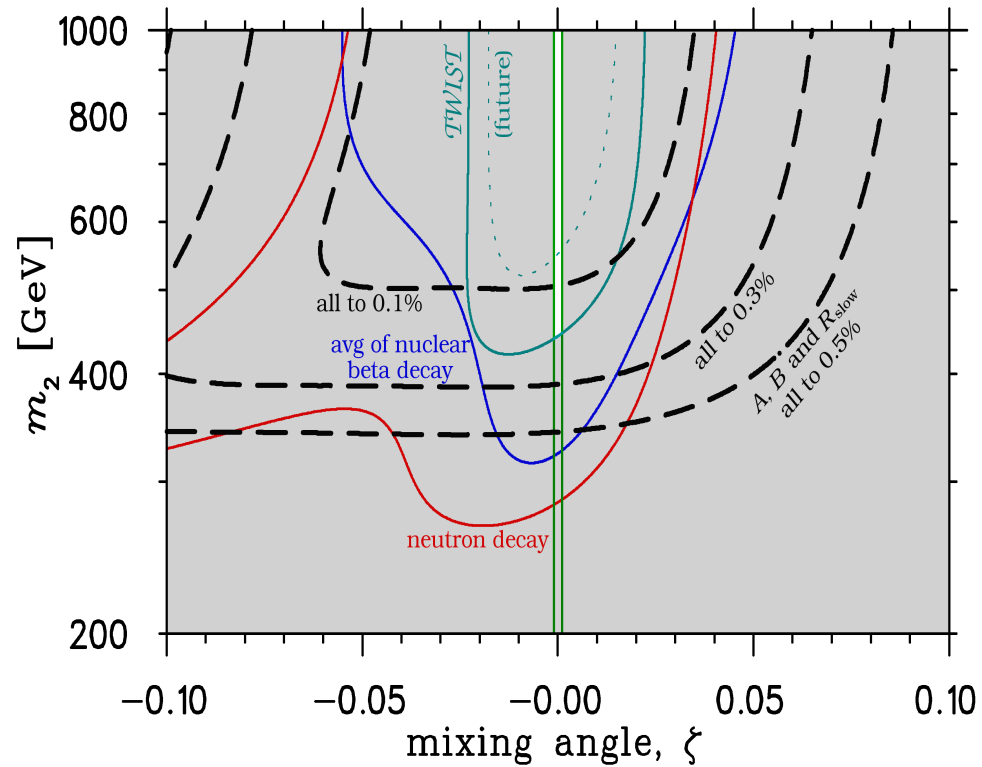
# JUST MEASURED

## Asymmetry\_Run\_0782





## Limits on Right-Handed Currents



## Tensor Interaction

The angular distribution of recoiling daughter nuclei of polarized  $\beta$  emitters, S.B. Treiman PR 110, 448 (1957):

$$W(\theta_r)d(\cos \theta_r) = \left\{1 + \frac{1}{3}c'\chi_2 - P(A_\beta + B_\nu)\chi_1 \cos \theta_r - c'\chi_2 \cos^2 \theta_r\right\}d(\cos \theta_r)$$

$$\chi_1, \chi_2 \text{ kinematical functions, } c' = c \frac{J(J+1) - 3\langle(\vec{J}\cdot\vec{j})^2\rangle}{J(2J-1)}.$$

For pure GT transitions and no Tensor Interaction:  $A_\beta + B_\nu = 0$

$$5/8(A_\beta + B_\nu) = 2C_T C'_T + \frac{m_\beta}{E_\beta}(C_T - C'_T)$$

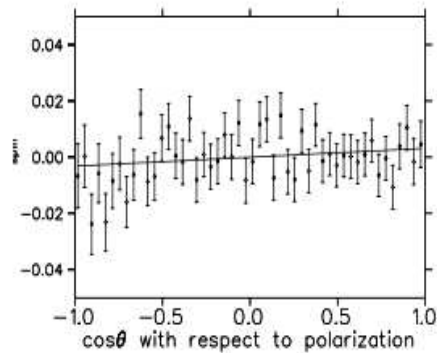
And can be deduced from Asymmetry measurements:

$$A_{\text{spin}} = \frac{W[\theta, P] - W[\theta, -P]}{W[\theta, P] + W[\theta, -P]} = \frac{\chi_1 P(A_\beta + B_\nu) \cos \theta}{1 + c'\chi_2 + c'\chi_2 \cos^2 \theta}$$

Insensitive to Right-Handed currents; constrains Tensor Interaction

Using recoil momentum information enhances the sensitivity and allows separation of SM recoil-order corrections

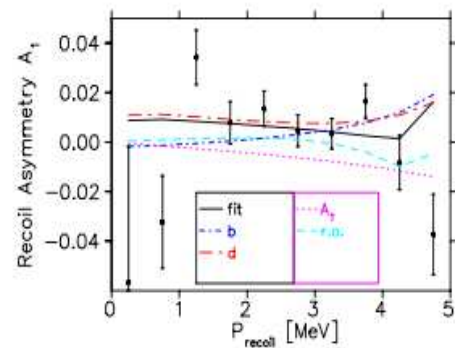
(O. Aviv, MSc. Thesis, Tel Aviv University (2004)):



$$A_{spin}(P_R) = \frac{(f_4(A_\beta + B_\nu) - f_7b)P\cos\theta}{f_1 - f_6b - f_2(a_{\beta\nu} + c'/3) + c'(f_3 + f_5\cos^2\theta)}$$

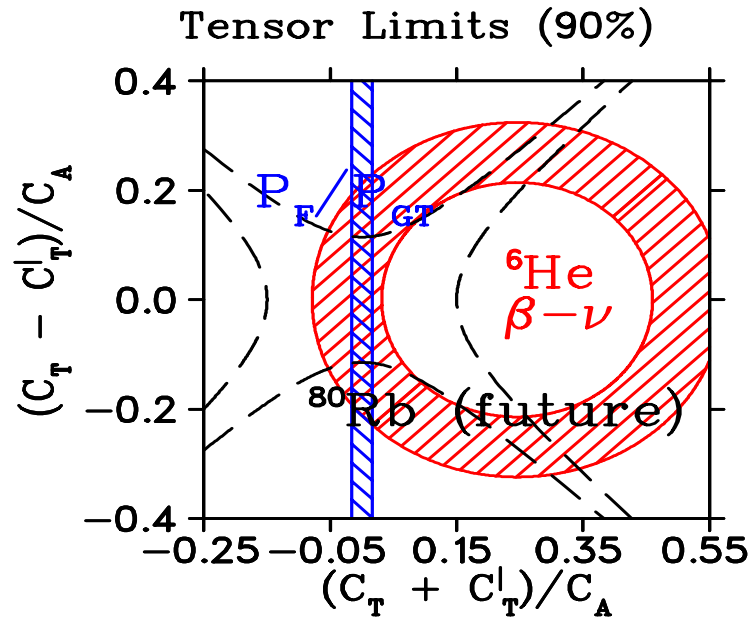
$f_i(P_R)$  : Calculated functions of recoil momentum

Use polarized  $^{80}\text{Rb}$ ,  $1^+ \rightarrow 0^+$  pure GT transition.  $\mathbf{P}_{Recoil}$  from TOF to Shakeoff  $e^-$  MCP



$(A_\beta + B_\nu) = 0.015 \pm 0.029$  arXiv: 0811.0052 [nucl-ex],

J.R.A. Pitcairn *et al.*, Phys. Rev. C79, 015501 (2009)



Experimental precision better by an order of magnitude, **BUT:**

Constraints on Tensor Interaction dominated by theoretical uncertainties in Recoil-Order corrections

# SUMMARY

- Studies of  $\beta$  decay of trapped radioactive nuclei provide constraints on the Standard Model
- Next generation experiments will provide tighter constraints, complementary to measurements with HE accelerators

$$\begin{aligned}
\xi &= |M_F|^2(|C_S|^2 + |C_V|^2 + |C'_S|^2 + |C'_V|^2) + |M_{GT}|^2(|C_T|^2 + |C_A|^2 + |C'_T|^2 + |C'_A|^2) \\
a_{\beta\nu}\xi &= |M_F|^2(-|C_S|^2 + |C_V|^2 - |C'_S|^2 + |C'_V|^2) + \frac{|M_{GT}|^2}{3}(|C_T|^2 - |C_A|^2 + |C'_T|^2 - |C'_A|^2) \\
b\xi &= \pm 2\text{Re}[|M_F|^2(C_S C_V^* + C'_S C_V'^*) + |M_{GT}|^2(C_T C_A^* + C'_T C_A'^*)] \\
c\xi &= |M_{GT}|^2 \Lambda_{J'J}(|C_T|^2 - |C_A|^2 + |C'_T|^2 - |C'_A|^2) \\
A_\beta\xi &= 2\text{Re}[\pm |M_{GT}|^2 \lambda_{J'J}(C_T C_T'^* - C_A C_A'^*) + \delta_{J'J} |M_{GT}| |M_F| \sqrt{J/(J+1)}(C_S C_T'^* \\
&\quad + C'_S C_T^* - C_V^* C_A'^* - C'_V C_A^*)] \\
B_\nu\xi &= 2\text{Re}\{|M_{GT}|^2 \lambda_{J'J} [\frac{m_e}{E_e}(C_T C_A'^* + C'_T C_A^*) \pm (C_T C_T'^* + C_A C_A'^*)] \\
&\quad - \delta_{J'J} |M_{GT}| |M_F| \sqrt{J/(J+1)} \times [(C_S C_T'^* + C'_S C_T^* + C_V C_A'^* + C'_V C_A^*) \\
&\quad \pm \frac{m}{E_e}(C_S C_A'^* + C'_S C_A^* + C_V C_T'^* + C'_V C_T^*)]\} \\
D\xi &= 2\text{Im}\{\delta_{J'J} |M_F| |M_{GT}| \sqrt{\frac{J}{J+1}}(C_S C_T^* + C'_S C_T'^* - C_V C_A^* - C'_V C_A'^*)\}
\end{aligned}$$

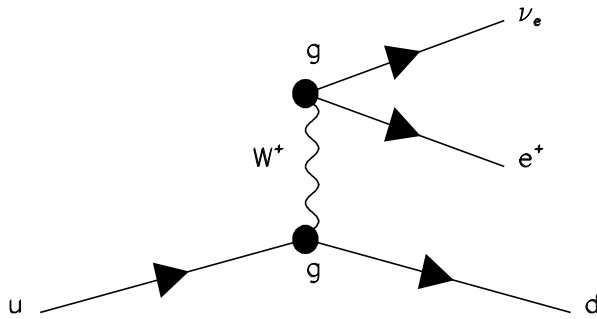
$$\lambda_{J'J} = \begin{cases} 1, & J \rightarrow J' = J - 1 \\ \frac{1}{J+1}, & J \rightarrow J' = J \\ -\frac{J}{J+1}, & J \rightarrow J' = J + 1 \end{cases}$$

$$\Lambda_{J'J} = \begin{cases} 1, & J \rightarrow J' = J - 1 \\ -\frac{2J-1}{J+1}, & J \rightarrow J' = J \\ \frac{J(2J-1)}{(2J+3)(J+1)}, & J \rightarrow J' = J + 1 \end{cases}$$

$C_i$ : Interaction Amplitudes (complex)

$$\begin{aligned}
C_V &= g_V(a_{LL} + a_{LR} + a_{RR} + a_{RL}) & C'_V &= g_V(a_{LL} + a_{LR} - a_{RR} - a_{RL}) \\
C_A &= g_A(a_{LL} - a_{LR} + a_{RR} - a_{RL}) & C'_A &= g_A(a_{LL} - a_{LR} - a_{RR} + a_{RL}) \\
C_S &= g_S(A_{LL} + A_{LR} + A_{RR} + A_{RL}) & C'_S &= g_S(A_{LL} + A_{LR} - A_{RR} - A_{RL}) \\
C_T &= 2g_T(\alpha_{LL} + \alpha_{RR}) & C'_T &= 2g_T(\alpha_{LL} - \alpha_{RR})
\end{aligned}$$

$g_i$  : Hadronic Form Factors       $a_{ij}$  : Chirality coupling constants     $i : \nu$      $j : \text{quark}$



**Standard Model: V - A,  
left handed**

$$g_V = 1, \quad g_A = -1.27 \text{ (n decay)}$$

$$a_{LL} = V_{ud} \frac{g^2}{8M_W^2} \cong 8 \cdot 10^{-6} \text{ GeV}^{-2}$$

$$a_{ij}, A_{i,j}, \alpha_{i,j} = 0 \quad i, j \neq L, L$$

$$a_{\beta\nu} = \frac{y^2 - \frac{1}{3}}{y^2 + 1}, \quad y = \frac{C_V M_F}{C_A M_{GT}}$$

$$b = 0$$

$$c = \frac{-\Lambda_{JJ'}}{1 + y^2}$$

$$A_\beta = \frac{\mp \lambda_{JJ'} - 2\delta_{JJ'} y \sqrt{J/(J+1)}}{y^2 + 1}$$

$$B_\nu = \frac{\pm \lambda_{JJ'} - 2\delta_{JJ'} y \sqrt{J/(J+1)}}{y^2 + 1}$$

$$D = 0$$

